

Animating Virtual Characters

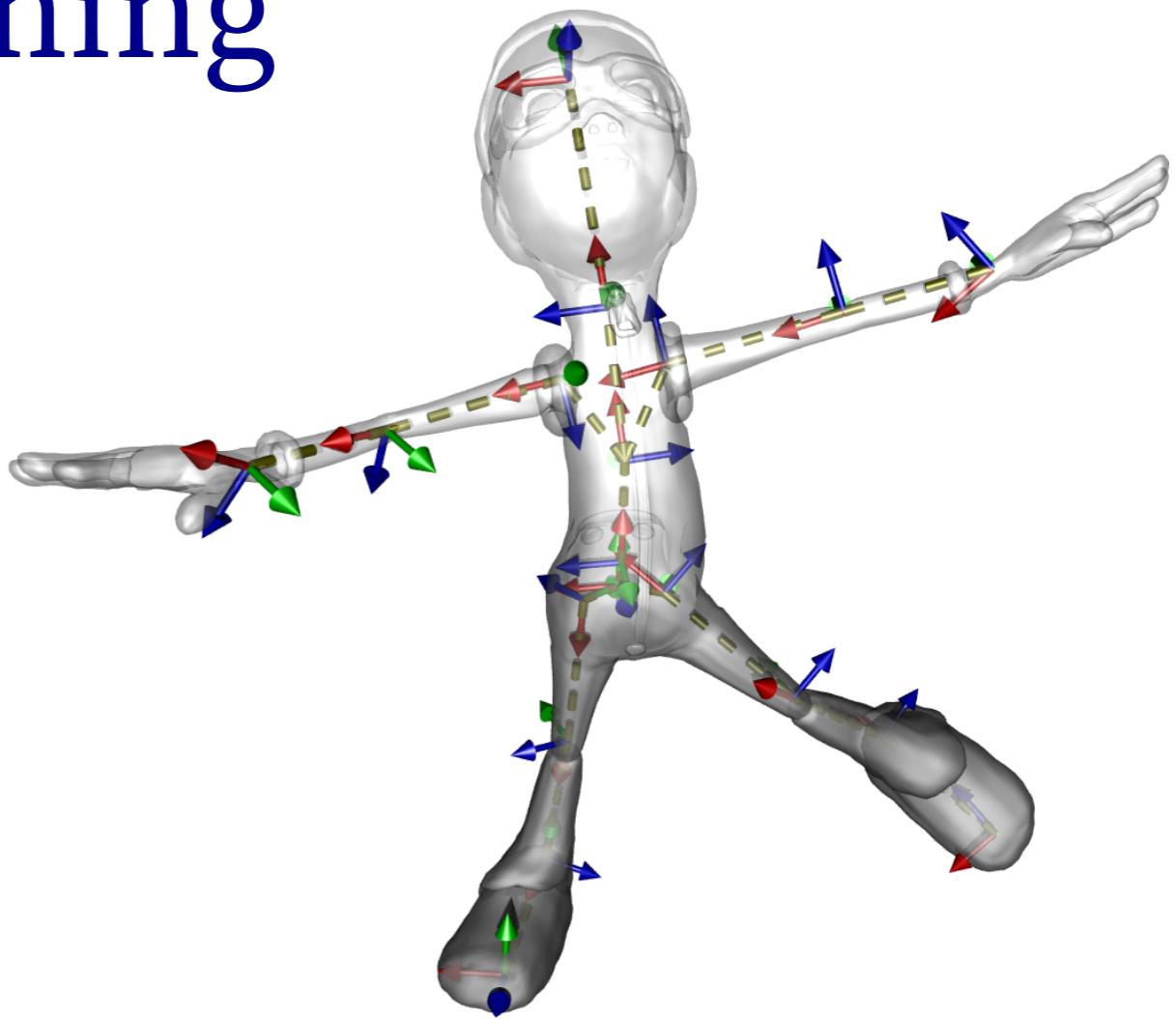
Skin deformation

Skeleton based deformation - Skinning

Objective: Deform articulated character

Idea: Use skeleton to control limbs

Articulations as rotations



Animation Skeleton

Set of frames T_i : position, orientation

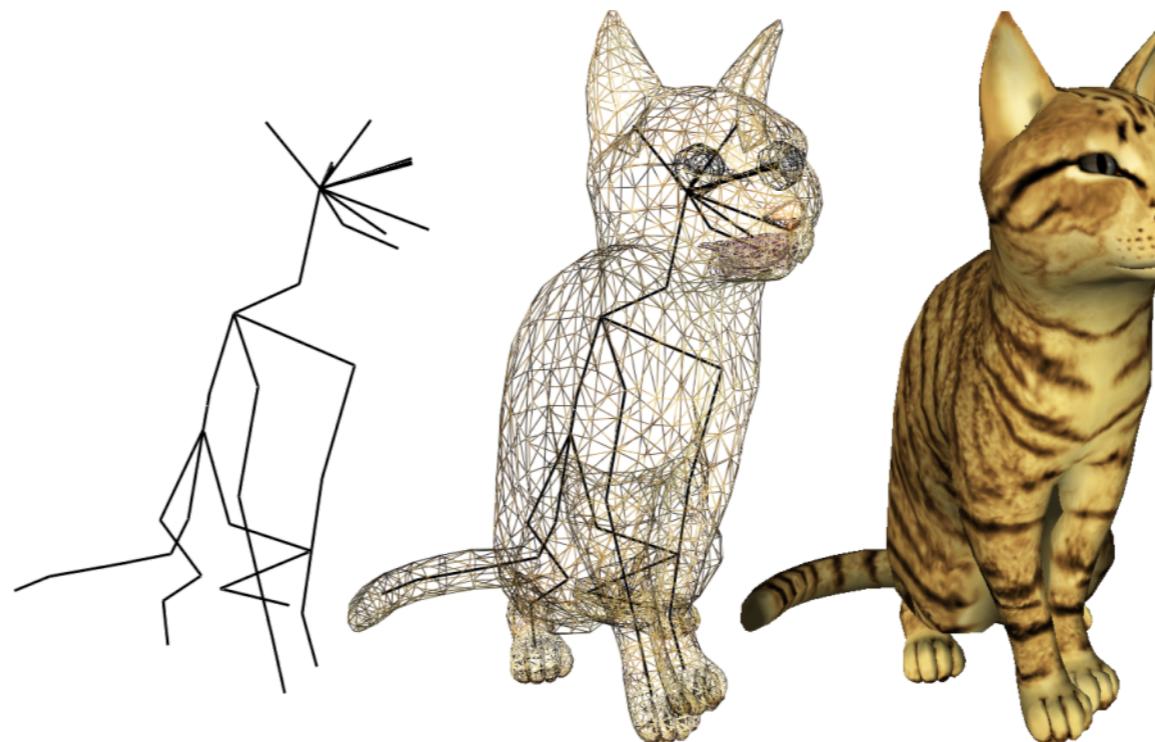
Describe non-rigid parts of the character (dof)

Terminology

Joint = A frame T_i

Bone = Segment between two joints

Note: Animation skeleton \neq Anatomical skeleton



Rigid Skinning

Attach rigidly subset of vertices to specific bones, described by its root joint/frame.

Vertices are following rigid deformation of their associated frame.

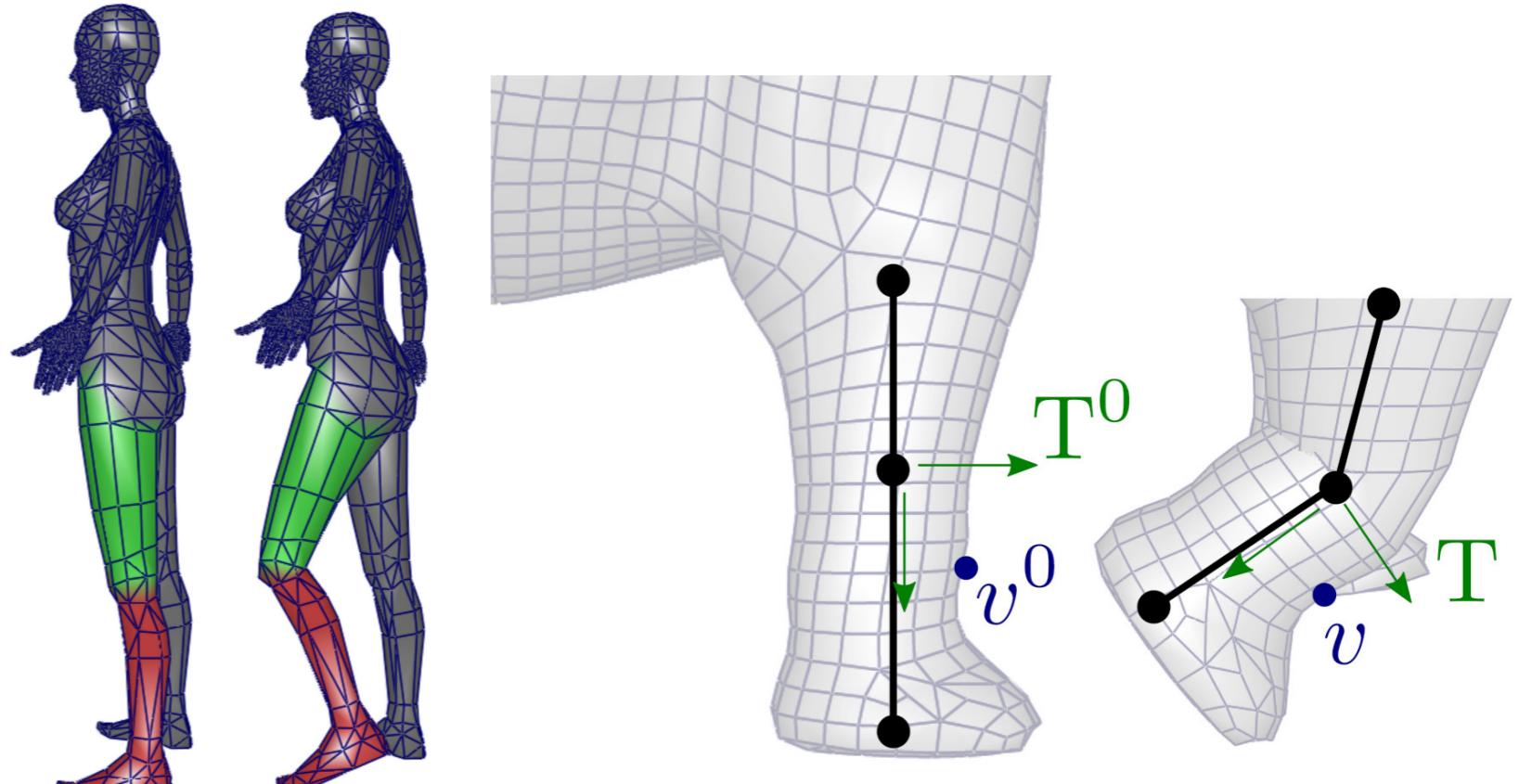
Deformation formulation

Consider, at rest pose/initial state

- A frame T^0
- A vertex v^0 attached to this frame

After deformation

- New frame T
- New vertex position v



Question: What are the new coordinates v w/r T, T^0, v^0 ?

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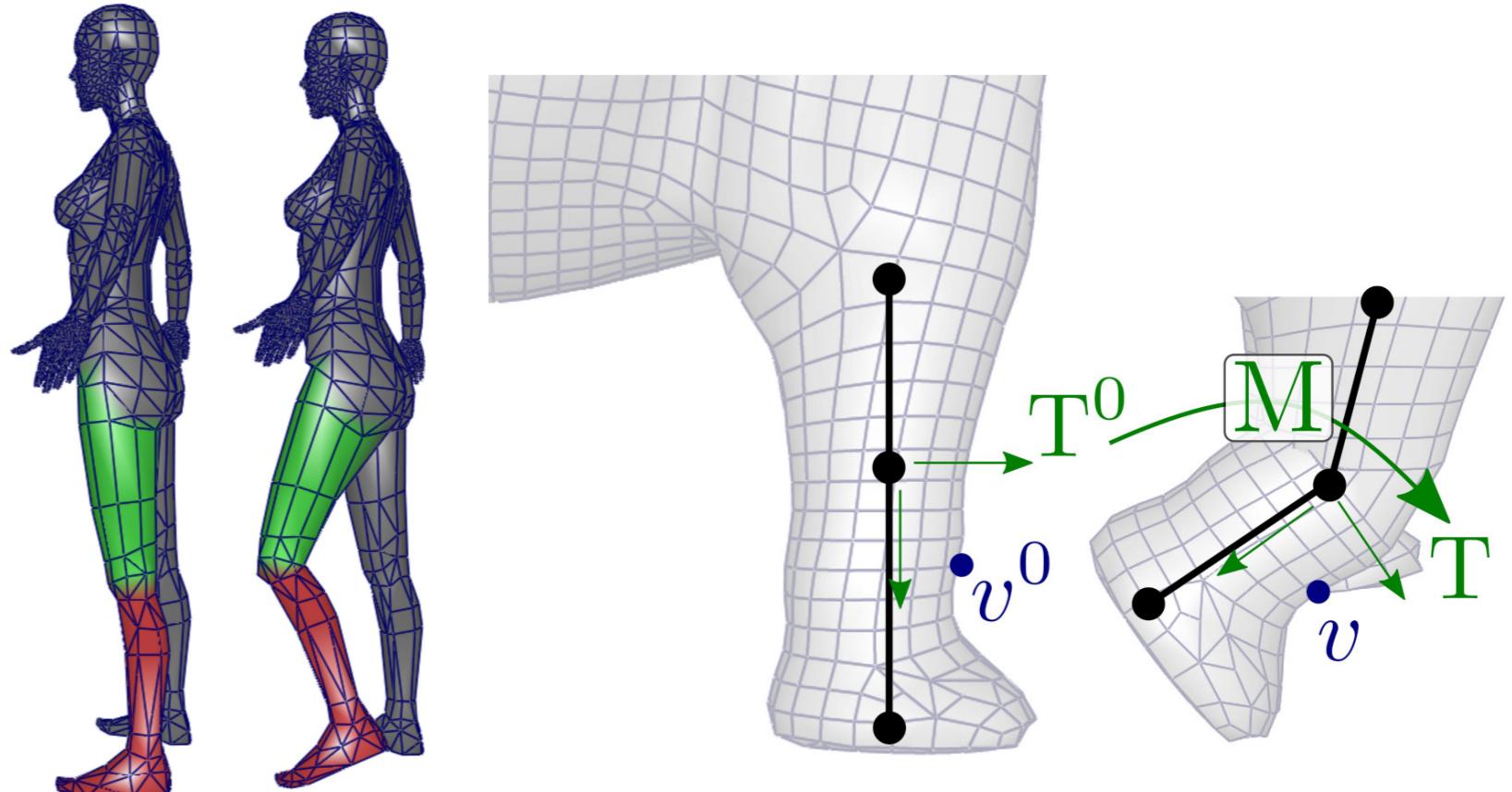
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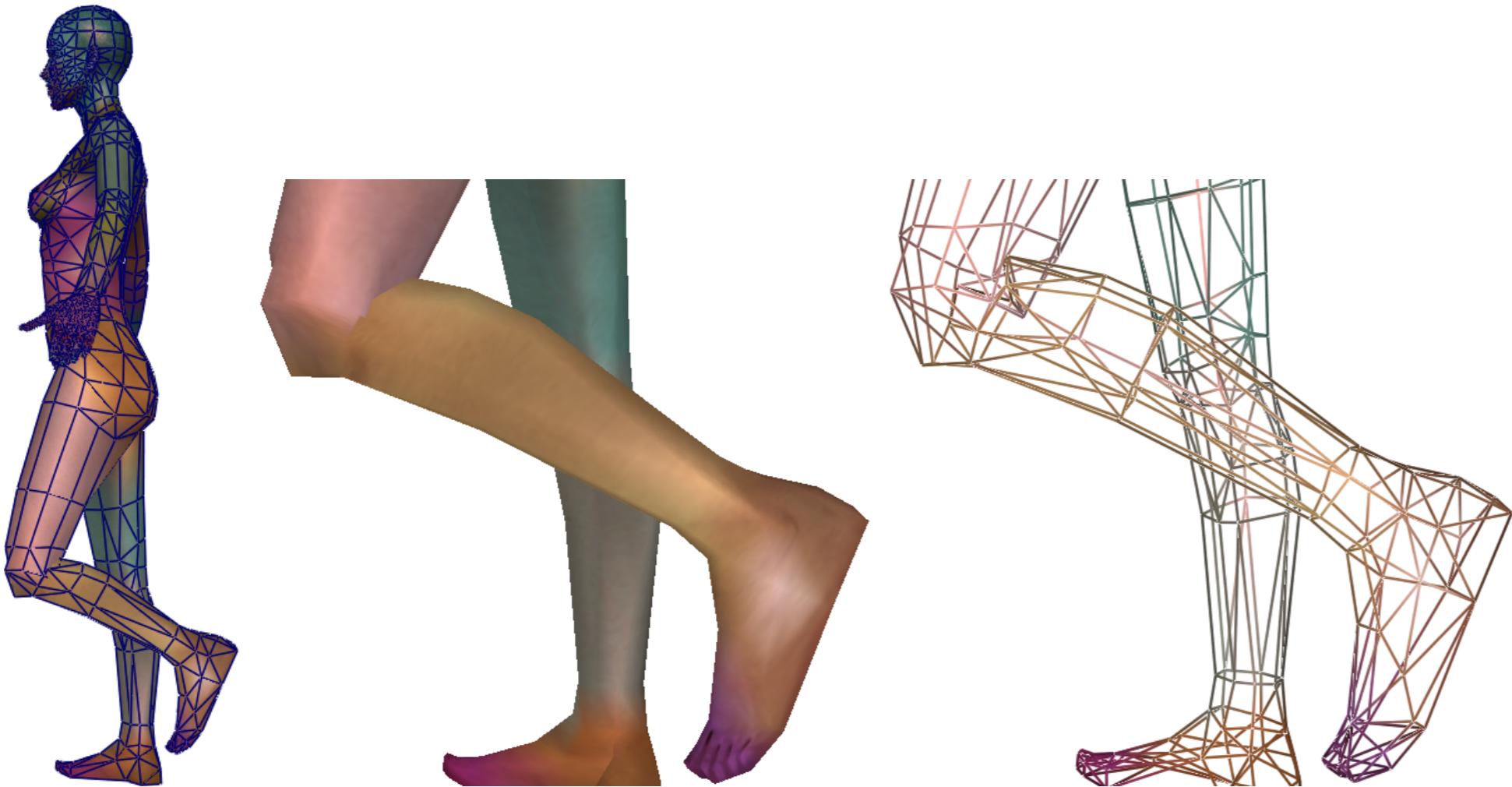
v^0 and v have similar local coordinates w/r to T^0 and T

$$\Rightarrow T^{-1}v = (T^0)^{-1}v^0$$

$$\Rightarrow v = T (T^0)^{-1}v^0 = M v^0$$

Rigid Skinning

- (+) Skeleton is easy to build
- (+) Skeleton interaction is intuitive to model rigid articulation
- (-) Discontinuities/Inter-penetrations



Idea of smooth skinning: Blend discontinuous transformation around articulation

Smooth skinning

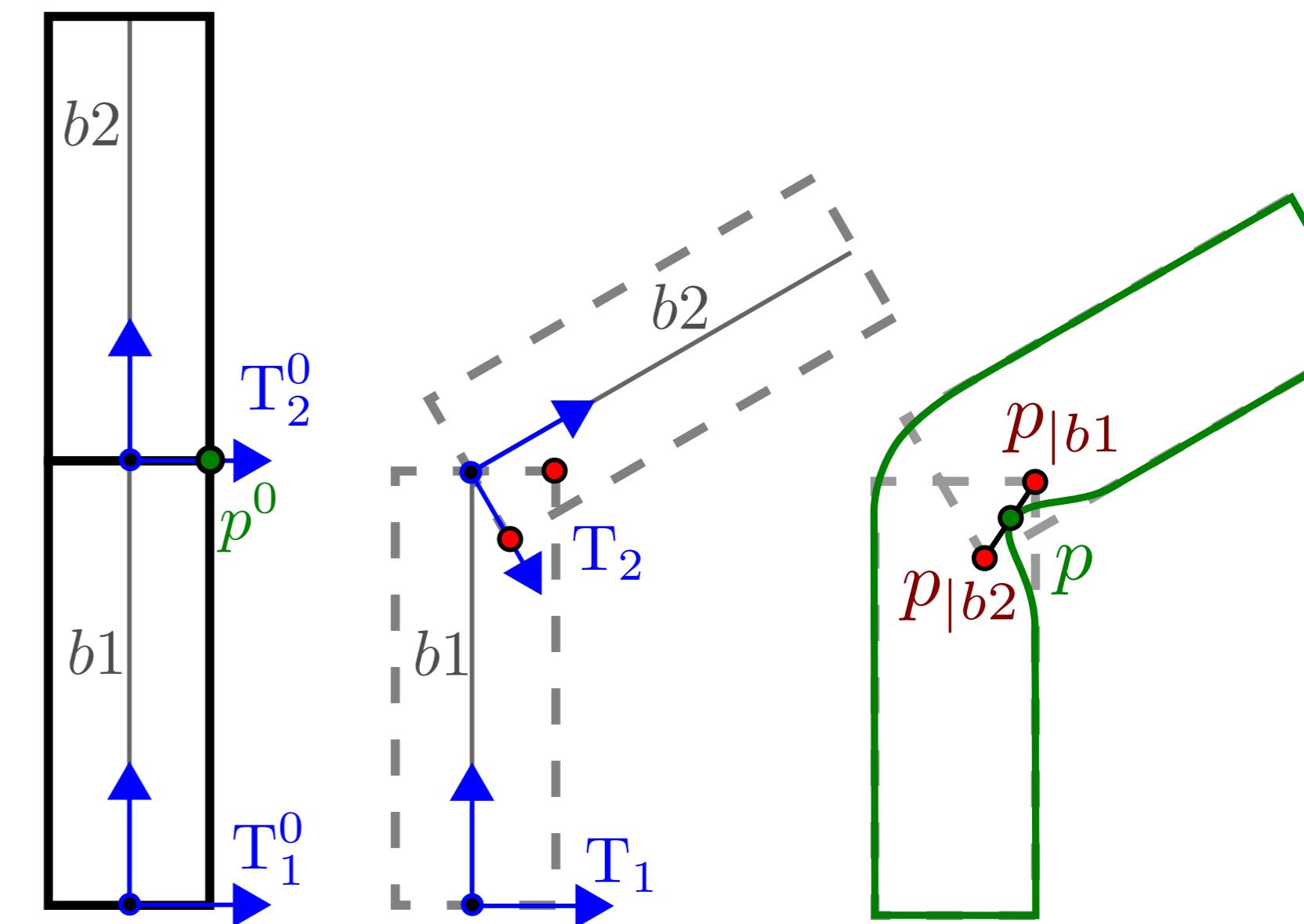
Linear Blend Skinning (LBS): Linear interpolation of positions between associated frames

Example at middle vertex position of a bending cylinder

$$p = 0.5 p_{|b1} + 0.5 p_{|b2}$$

$$p = \underbrace{0.5 T_1 (T_1^0)^{-1} p^0}_{M_1} + \underbrace{0.5 T_2 (T_2^0)^{-1} p^0}_{M_2}$$

$$p = (0.5 M_1 + 0.5 M_2) p^0$$



Smooth skinning

Linear Blend Skinning (LBS): Linear interpolation of positions between associated frames

Example at middle vertex position of a bending cylinder

$$\begin{aligned} p &= 0.5 p_{|b1} + 0.5 p_{|b2} \\ p &= 0.5 \underbrace{\mathbf{T}_1 (\mathbf{T}_1^0)^{-1}}_{\mathbf{M}_1} p^0 + 0.5 \underbrace{\mathbf{T}_2 (\mathbf{T}_2^0)^{-1}}_{\mathbf{M}_2} p^0 \\ p &= (0.5 \mathbf{M}_1 + 0.5 \mathbf{M}_2) p^0 \end{aligned}$$

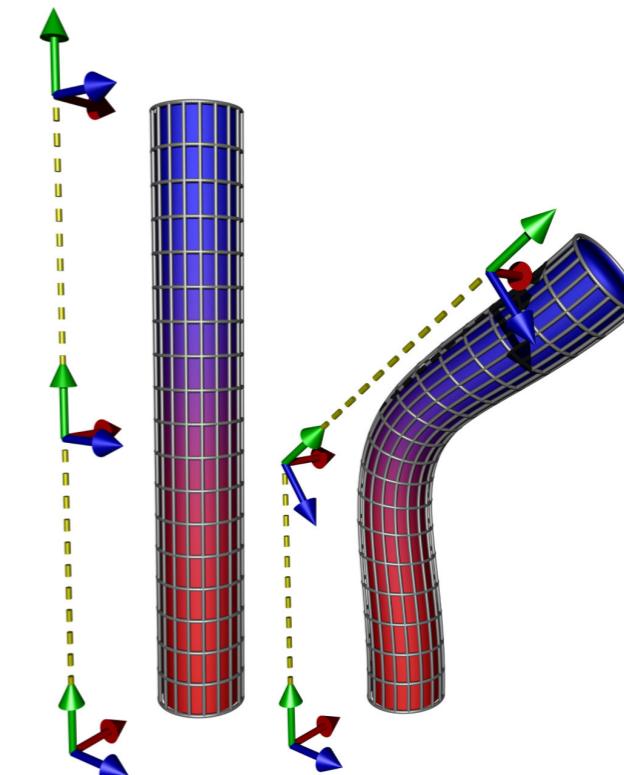
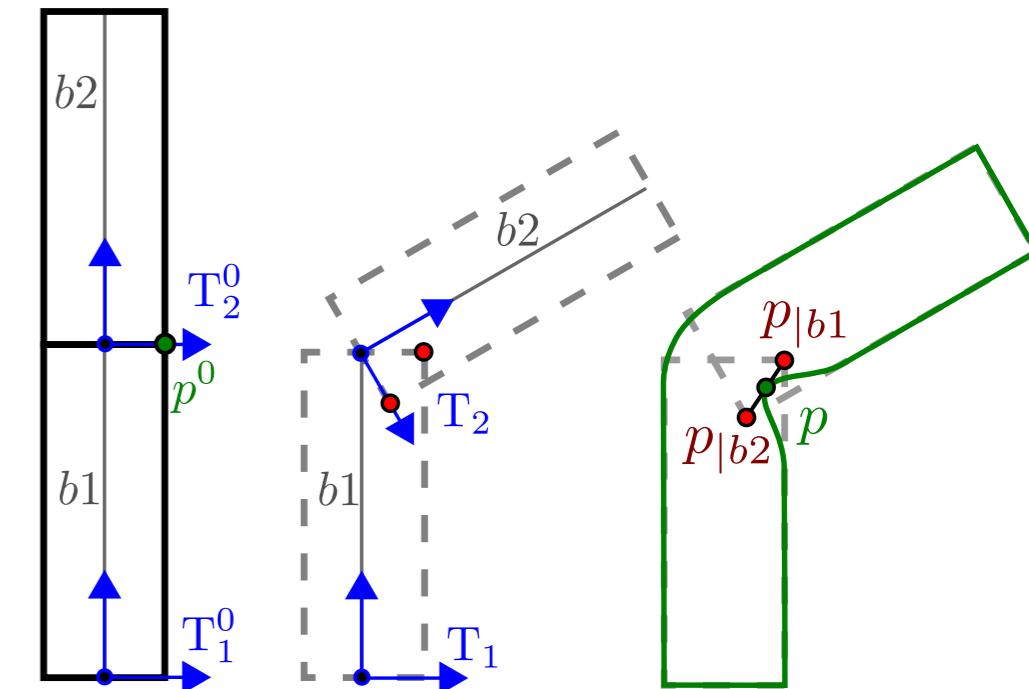
Can be generalized to arbitrary interpolation between two bones

$$p = \alpha p_{|b1} + (1 - \alpha) p_{|b2} = (\alpha \mathbf{M}_1 + (1 - \alpha) \mathbf{M}_2) p^0$$

α : skinning weights

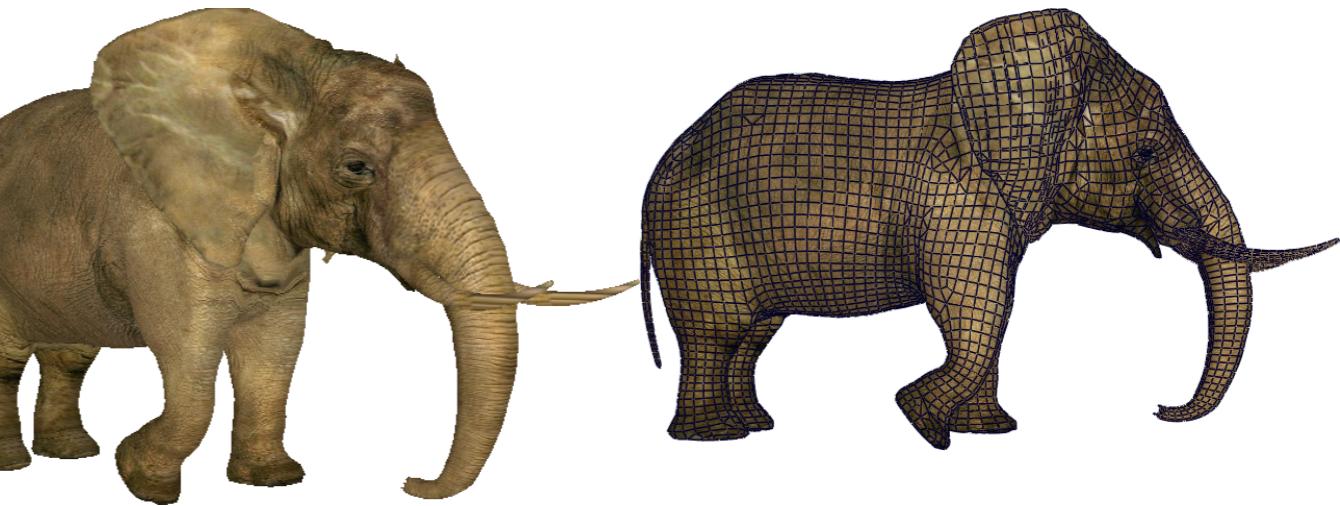
Can be generalized to any number of bones

$$p = \sum_{k=0}^{N-1} \alpha_k p_{|bk} = \left(\sum_{k=0}^{N-1} \alpha_k \mathbf{M}_k \right) p^0, \quad \sum_k \alpha_k = 1$$



Smooth skinning - Summary

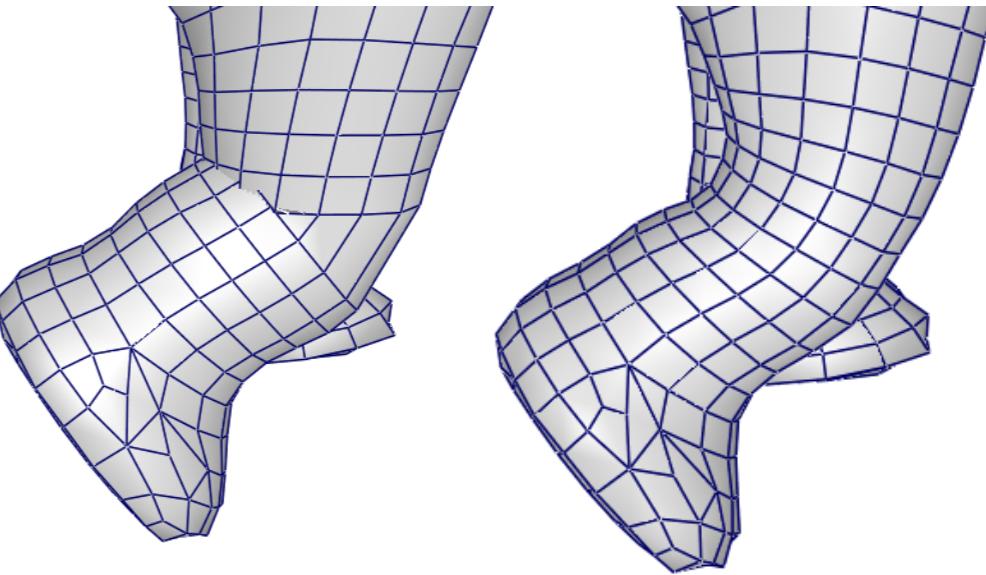
$$p = \left(\sum_{k=0}^{N-1} \alpha_k M_k \right) p^0 = \left(\sum_{k=0}^{N-1} \alpha_k T_k (T_k^0)^{-1} \right) p^0$$
$$\forall k, \alpha_k \in [0, 1], \text{ and } \sum_{k=0}^{N-1} \alpha_k = 1$$



The current **standard** for almost all articulated character deformations

- Intuitive deformation
- Controlable shape (*through weights*)
- Fast to compute (GPU compatible)
matrix average, multiplication matrix-vector

⇒ Heavily used in Animation cinema & Video Game



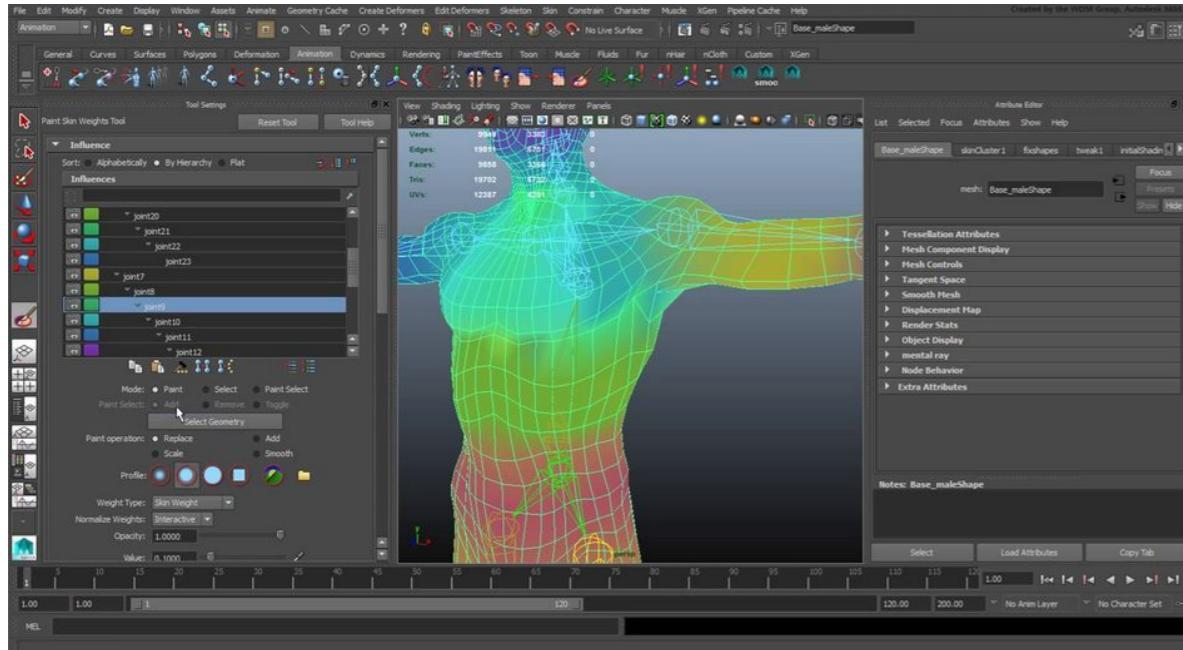
[*Joint-Dependent Local Deformations for Hand Animation and Object Grasping*. Nadia Magnenat-Thalmann, Rochard Laperrière, Daniel Thalmann. *Graphics Interface*, 1988]

[*Over My Dead, Polygonal Body*. Jeff Lander. *Game Developer Magazine*, 1998]

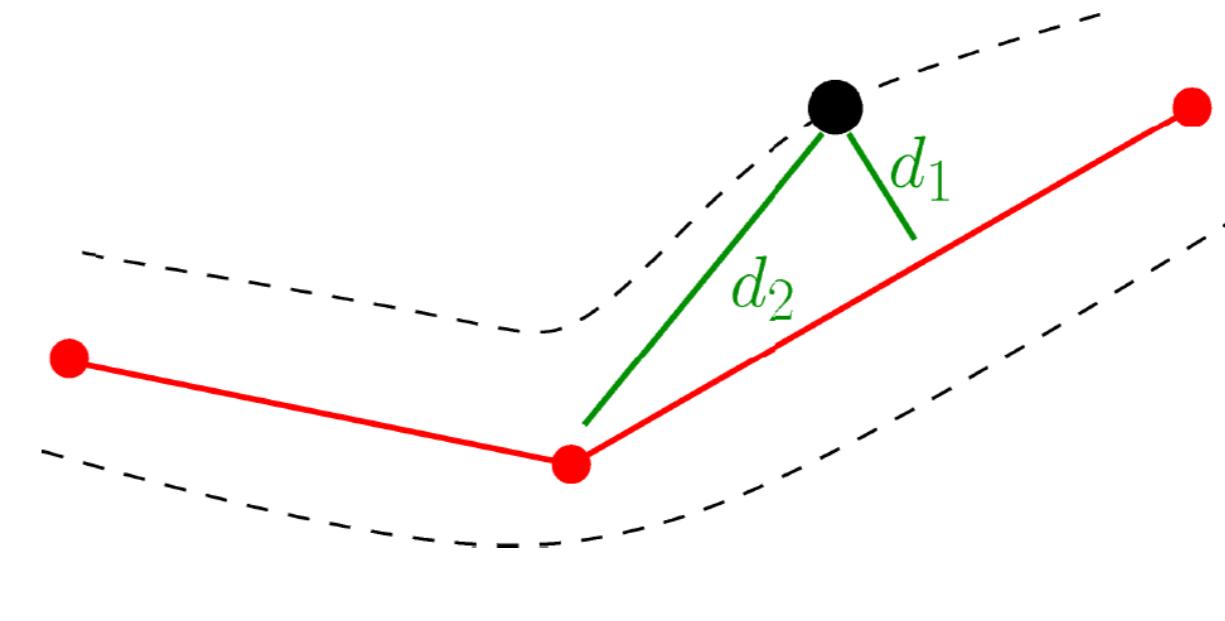
Skinning weights

How to generate skinning weights ?

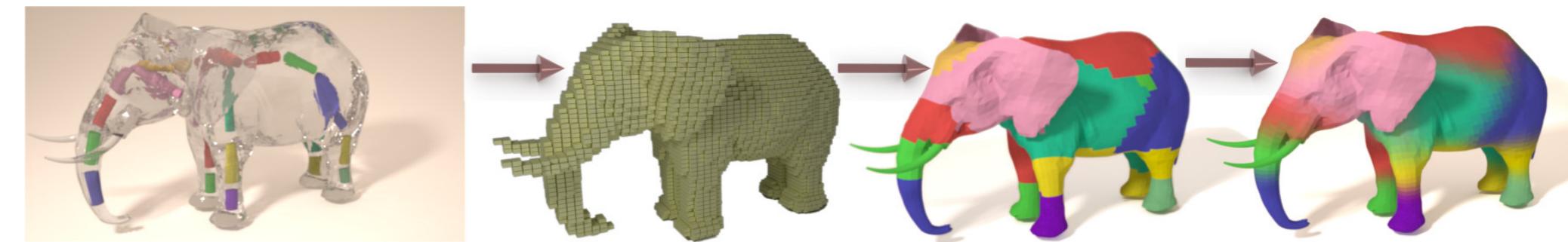
- Paint them manually
- Automatic computation



ex. Using cartesian distances: $\alpha_1 = d_1^{-1}/(d_1^{-1} + d_2^{-1})$



Or using diffusion on the volume/surface



Rigging: Associating bones and skinning weights (or any animation handle) to mesh parts

Skinning: File Format

Unfortunately few standard open format to store skinning animation data

Main open format: Collada (XML), glTF (JSON)

Common software related formats: FBX, Blend, 3DS, ...

```
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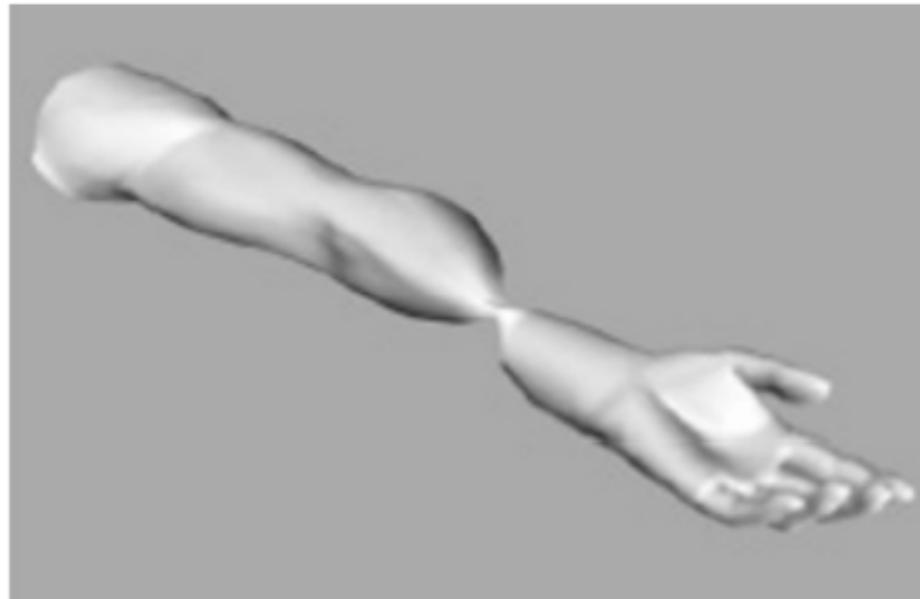
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.json

Linear Blend Skinning - Limitations

- Non-trivial rigging settings
- Artifacts for large rotations: Candy wrapper, Collapsing elbow

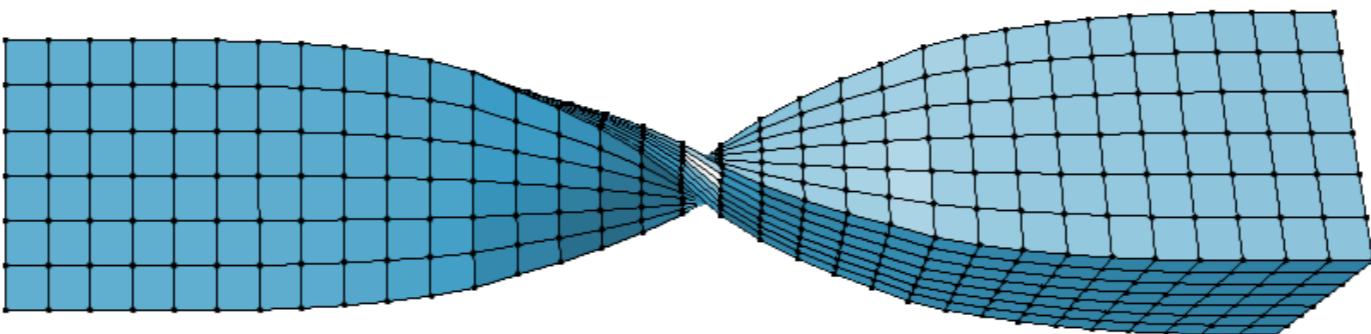


Candy wrapper



Collapsing elbow

Linear blending between rigid transformation matrices



Skinning improvement

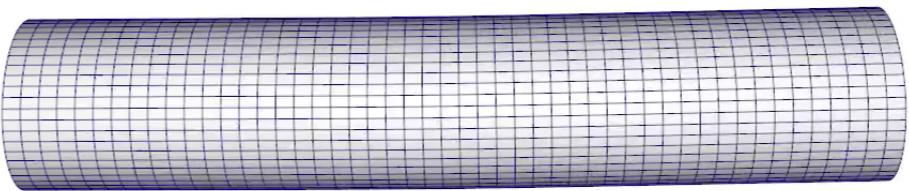
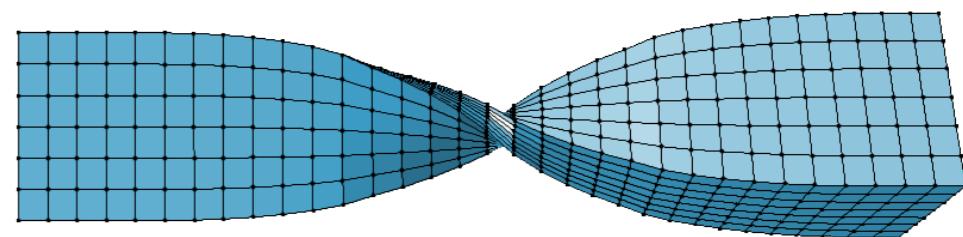
Avoid linear blending b/w affine transform matrices

First idea: Split rigid transformation matrices in

- rotation part: blend using quaternions (solve candy wrapper)
- translation part: blend linearly

But doesn't work for general deformation: Arbitrary center of rotation

Rotation and translations are treated separately



Possibility to compute an optimal center of rotation at each frame

[Spherical Blend Skinning: A Real-time Deformation of Articulated Models. L. Kavan, J. Zara. I3D 2005.]

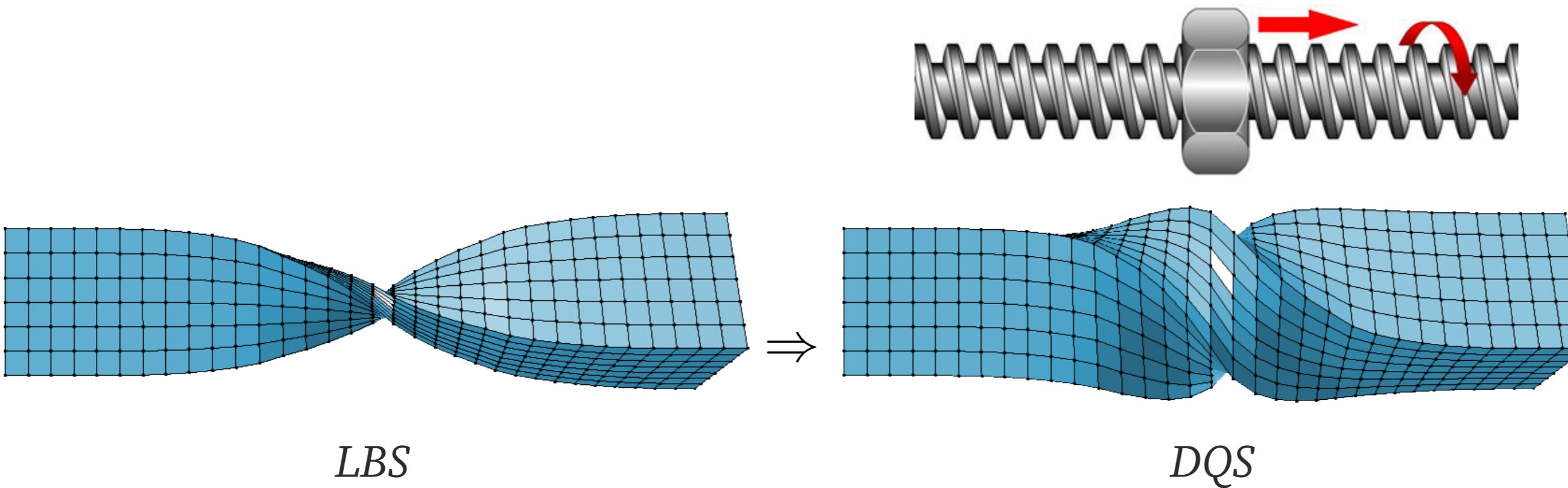
Skinning improvement: Dual Quaternion

Second idea: Use of **dual quaternion**

$$\hat{q} = q_0 + \epsilon q_\epsilon, \quad \epsilon \text{ dual element.}$$

Dual quaternion = generalization of quaternion to handle *rigid transformation*
Rotation + translation

Unit dual quaternion models rigid transformation as **screw motions**
= *rotation about an axis followed by a translation in the direction of this axis*



Dual number and dual quaternion

Dual number $a = a_0 + \epsilon a_\epsilon$

Dual element ϵ is nilpotent : $\epsilon \neq 0, \epsilon^2 = 0$

ϵ commonly used to model infinitesimal quantity (ex. automatic differentiation)

Dual quaternion \hat{q} = Generalization of quaternion to dual numbers

$$\hat{q} = q_0 + \epsilon q_\epsilon$$

- q_0 : pure rotation component
- q_ϵ : encodes translation component (dual part)

Given a unit quaternion q_0 , and a translation $t = (t_x, t_y, t_z)$, the associated unit dual quaternion is

$$\hat{q} = q_0 + \frac{\epsilon}{2} q_t q_0 \quad q_t = (t_x, t_y, t_z, 0)$$

Unit dual quaternion ($\|\hat{q}\| = 1$) describe the set of rigid transformation as screw motion.

Axis-angle representation with dual quaternion

Similarly to quaternion: "angle/axis" correspondance

- $\hat{q} = \cos(\hat{\theta}/2) + \hat{n} \sin(\hat{\theta}/2)$

- $\hat{\theta} = \theta_0 + \epsilon \theta_\epsilon$

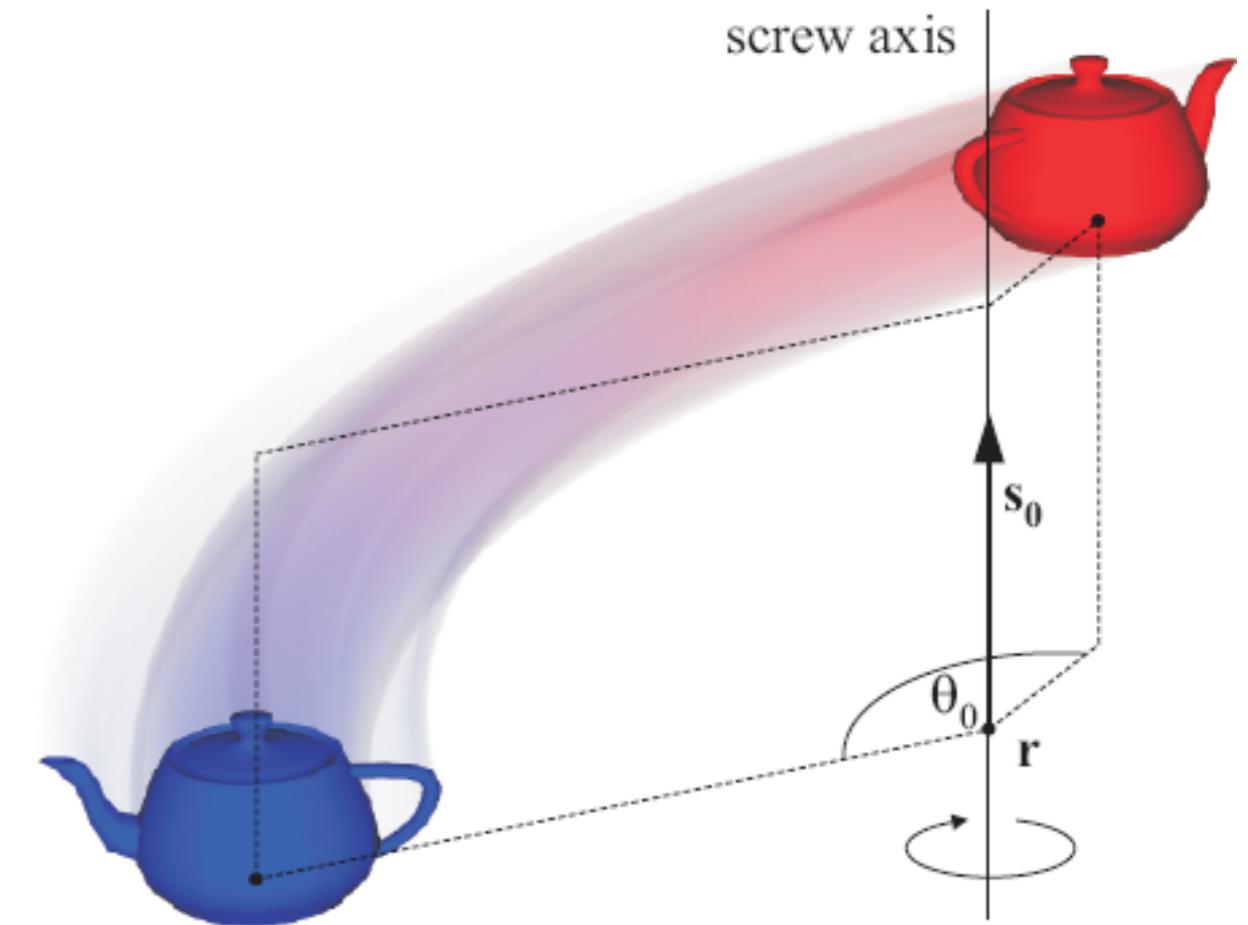
- θ_0 : angle of rotation

- $\theta_\epsilon = t \cdot n_0$: quantity of translation along n_0

- $\hat{n} = n_0 + \epsilon n_\epsilon$

- n_0 : axis of rotation

- $n_\epsilon = \frac{1}{2} ((n_0 \times t) \cotan(\theta_0/2) + t) \times n_0$: called the moment of the rotation axis.



Convert dual quaternion to rotation/translation

Given a non-unit dual quaternion as input $\hat{q}' = q'_0 + \epsilon q'_\epsilon$

How to compute the components of $\hat{q}' / \|\hat{q}'\| = \hat{q} = q_0 + \epsilon q_\epsilon$?

Express the parameterization in rotation-translation:

$$\hat{q} = q_0 + \frac{\epsilon}{2} q_t q_0, \quad q_t = (t_x, t_y, t_z, 0)$$

First, normalize the non dual component: $\hat{q}' / \|q'_0\|$

$$\Rightarrow q_0 = q'_0 / \|q'_0\|$$

Second, enforce the parameterization of the dual component: $\frac{1}{2} q_t q_0 = q'_\epsilon / \|q'_0\|$

$$\Rightarrow q_t = 2 q'_\epsilon q_0^\star / \|q'_0\|$$

Dual Quaternion Skinning (DQS)

1- Encode rigid transformation (q^i, t^i) into dual quaternion

$$\hat{q}^i = q_0^i + \frac{\epsilon}{2} q_t^i q_0^i, \quad q_t^i = (t_x^i, t_y^i, t_z^i, 0)$$

2- Compute blending in the dual quaternion space (ScLERP)

$$\hat{q}' = \sum_i \omega_i \hat{q}^i = q'_0 + \epsilon q'_\epsilon$$

3- Extract components (q, t) from \hat{q}'

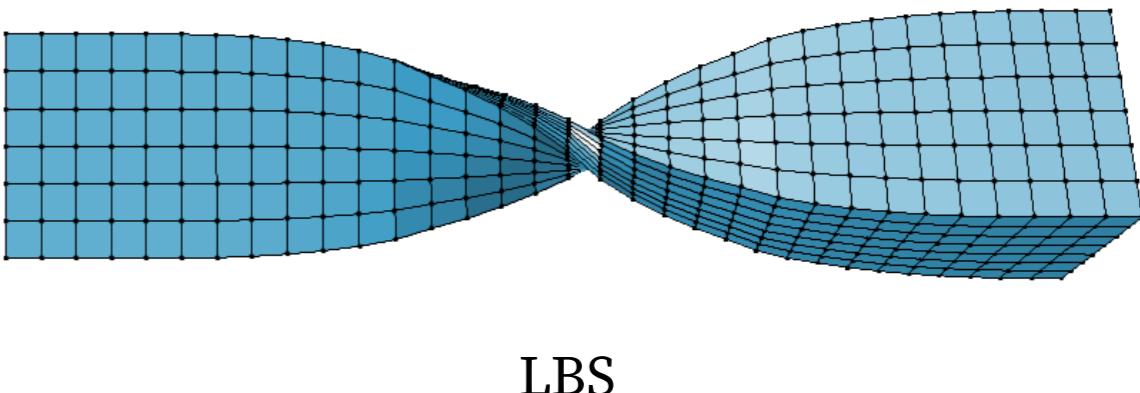
$$- q = q'_0 / \|q'_0\|$$

$$- (t_x, t_y, t_z, 0) = 2 q'_\epsilon q^*$$

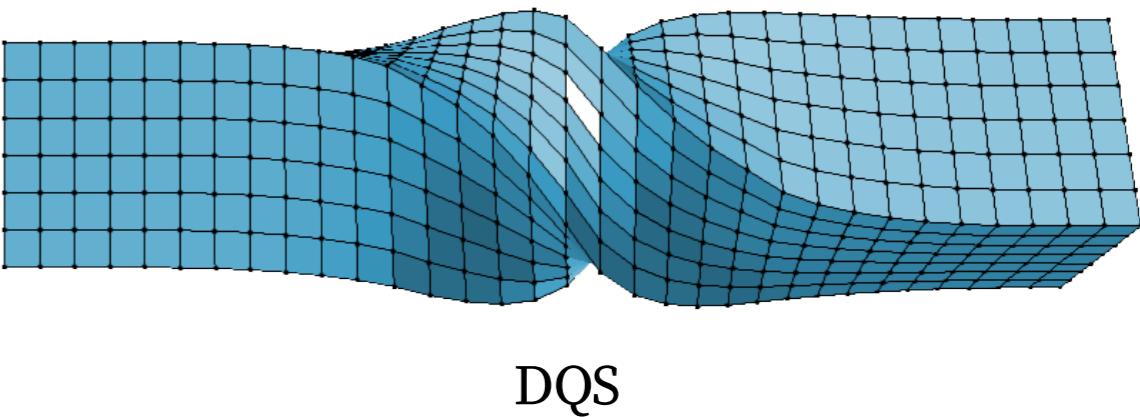
q^* : conjugate of q .

4- Apply finally the transformation (q, t) to position p_0

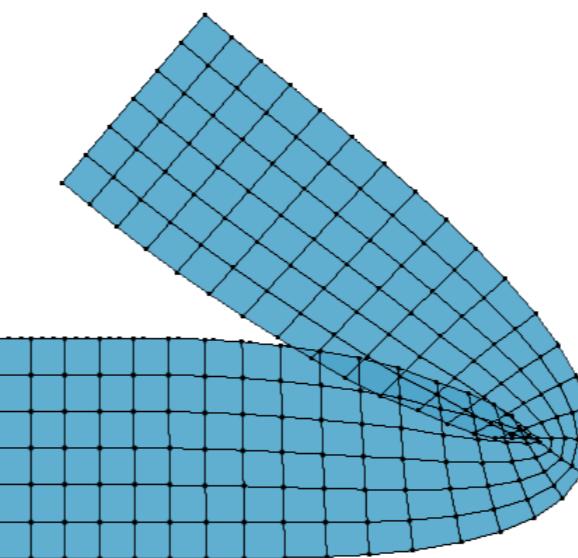
[Skinning with Dual Quaternions. Kavan et al. I3D, 2007]



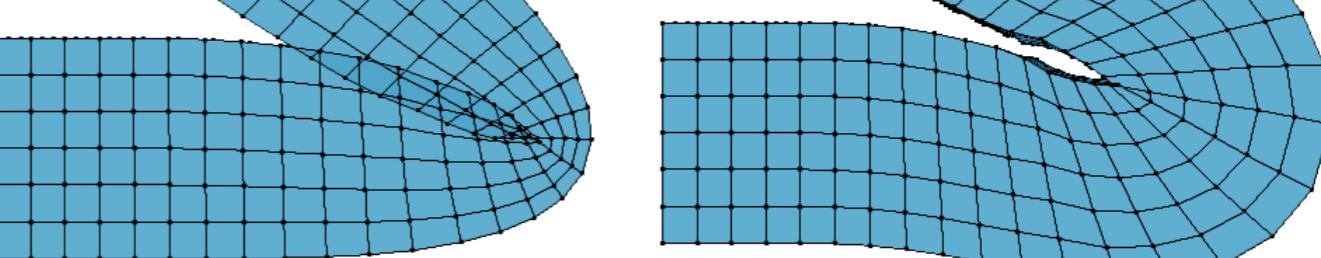
LBS



DQS



LBS



DQS

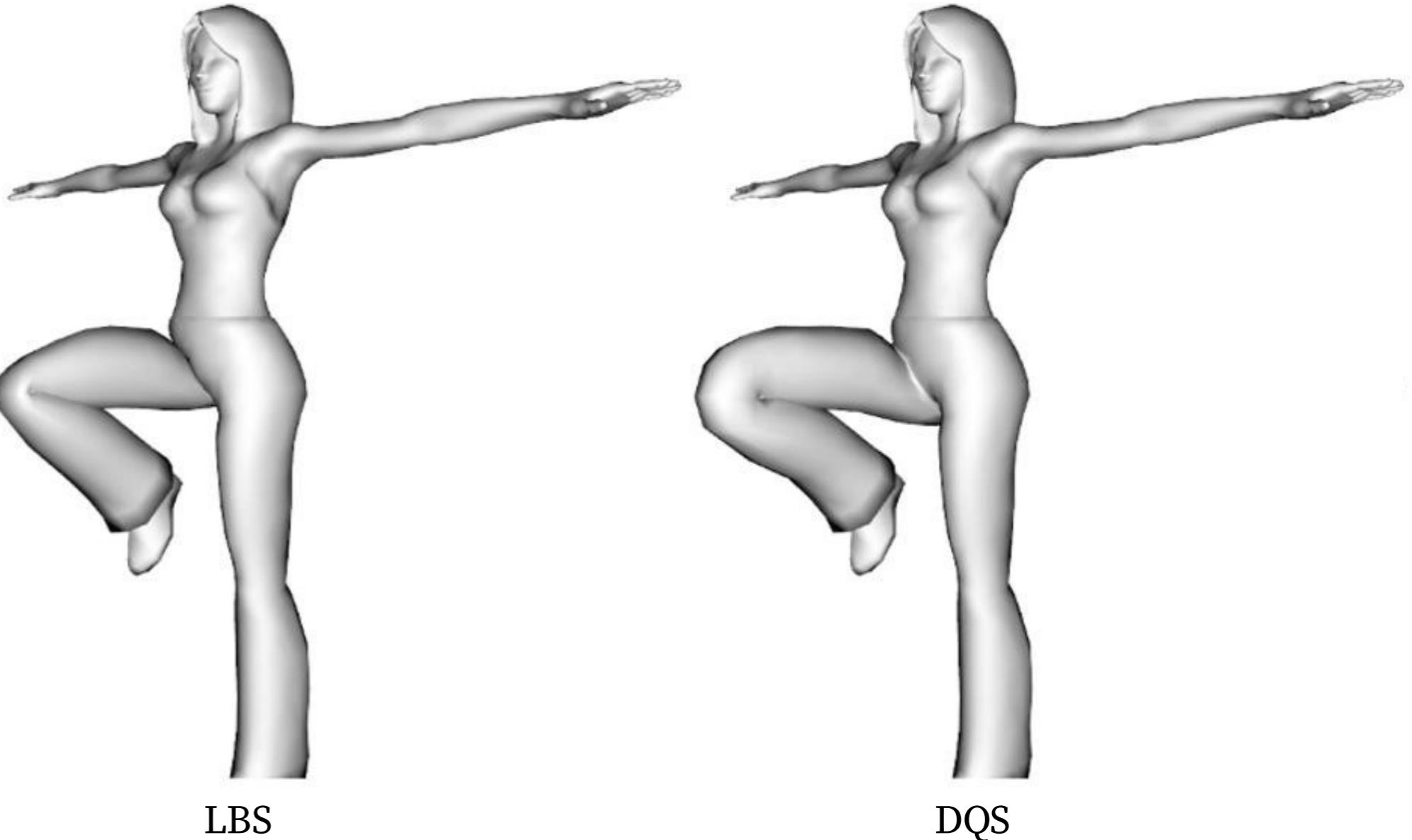
Dual Quaternion VS LBS

Dual quaternion

- (+) Fully solves *candy wrapper* artifact
- (+) Almost as efficient as LBS
- (-) May create artificial/unwanted bulge

Not always preferred to LBS

Both solutions (LBS, DQS) are proposed in standard tools



Character Animation

Skeletal Animation

Skeleton structure

Characteristics

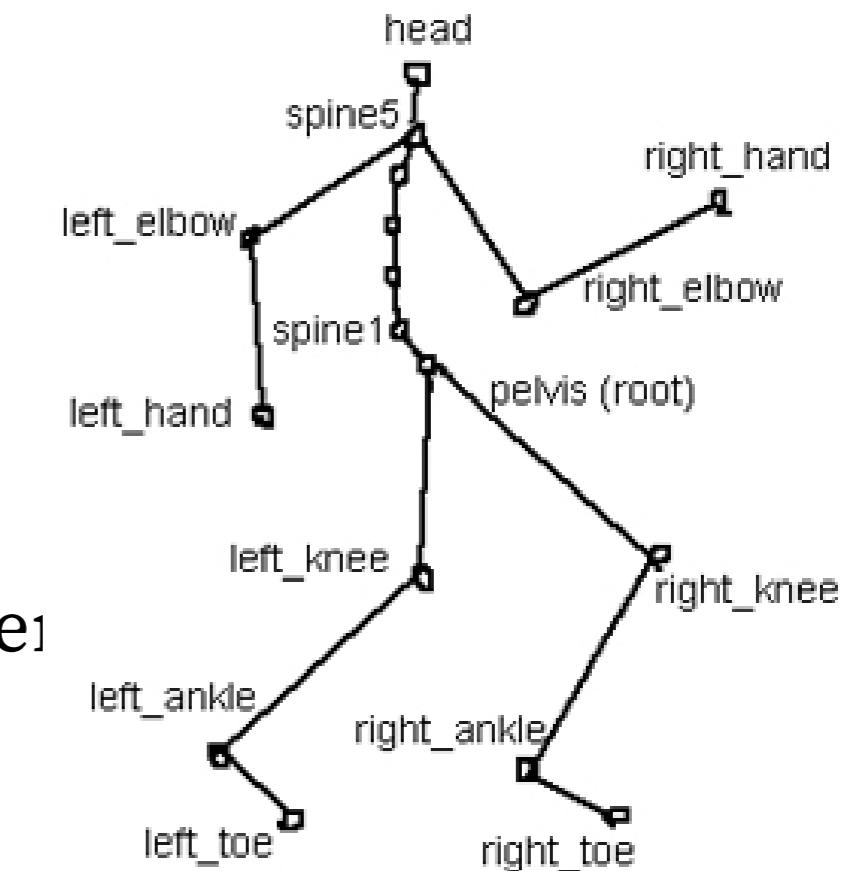
- Hierarchical representation

All children follow the transformation of the parent

Need to define a root: usually at the hips/pelvis

- Convenient to express relative transformation with respect to the parent

ex. Ankle is at 20° w/r knee



Converting local to global frames/joint coordinates

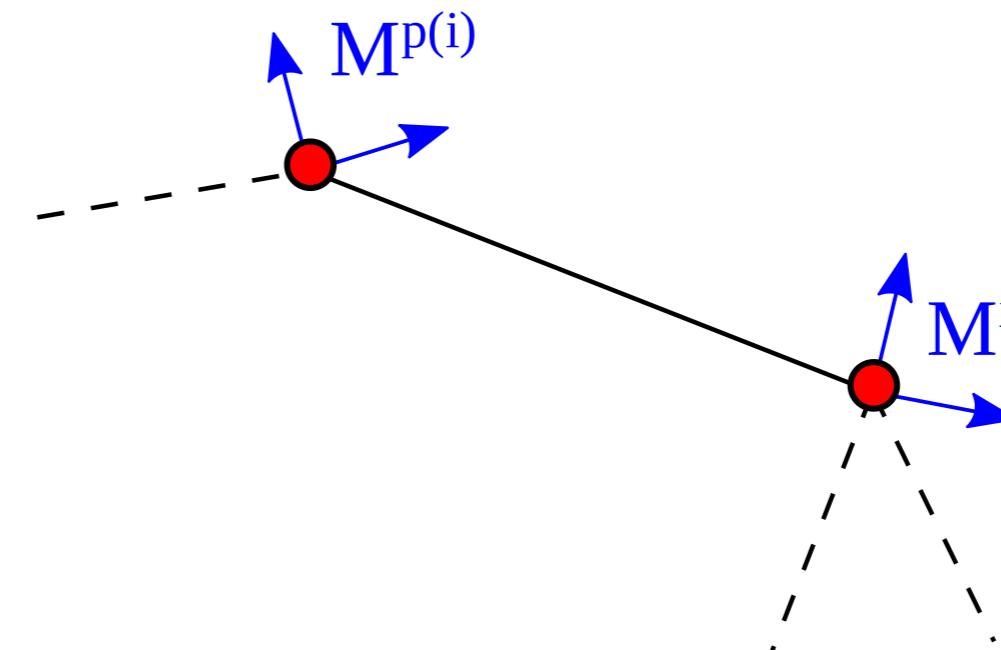
- With 4x4 matrices M

$$M_{global}^i = M_{global}^{p(i)} M_{local}^i$$

- With translation t , rotation R

$$R_{global}^i = R_{global}^{p(i)} R_{local}^i$$

$$t_{global}^i = t_{global}^{p(i)} + R_{global}^{p(i)} t_{local}^i$$



Encoding hierarchical skeleton

- Simplest encoding based on index within vector

```
Geometry=[M0, M1, M2, M3, M4, M5]
```

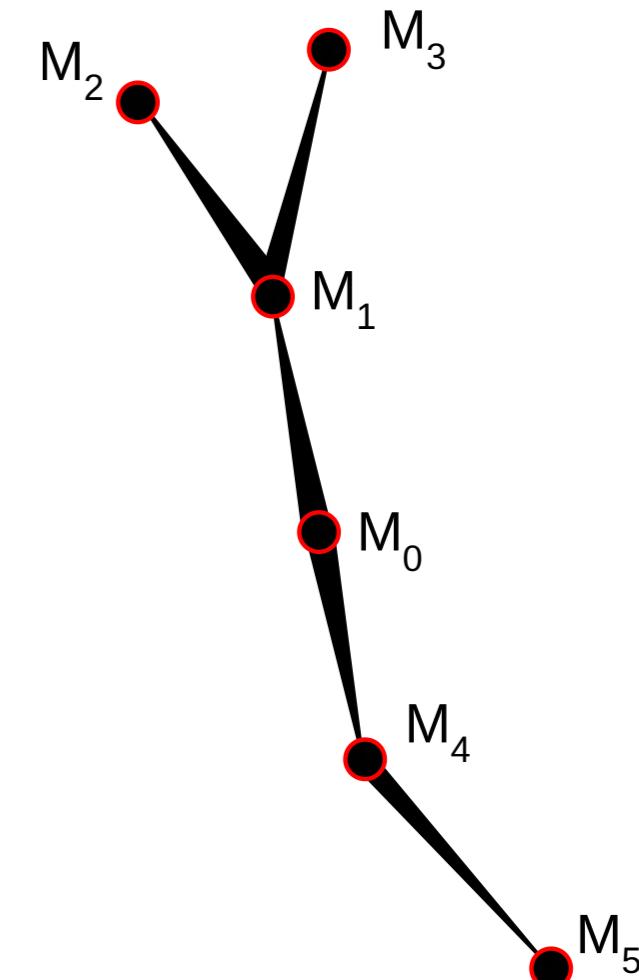
```
Parent = [-1,0,1,1,0,4]
```

- Convert local coordinates to global coordinates

```
local (Geometry) <- std::vector of rotation (r), translation (p)
```

```
global (Geometry) <- std::vector of rotation (r), translation (p)
```

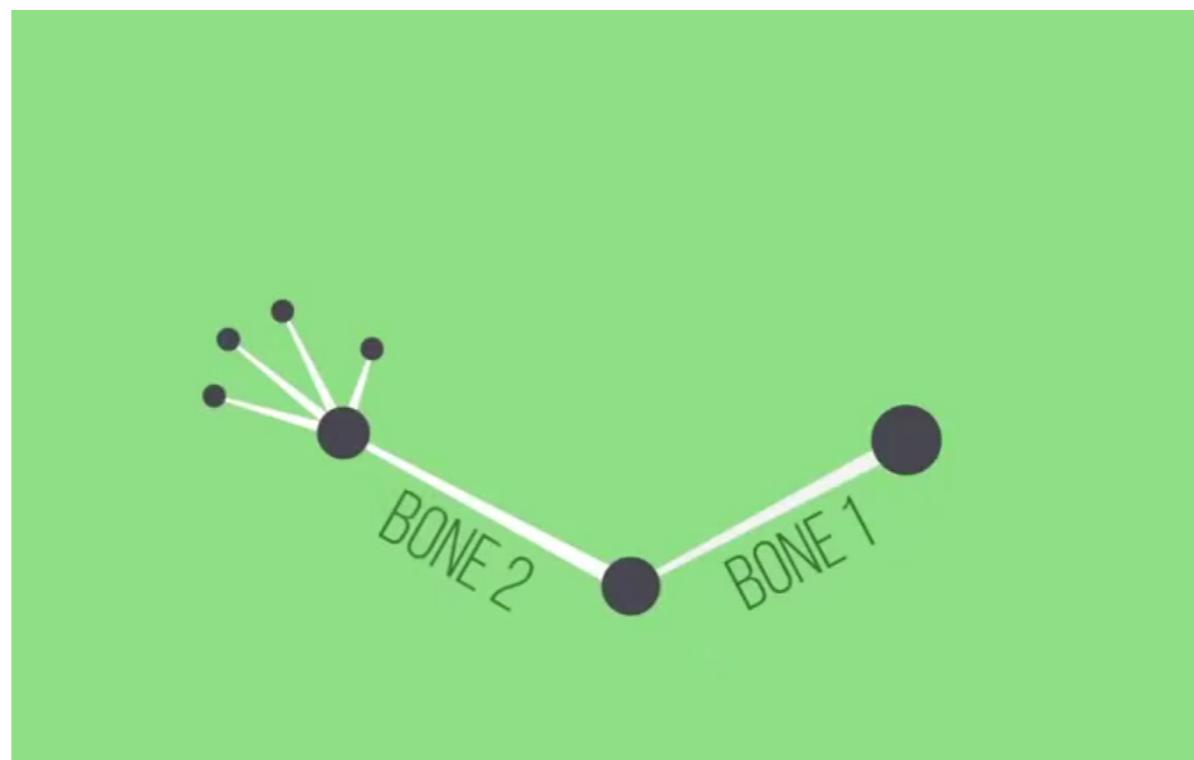
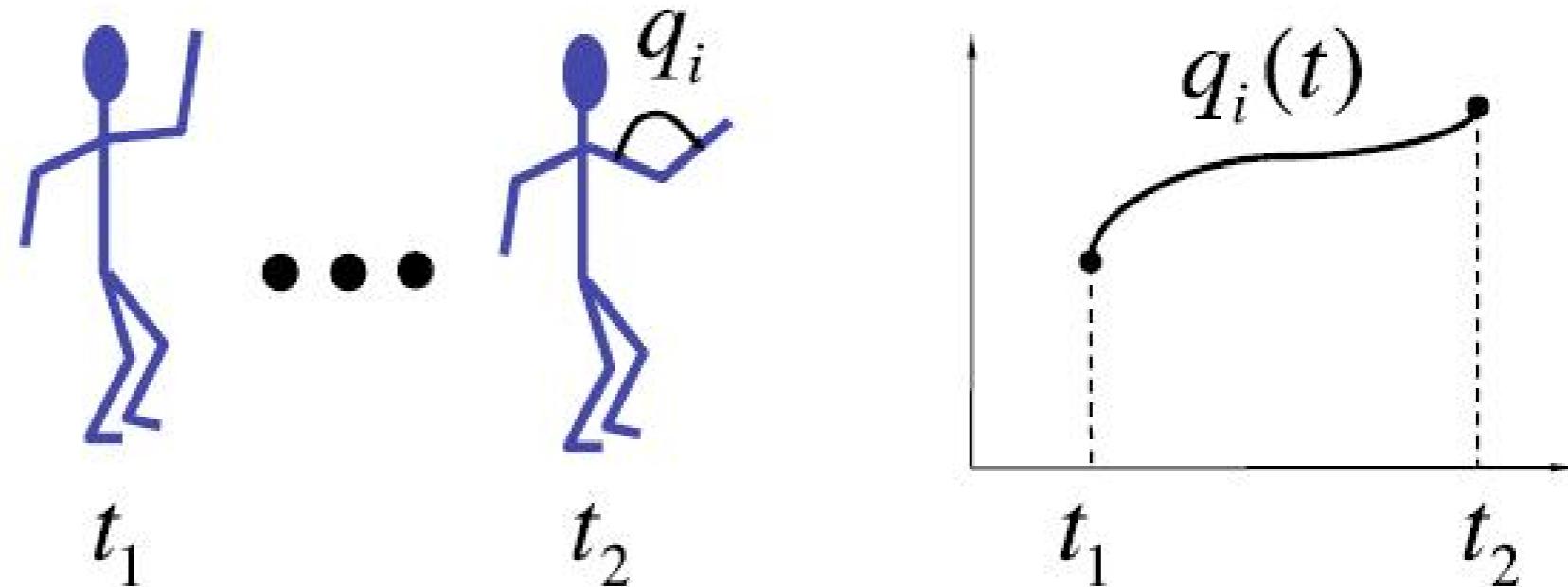
```
global[0] = local[0];
for(size_t k=1; k<N; ++k)
{
    int parent = Parent[k];
    global[k].r = global[parent].r * local[k].r;
    global[k].p = global[parent].r * local[k].p + global[parent].p;
}
```



Forward kinematics

FK - Forward Kinematics

- Each join angle is set manually
 - Adapted to set orientation of specific parts
 - Interpolate rotations during animation
- (+) Generates curved trajectory naturally



MiloScerny Animation

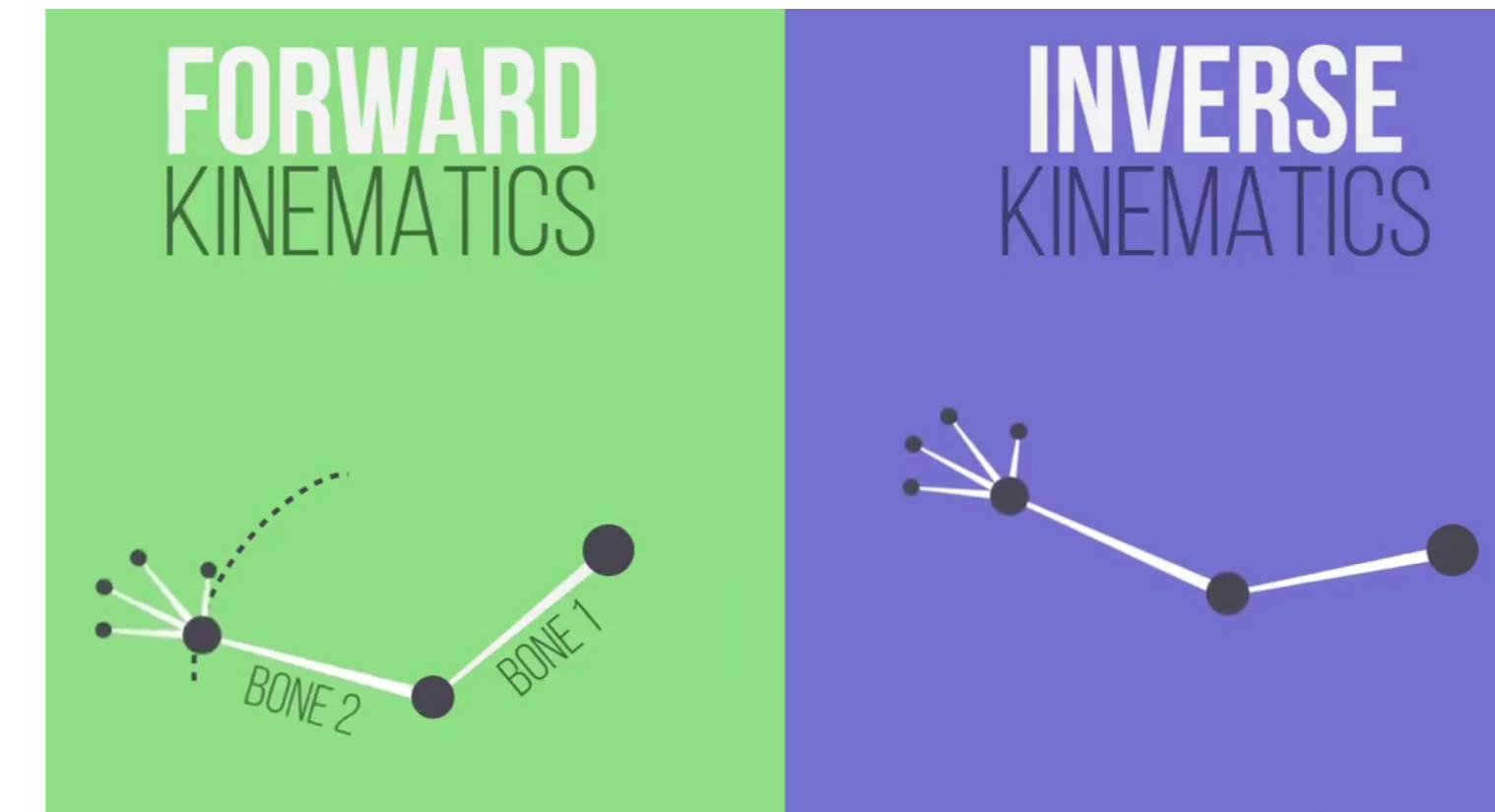
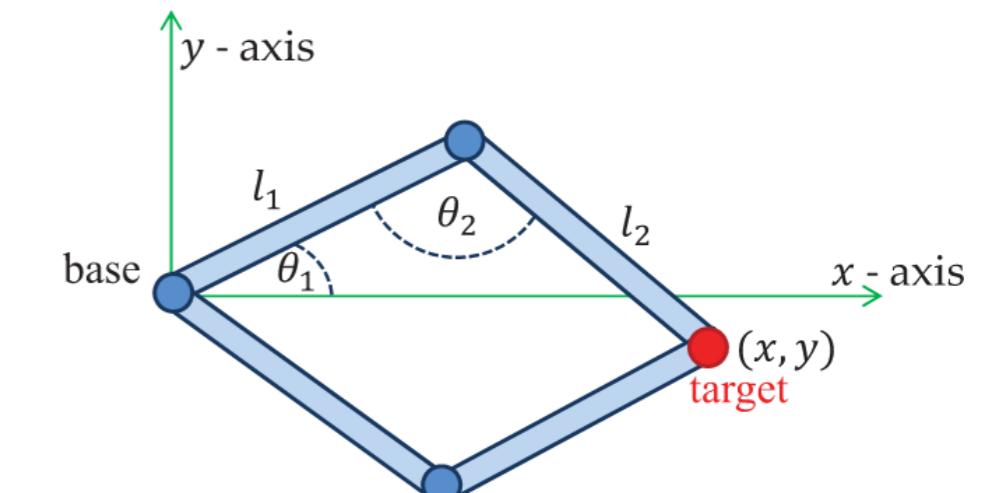
Inverse Kinematics

IK: Inverse Kinematics

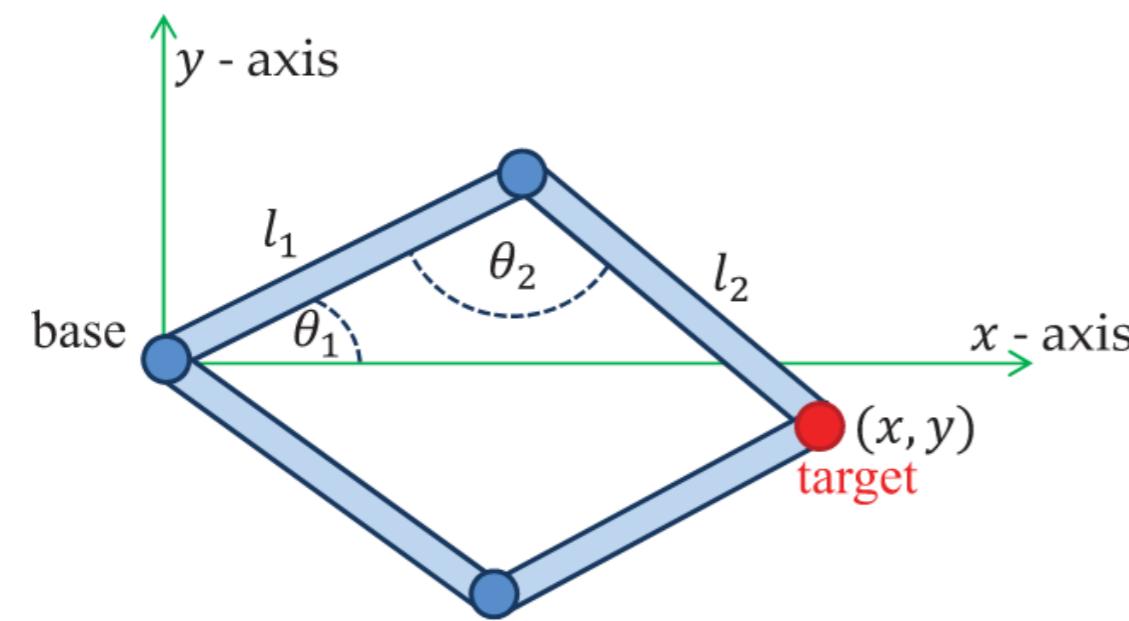
- Describe position (/and orientation) of *end-effectors* (contact, walking, etc)
- Compute joint angles reaching this position

$$p_k = p_0 + \sum_{i=0}^{k-1} l_i R_i u_i$$

R_i can be expressed with various rotation parameters (Matrices, Euler angles, axis/angle, quaternions, etc)



IK Example with two bones



[*Inverse Kinematics Techniques in Computer Graphics: A Survey. A. Aristidou et al. STAR EG. 2017.*]

In general the general case $p_k = f(\theta_i)$

- Look for $\theta_i = f^{-1}(p_k)$
- f is a non linear function
- There may exists multiple solutions (or none)
- Solutions may exhibits discontinuities
- Closed form solution are not available

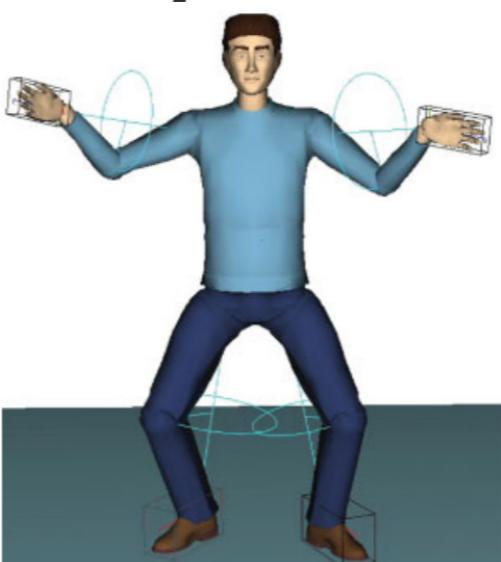
Two solutions defined by

$$\cos(\theta_1) = \frac{l_1^2 + x^2 + y^2 - l_2^2}{2l_1 \sqrt{x^2 + y^2}}$$

$$\cos(\theta_2) = \frac{l_1^2 + l_2^2 - (x^2 + y^2)}{2l_1 l_2}$$

Some attempts for explicit solutions in specific cases

[*Real-Time Inverse Kinematics Techniques for Anthropomorphic Limbs. D. Tolani et al. Graphical Models, 2000.*]
[*Analytical inverse kinematics with body posture control. M. Kallmann. Comp. Anim. & Virt. Worlds, 2008*]



IK: Numerical methods

Numerical inversion of $p = f(\theta)$, $\theta = (\theta_0, \dots, \theta_{N-1})$.

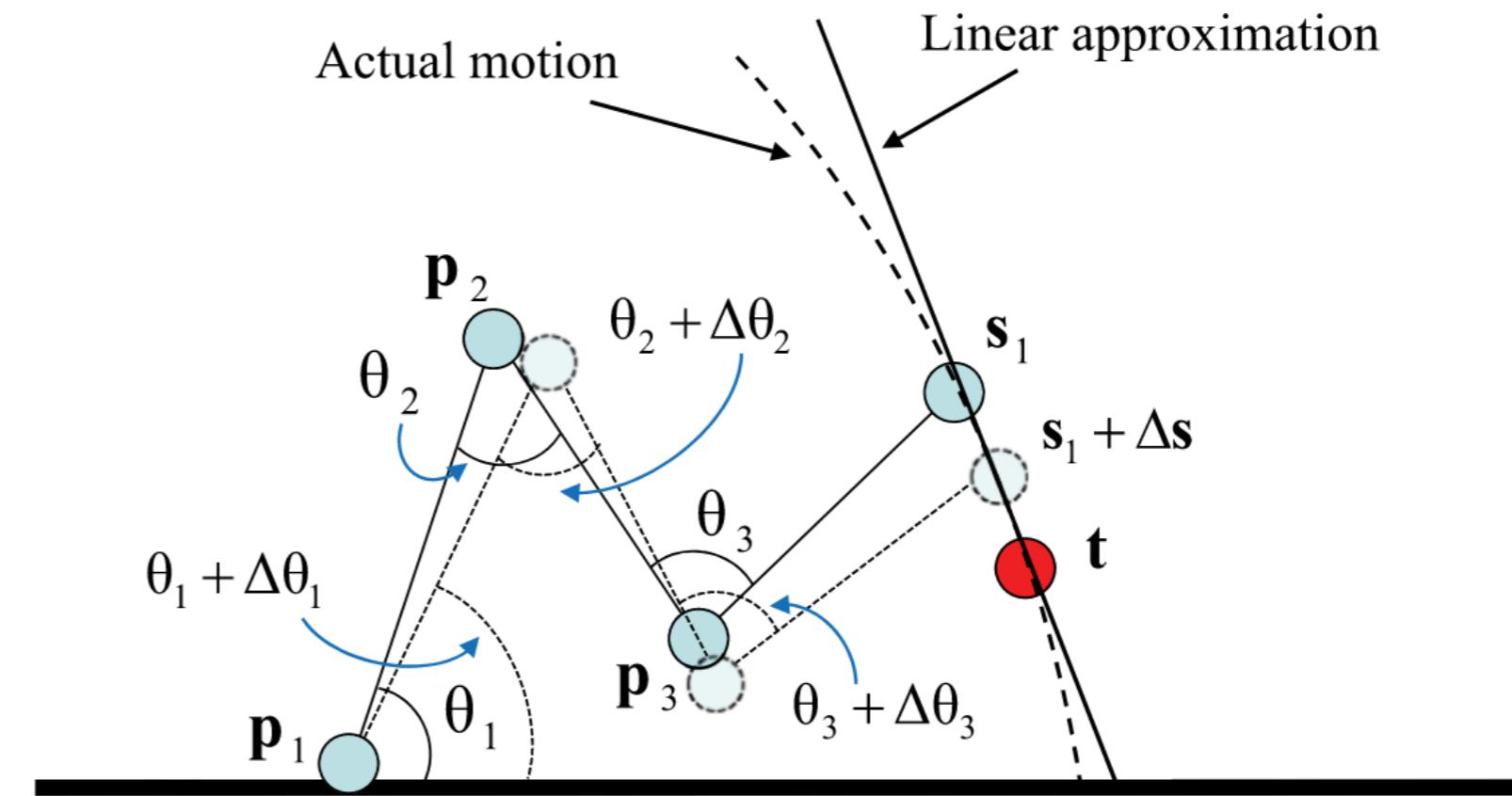
Consider small step size $p \rightarrow p + \Delta p$

$$\Delta p \simeq \underbrace{\left(\frac{\partial f}{\partial \theta} \right)}_J \Delta \theta$$

J - Jacobian matrix.

→ Not square ($3 \times N$), not invertible.

Unknown > # constraints



IK: Numerical methods

Several possible approaches to solve $\mathbf{J} \Delta\theta = \Delta p$

- Pseudo Inverse

$$\Delta\theta = \mathbf{J}^+ \Delta p, \text{ with } \mathbf{J}\mathbf{J}^+ = \mathbf{I}$$
$$\mathbf{J}^+ = \mathbf{J}^T (\mathbf{J} \mathbf{J}^T)^{-1}$$

- Can also be computed using SVD: $\mathbf{J}^+ = \mathbf{V}\Sigma^+ \mathbf{U}^T$

$$\Sigma_{ii} = \sigma_i, \Sigma_{ii}^+ = 1/\sigma_i \text{ if } \sigma_i \neq 0, 0 \text{ otherwise.}$$

- Adding damping to compensate for singularities

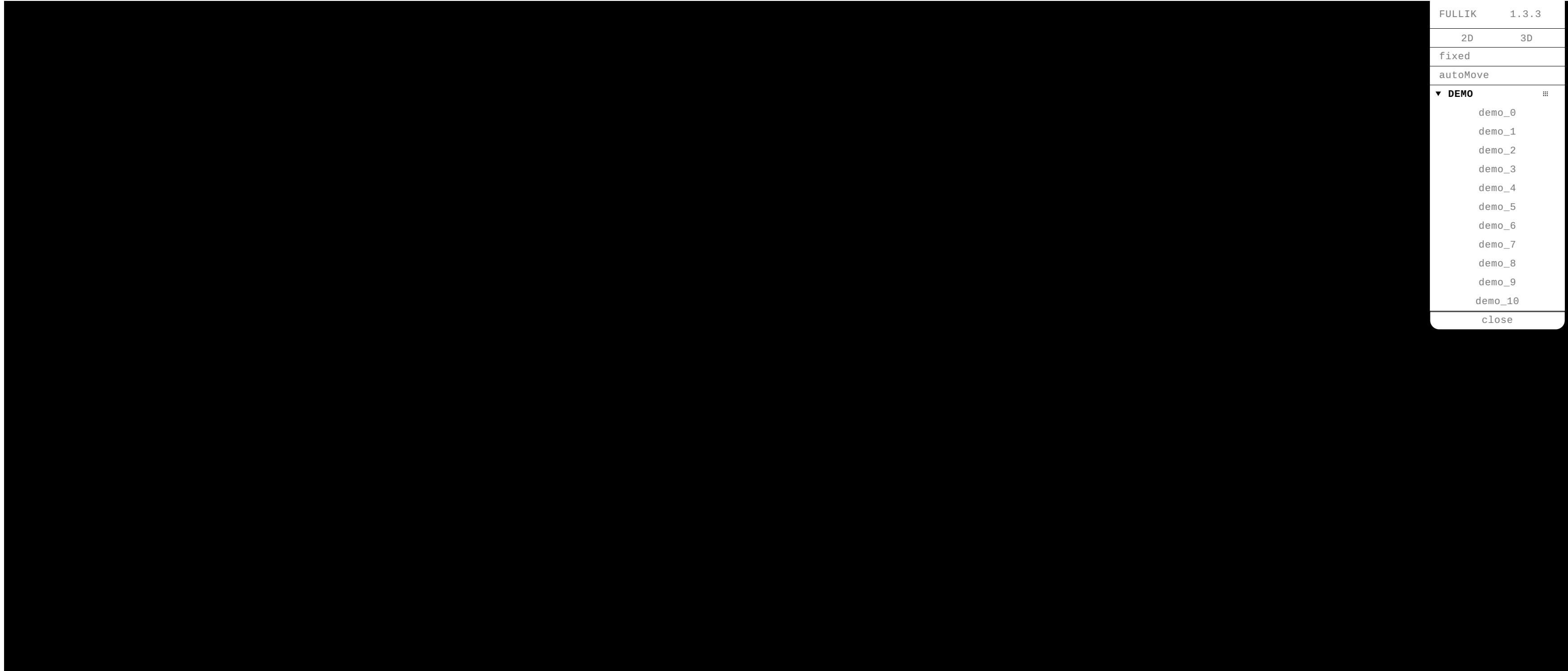
$$\Delta\theta = \mathbf{J}^T (\mathbf{J} \mathbf{J}^T + \lambda^2 \mathbf{I})^{-1} \Delta p$$

- Using Newton's methods

[*Inverse Kinematics Techniques in Computer Graphics: A Survey. A. Aristidou. STAR EG 2017*]

Inverse Kinematics

Example

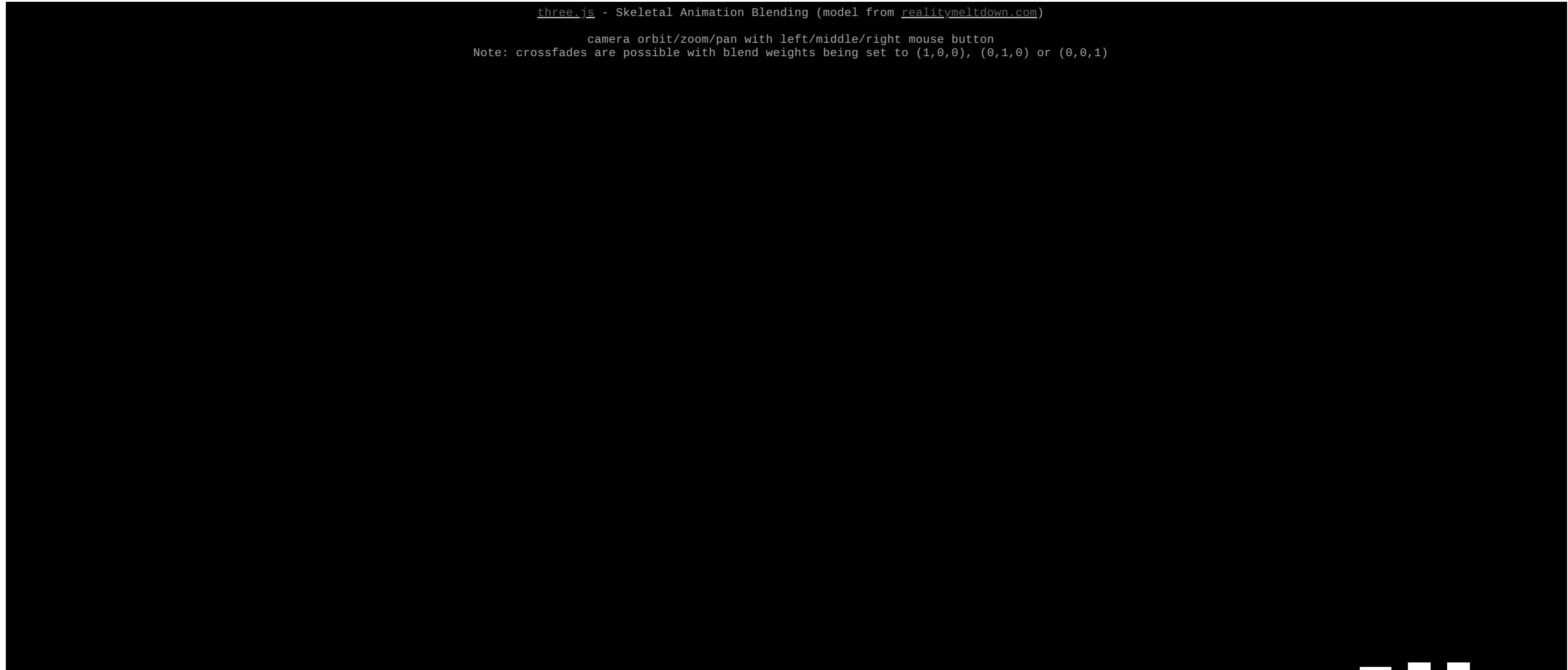


Synthesizing and controlling skeleton animation

Blending skeleton animation

Pre-store several looping animation

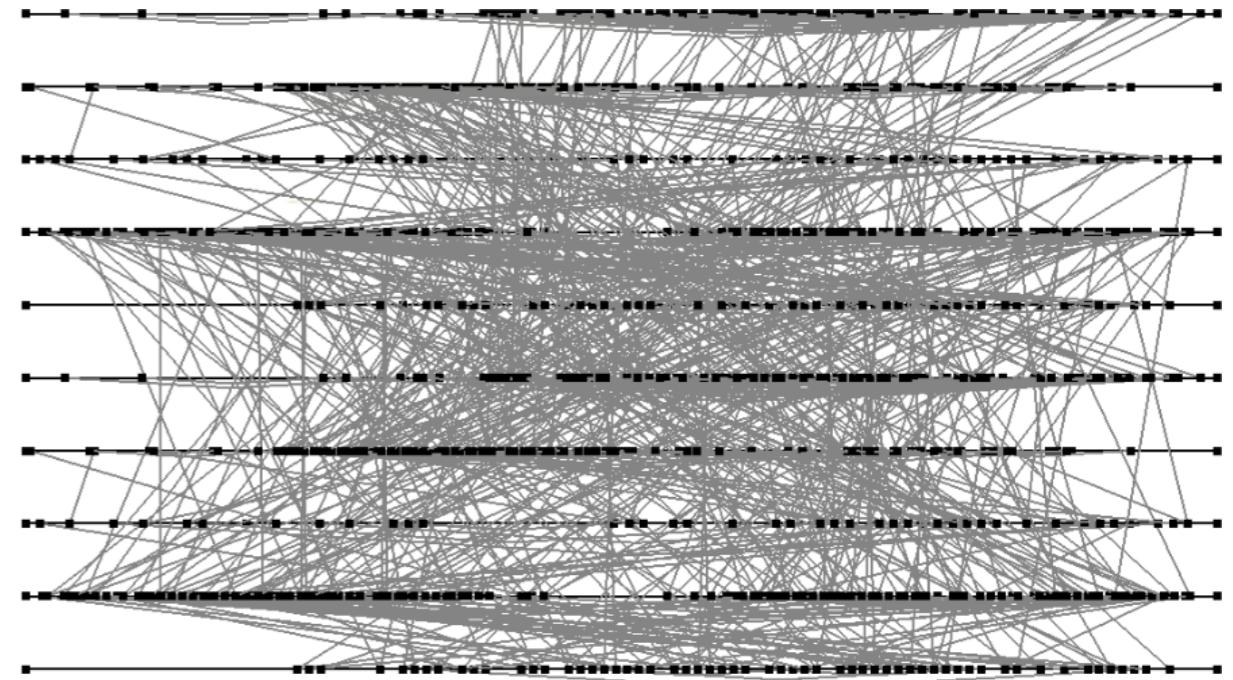
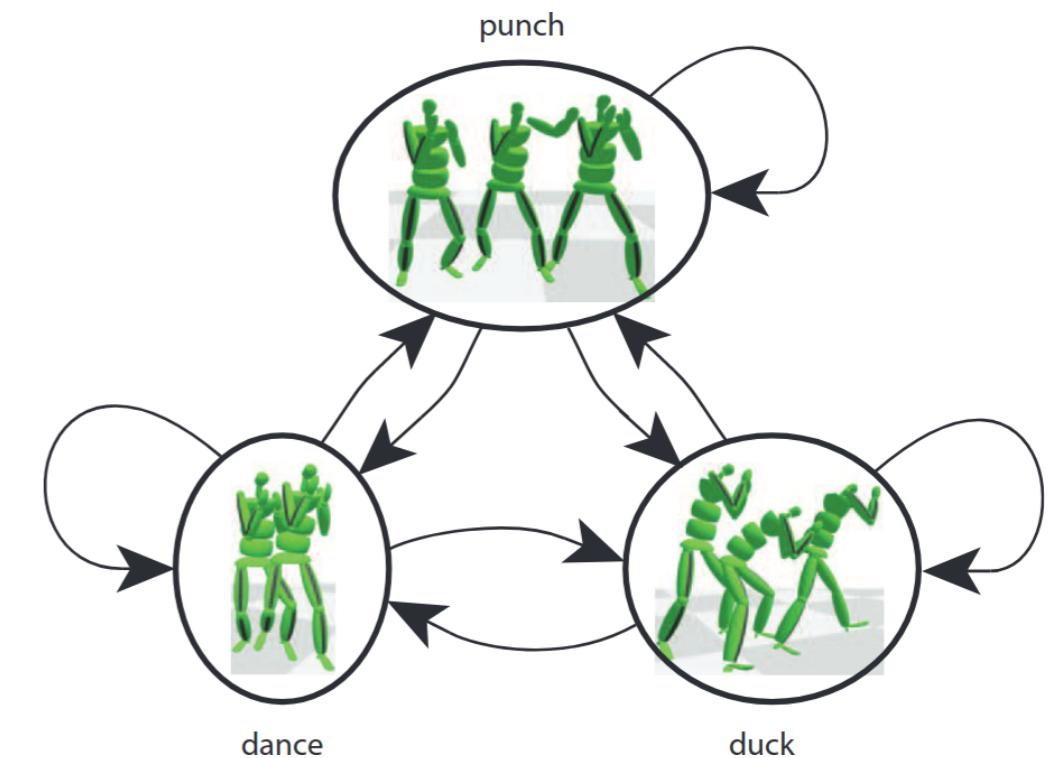
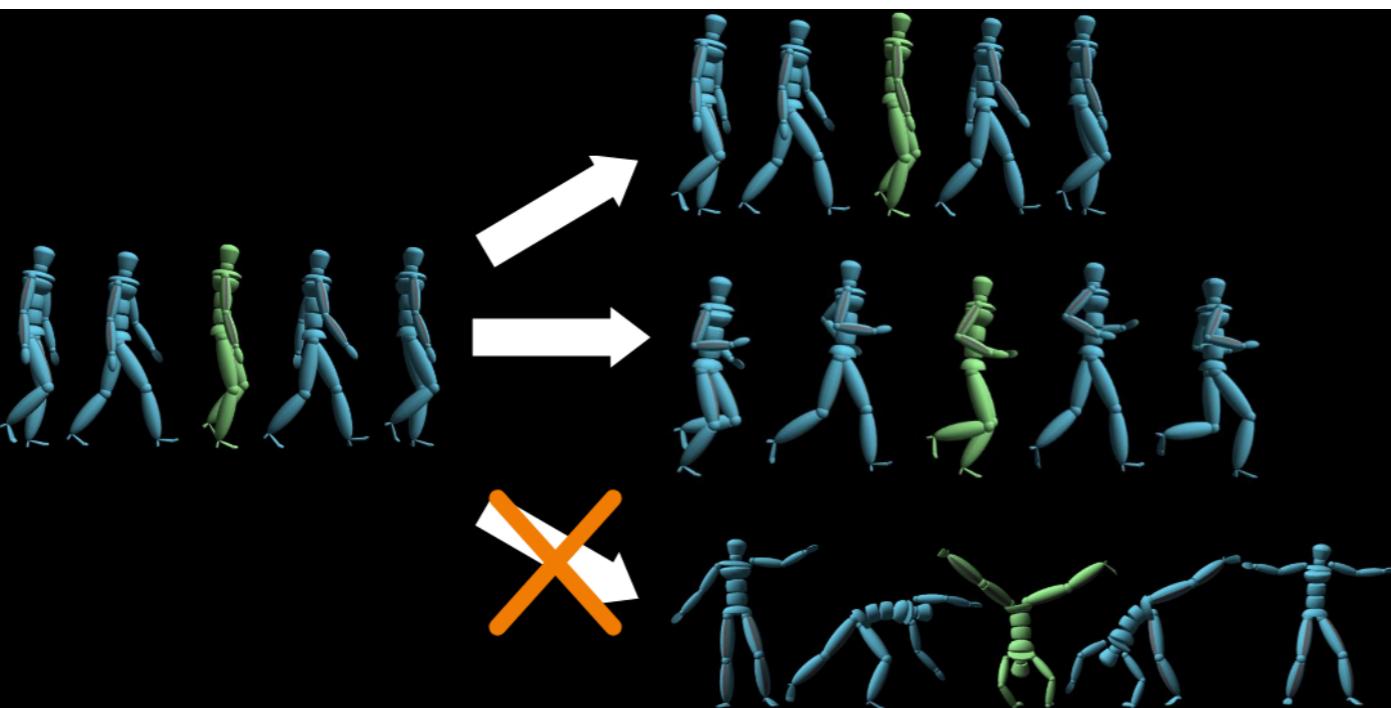
Blend between animation for transition



Motion graphs

Also called Move Trees (highly used in video games)

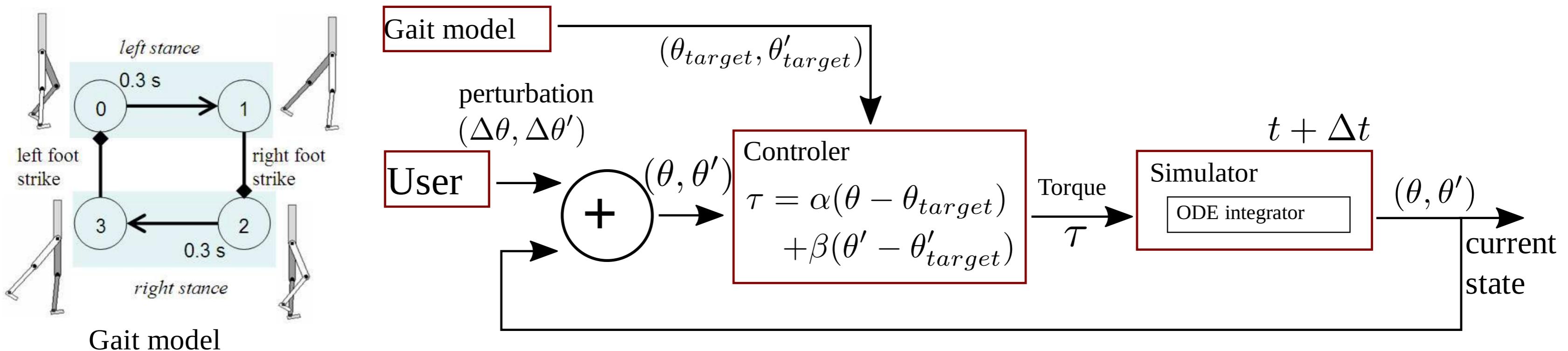
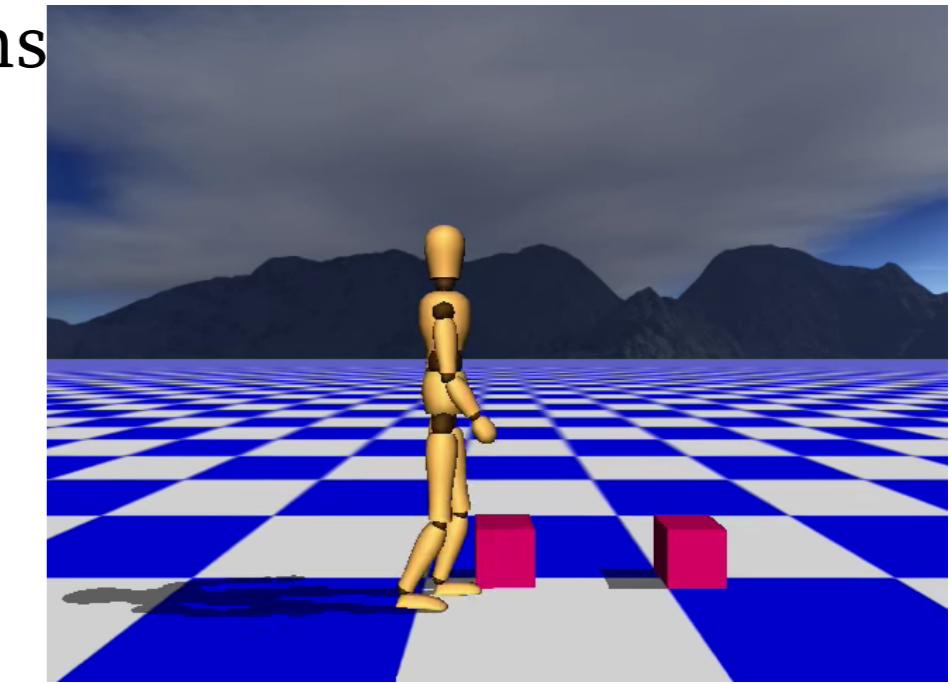
- Stores multiple precomputed animation
 - Manually design, motion capture, etc*
 - Find optimal transitions between different motions
- [Mizuguchi et al., Data driven motion transitions for interactive games, EG short paper, 2001]*
- [Kovar et al., Motion Graphs, ACM SIGGRAPH 2002]*
- [Heck and Gleicher, Parametric Motion Graphs, ACM SIGGRAPH 2007]*



Controllers

Mix between predefined motions and physics → allow user perturbations

- 1 - Define target $(\theta_{target}(t), \theta'_{target}(t))$
pre-defined finite state machine (Gait model)
 - 2 - Add user perturbation to the current state
 - 3 - Use proportional derivative controllers to compute joint torque τ
 - 4 - Integrate torque using rigid body simulator
 - 5 - Iterate

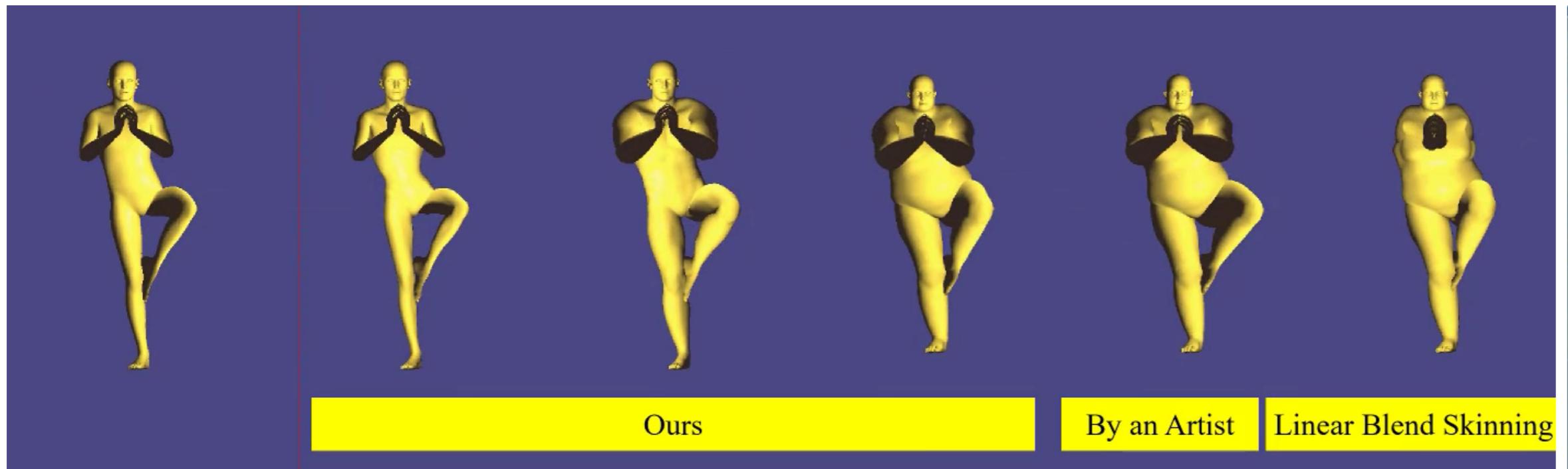
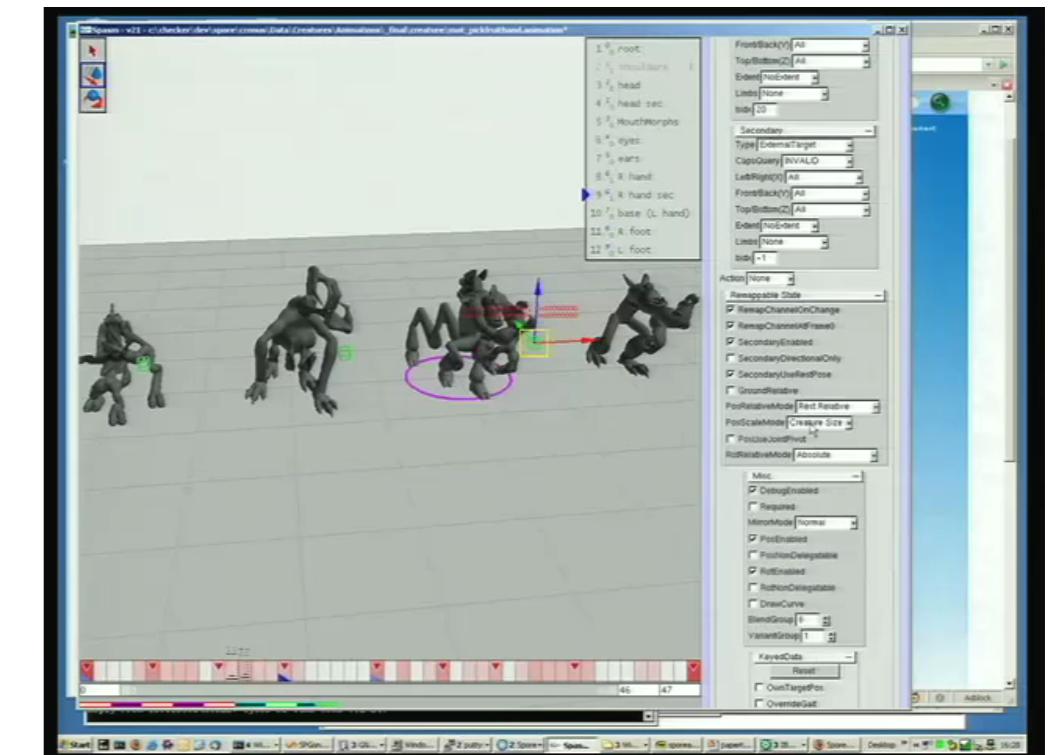


[M. Raibert and J. Hodgins. Animation of Dynamic Legged Locomotion, ACM SIGGRAPH 2001]

[K. Yin et al., SIMBICON: Simple Biped Locomotion Control, ACM SIGGRAPH 2007]

Motion transfert

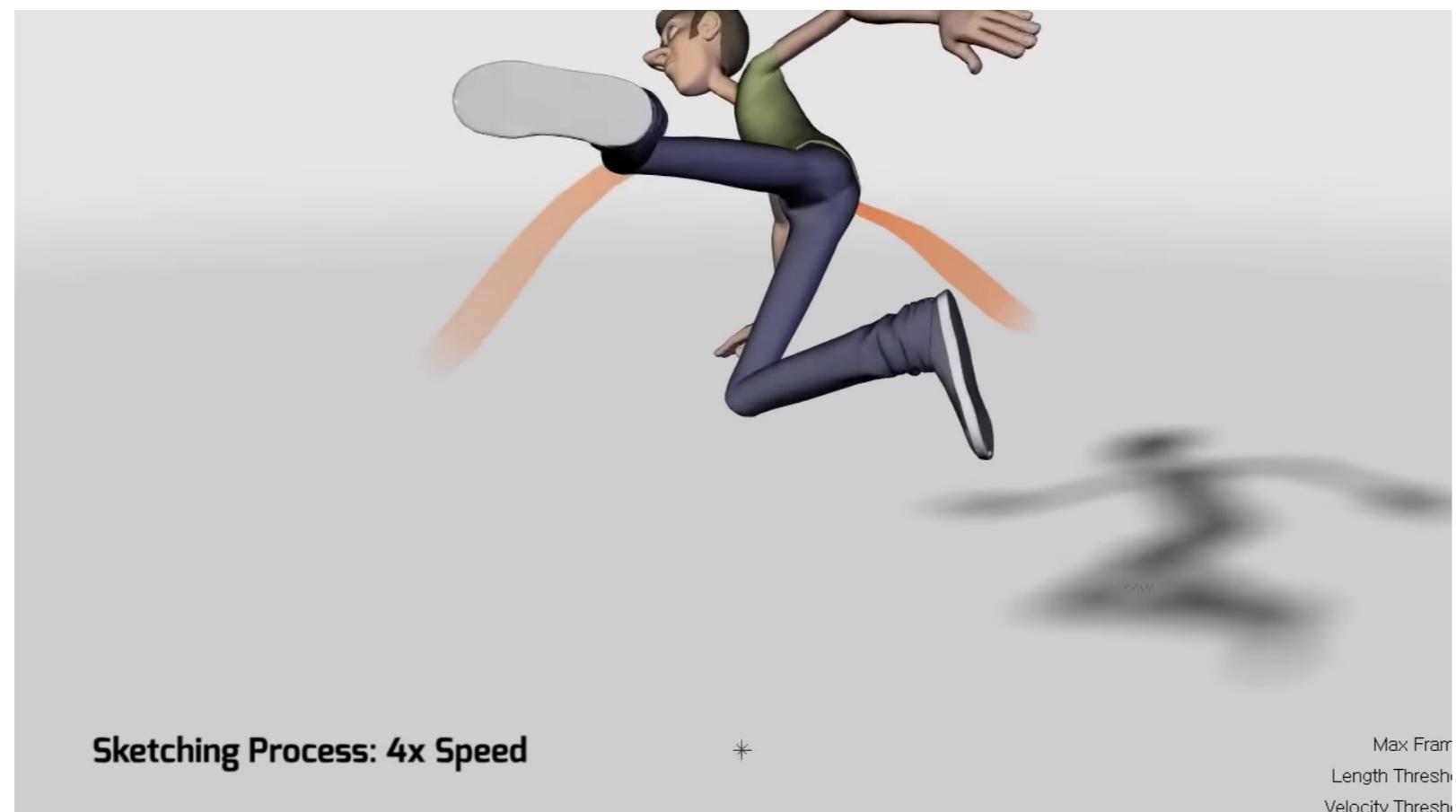
- Local coordinates mapping from skeletal motions
 - [C. Hecker et al., Real-time Motion Retargeting to Highly Varied User-Created Morphologies, SIGGRAPH 2008] (Spore)
- Including shape morphology
 - [Z. Liu et al., Surface based Motion Retargeting by Preserving Spatial Relationship, MIG 2018]



Animation design

Based on the *Line of Action*

- [Guay et al., The Line of Action: an Intuitive Interface for Expressive Character Posing, ACM SIGGRAPH Asia 2013]
- [Guay et al., Space-time sketching of character animation, ACM SIGGRAPH 2015]
- [Choi et al., SketchiMo: Sketch-Based Motion Editing for Articulated Characters, ACM SIGGRAPH 2016]



0:00 / 0:27

0:00 / 0:35

Automatic synthesis of skeletal animation

Seminal works

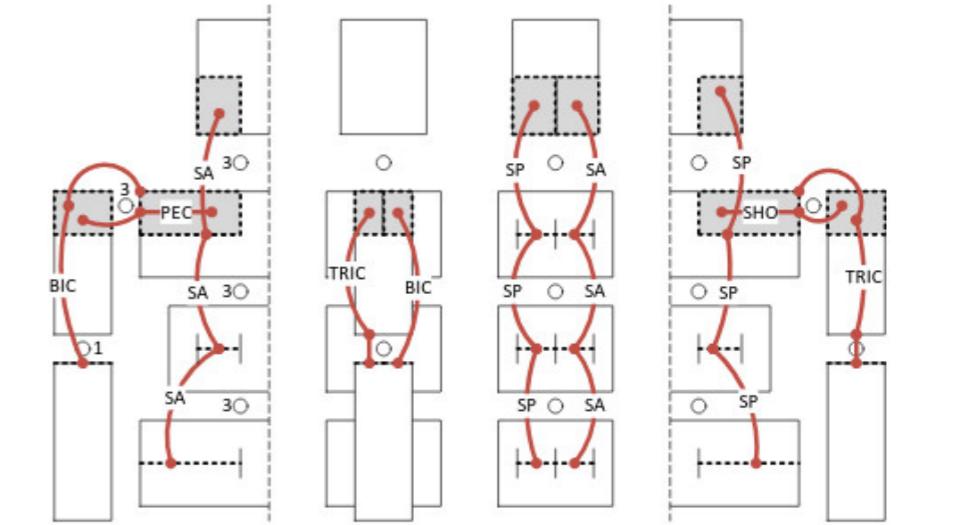
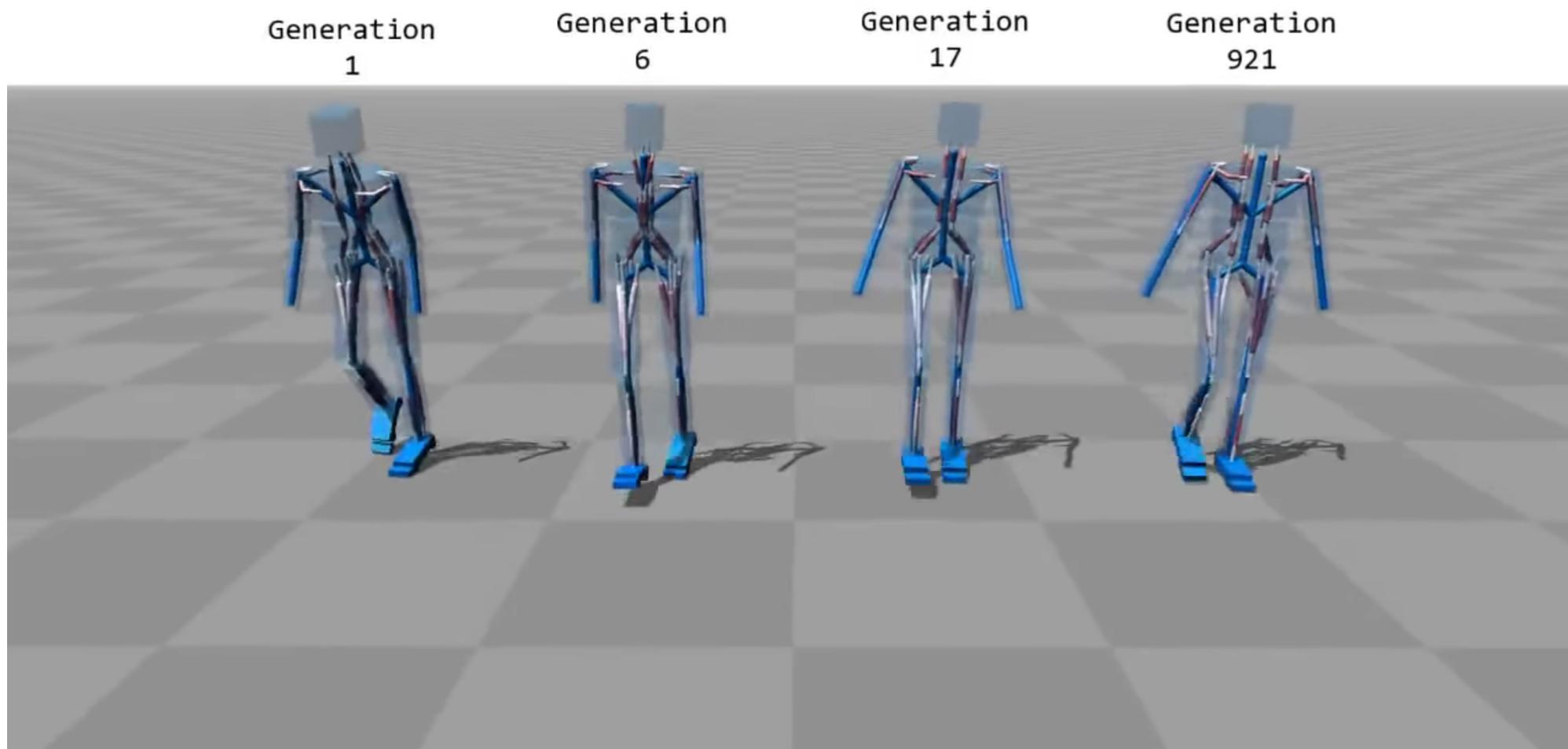
- [Evolving Virtual Creatures. Karl Sims. SIGGRAPH 1994]
- [Automated Learning of Muscle-Actuated Locomotion Through Control Abstraction. Radek Grzeszczuk and Demetri Terzopoulos. SIGGRAPH 1995]
- *Optimization toward objective function coupled with rigid bodies simulations*
- *Morphological variation from genetic algorithm*



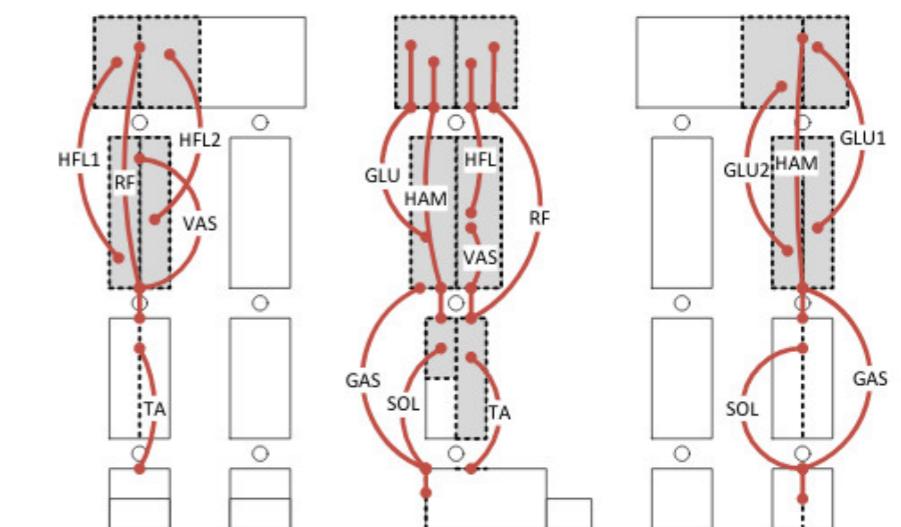
Optimizing muscle activation

- Take into account simple biomechanical model
- Optimize sequence of activation via reinforcement learning

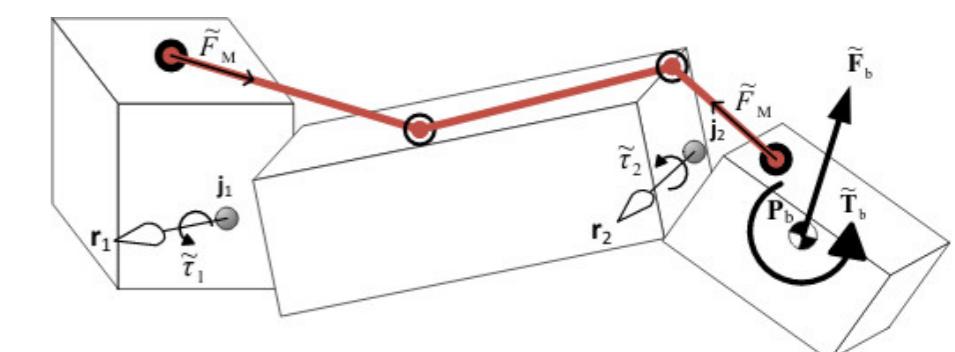
[*Flexible Muscle-Based Locomotion for Bipedal Creatures, T. Geijtenbeek et al. SIGGRAPH Asia 2013.*]



(a) Humanoid upper-body model: front, side arm, side body, and back.



(c) Humanoid lower-body model: front, side and back.

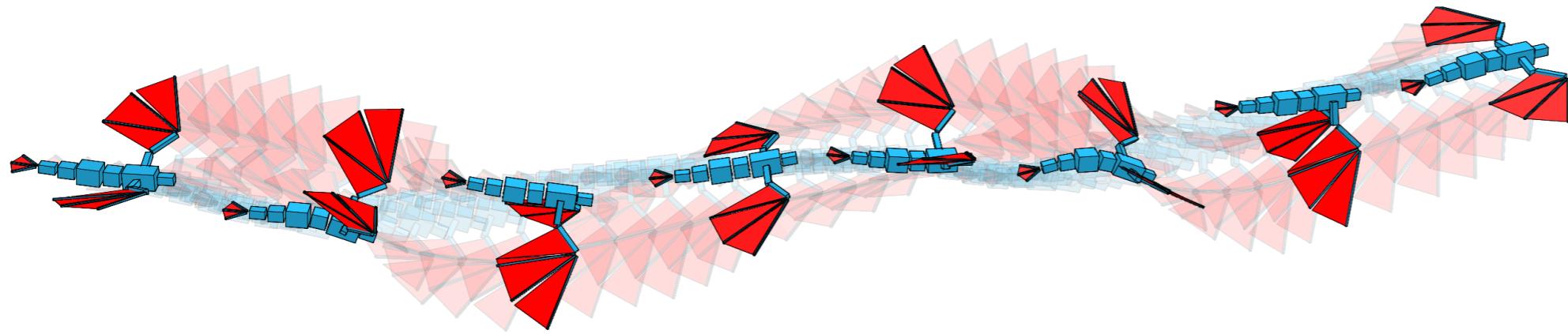


Use of deep learning

Deep reinforcement learning for complex optimization

Learn muscle activation

[Won et al. *How to Train Your Dragon: Example-Guided Control of Flapping Flight*, ACM SIGGRAPH Asia 2017]



Deep learning for real-time motion control

Learn phase of the motion cycle.

Use large data base of motion capture data

[Holden et al., *Phase-Functioned Neural Networks for Character Control*, ACM TOG 2017]



Animating crowds of characters

Interaction between particles

Interaction as **force field** (interact at distance)

Example of usage

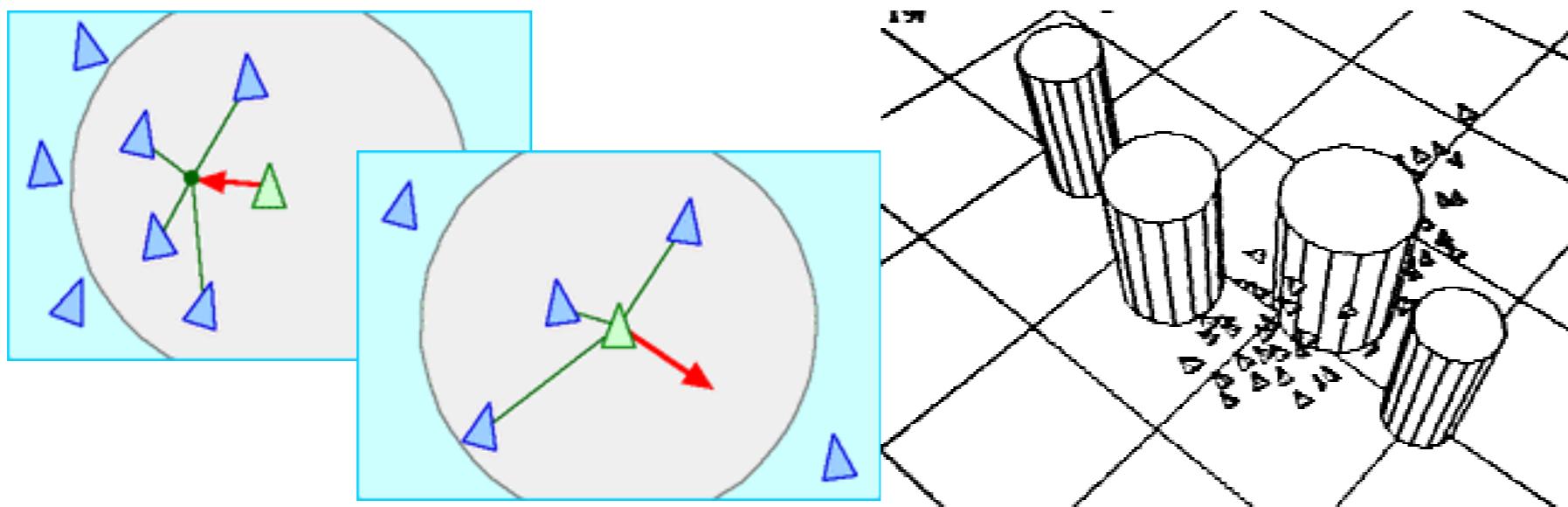
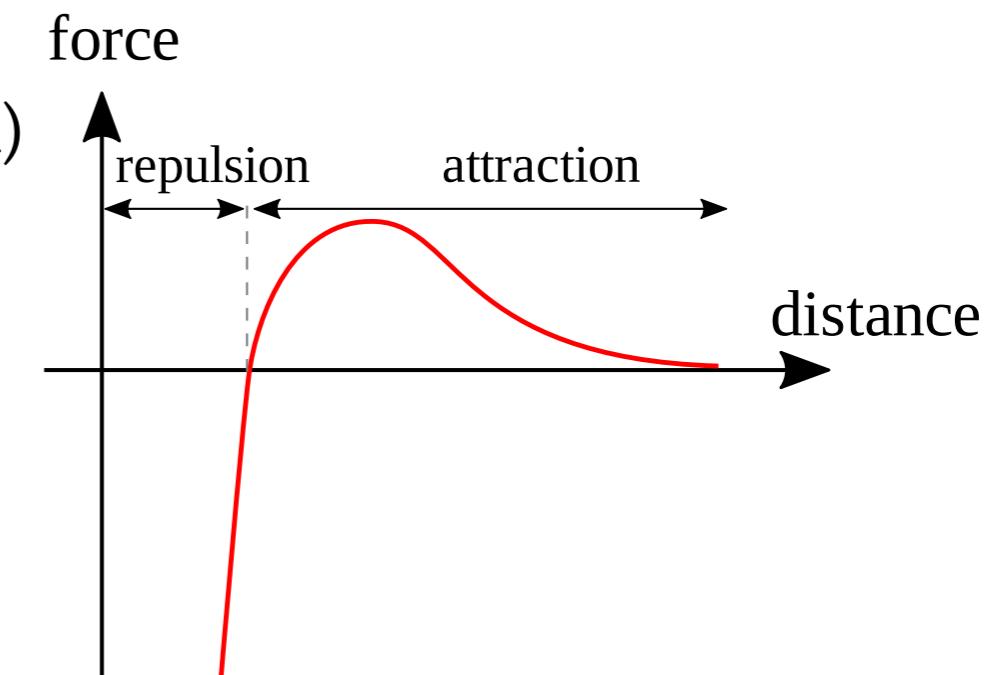
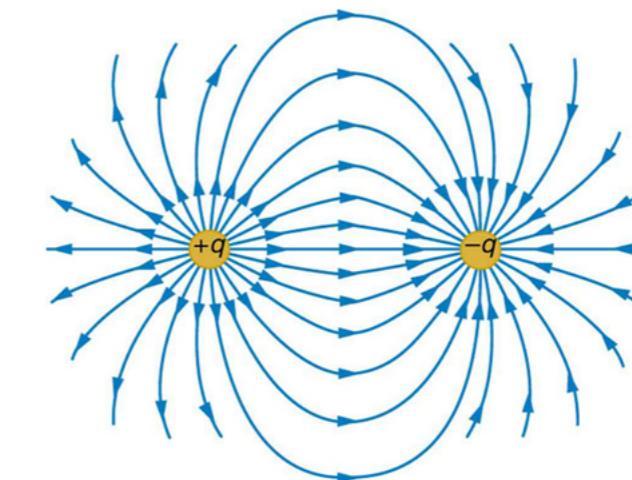
- Models crowd of life-like characters at large scale

Inspired from physics particles forces (ex. Lennard-Jones potential)

Attraction at *long-range*

Repulsion at *short-range*

- First model: **Boids** Craig Reynolds 1987
- Extended later to human crowd modeling



Boids Model

Introduced by

[Craig Reynolds. *Flocks, Herds, and Schools: A Distributed Behavioral Model*, SIGGRAPH 1987]

[Craig Reynolds. *Steering Behaviors For Autonomous Characters*. Proceedings of Game Developers, 1999]

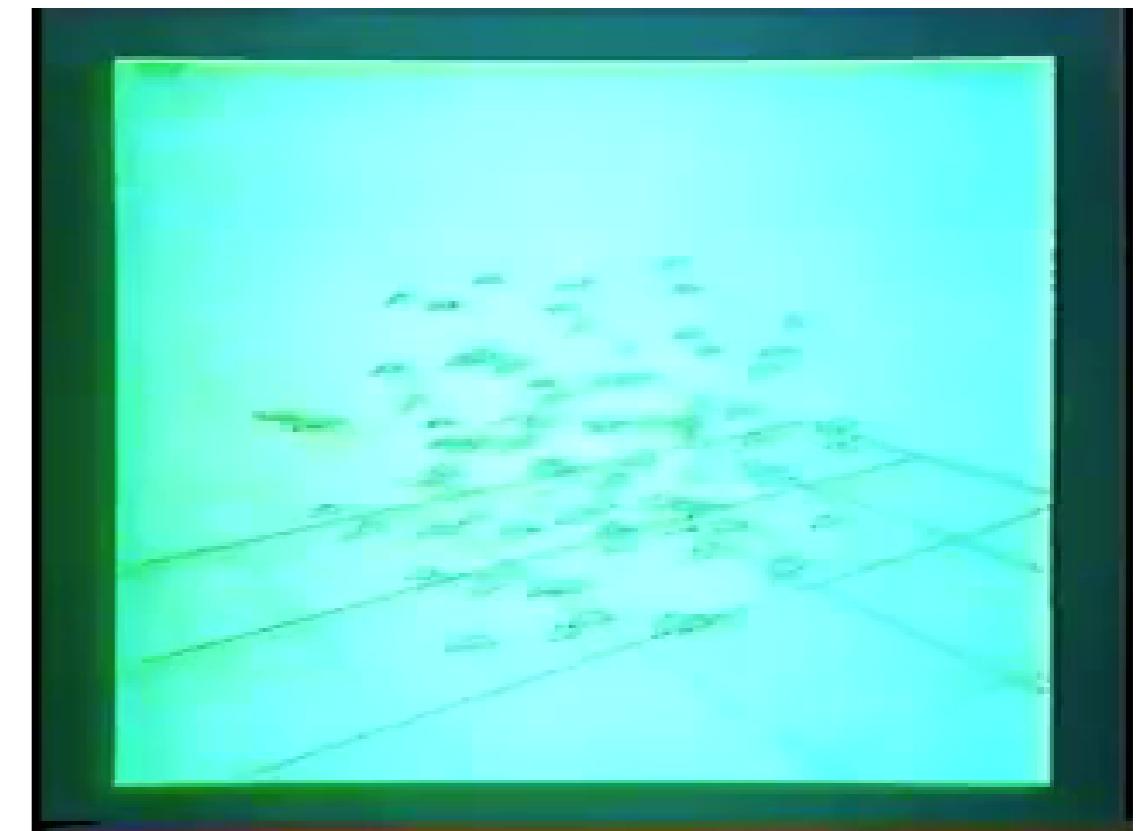
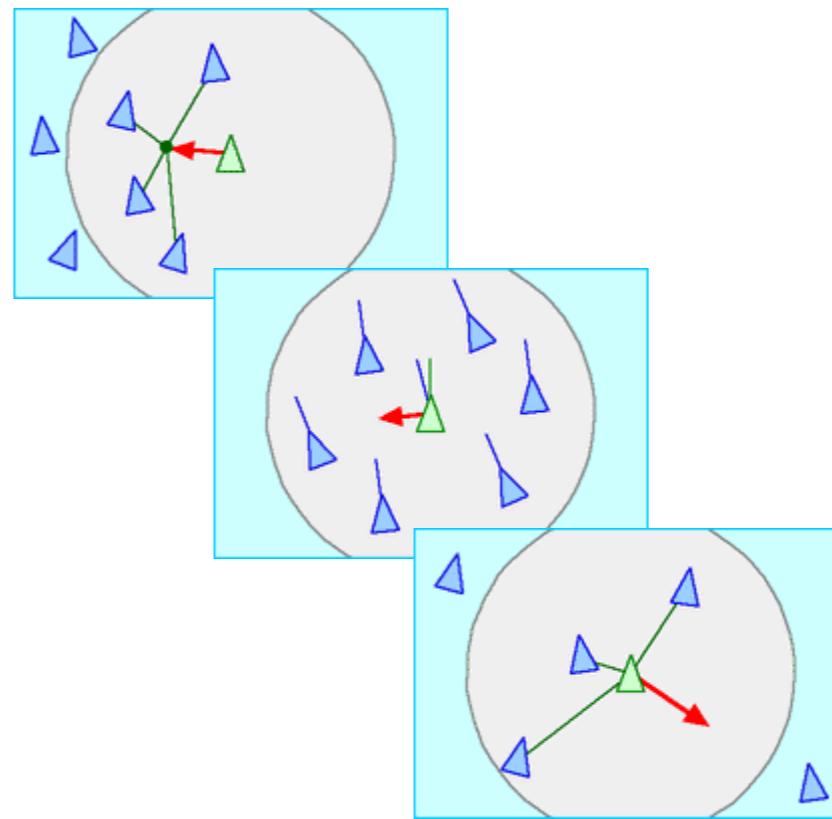
A boid is defined by its

- Position
- Speed
- Forces acting on it

Three basic local *steering behaviors* to model flocks

- **Cohesion** between local particles
- **Alignment** between local particles
- **Separation** between too close particles

=> Leads to emerging global behaviors.



Original video in 1986 (C. Reynolds)

Boids Model - Basic model.

- Set random initial position/speed to N particles.
- Set attraction/repulsion force depending on pairwise distances

$$F(p_i) = \sum_j f(\|p_j - p_i\|) \frac{p_j - p_i}{\|p_j - p_i\|}$$

Example

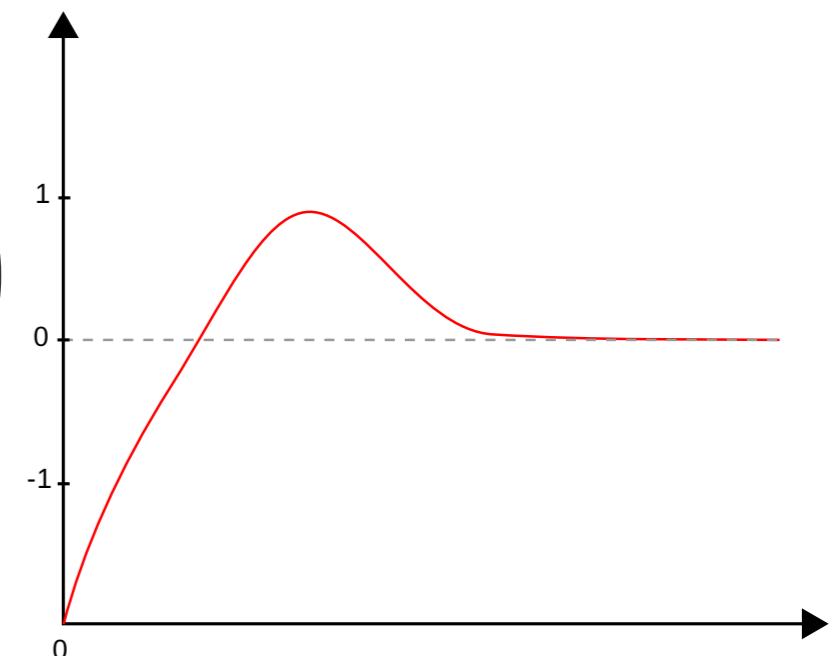
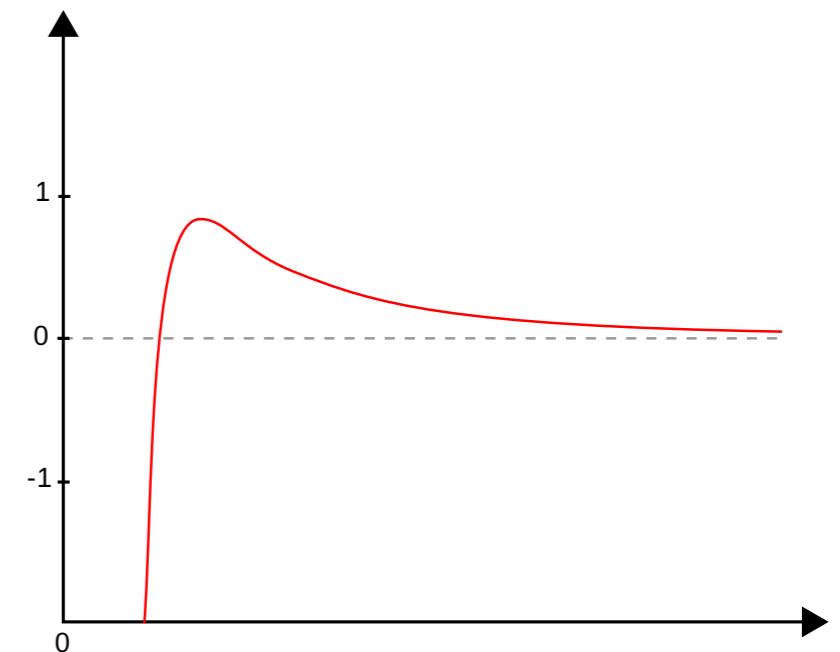
- Inverse of distance $f(x) = \frac{\alpha_1}{x^2} - \frac{\alpha_2}{x^4}$

- Exponential/Gaussian $f(x) = \alpha_1 \exp\left(-k \left(\frac{x - x_0}{x_0}\right)^2\right) - \alpha_2 \exp\left(\frac{x}{x_0}\right)$

- Integrate position and speed through time

$$v^{t+\Delta t}(p_i) = v^t(p_i) + \Delta t F(p_i^t)$$

$$p^{t+\Delta t}(p_i) = p^t(p_i) + \Delta t v^{t+\Delta t}(p_i)$$



Boids Model - Complexity.

Trivial implementation:

```
struct particle { vec3 p, v, f; };

std::vector<particle> boids;

// Initialize N boids ...
// ...

// compute pairwise force
for(int i=0; i<N; ++i)
{
    for(int j=0; j<N; ++j)
    {
        if( i!=j )
        {
            const vec3& pi = boids[i].p;
            const vec3& pj = boids[j].p;

            boids[i].f += force( norm(pi,pj)) / (pi-pj)/norm(pi-pj);
        }
    }
}

// integration
for(int i=0; i<N; ++i)
{
    boids[i].v = boids[i].v + dt * boids[i].f;
    boids[i].p = boids[i].p + dt * boids[i].v;
}
```

- What is the complexity (wrt. N) of this algorithm ?
- Can you think of a way to be more efficient for large N ?

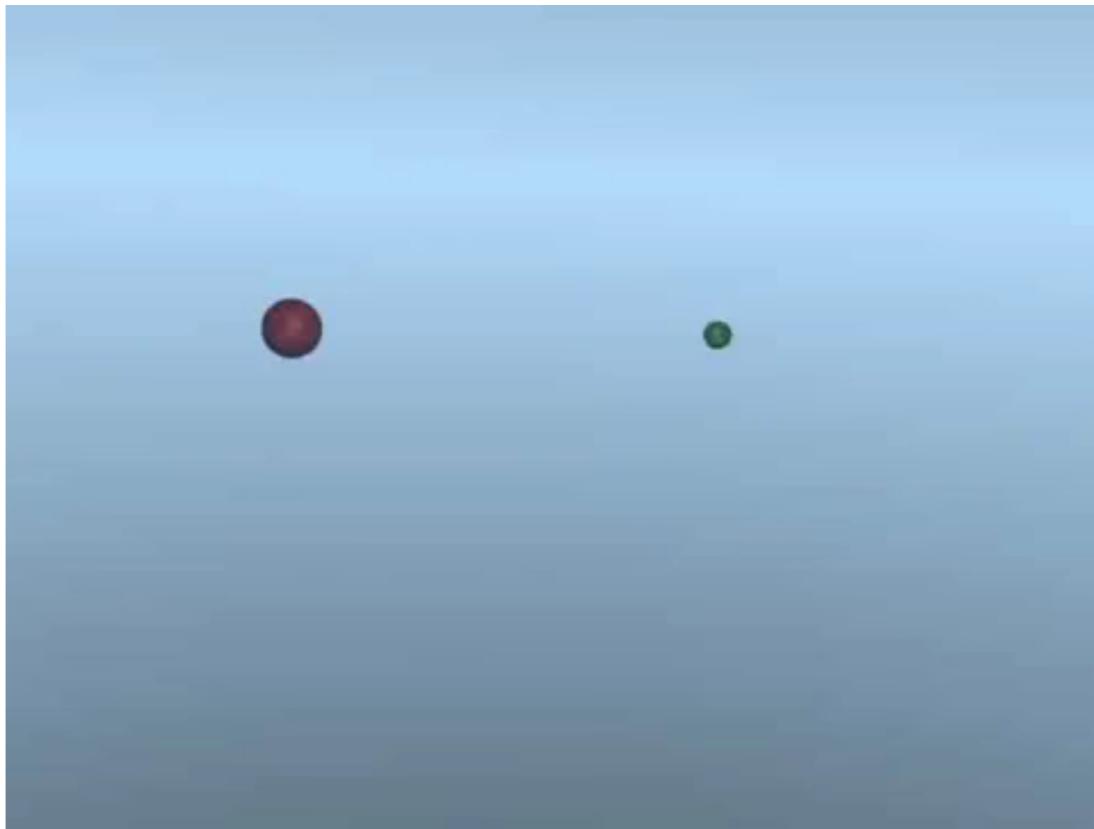
Boids Model - Usage and limitations

- Well adapted to flocks (birds, fishes - looking behavior)
- Display particles using 3D animated model

Additional behaviors

- Objective position/speed value
- Constraints: Obstacle avoidance, limited velocity
- Pursue and evade target/other particles - follow the leader, predators, etc.

- *Is collision between particles possible ?*
- *Human displacement are mostly guided by vision, what key element is missing in the basic boids force-based model ?*



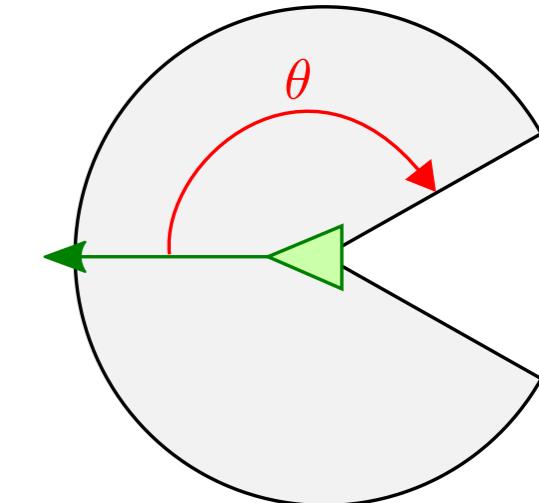
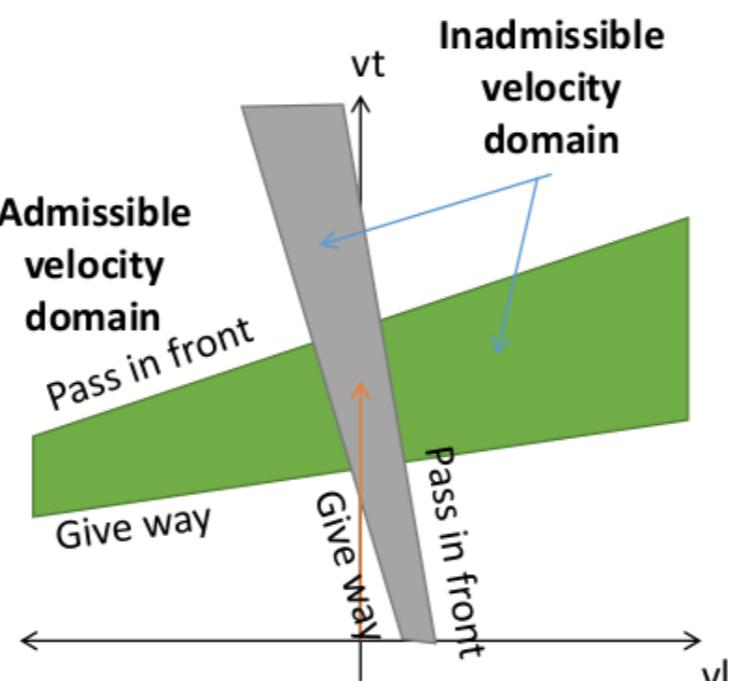
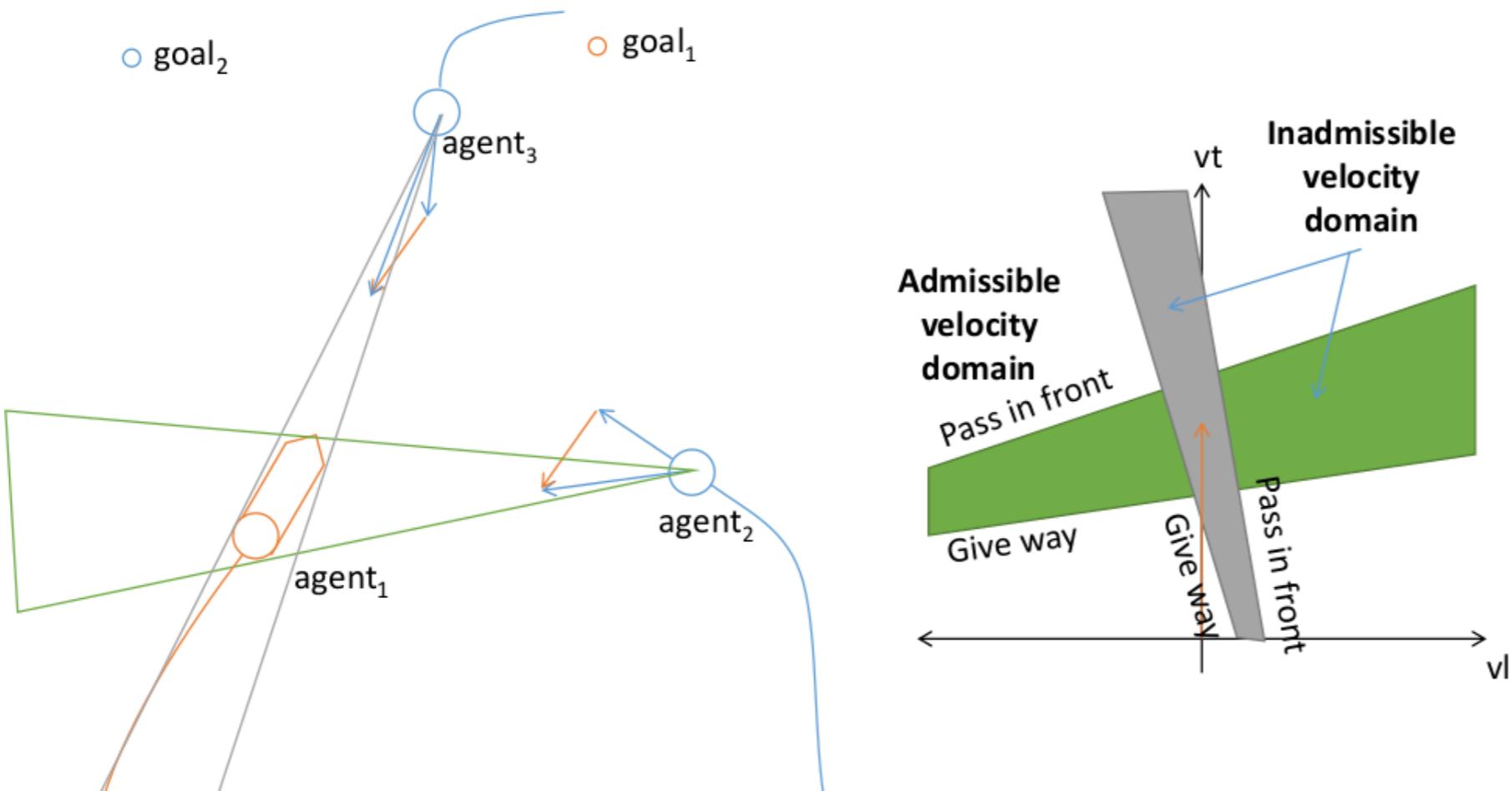
Boids Model - Extensions

Improving force computation

- Vision-based force computation (angle, speed) : limited view angle

Improving collision avoidance

- Velocity-based



[*Experiment-based Modeling, Simulation and Validation of Interactions between Virtual Walkers. J. Pettré et al. SCA 2009*]

Vision based displacement

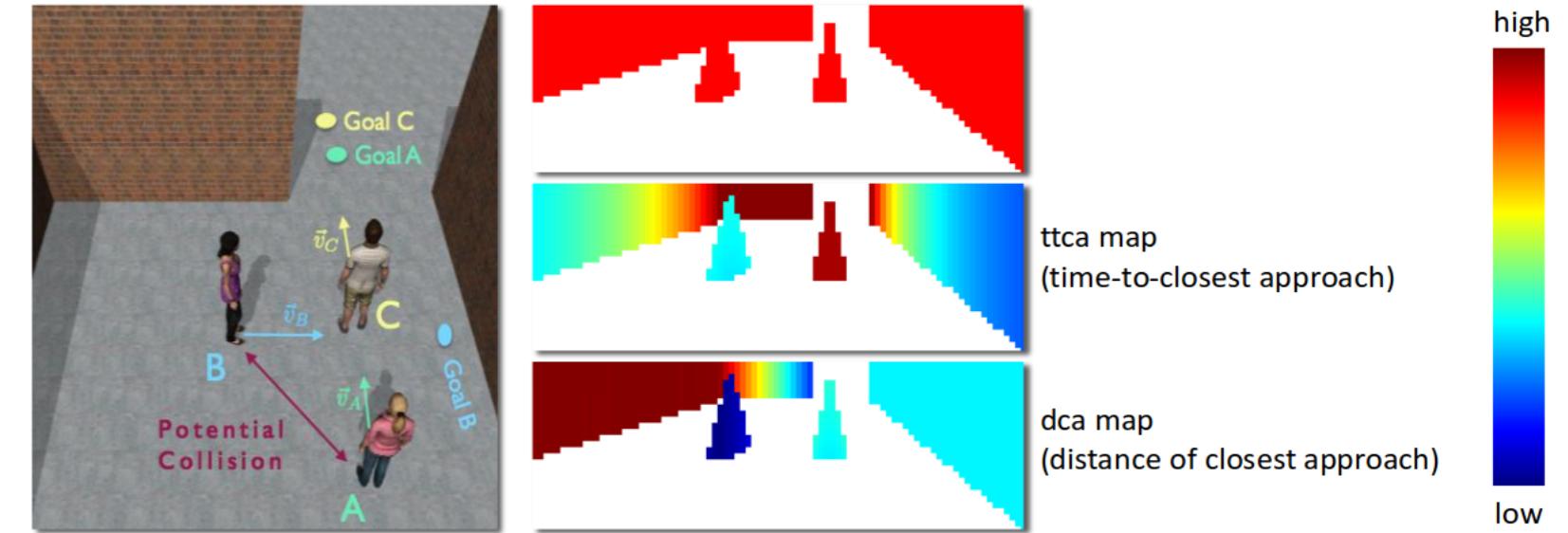
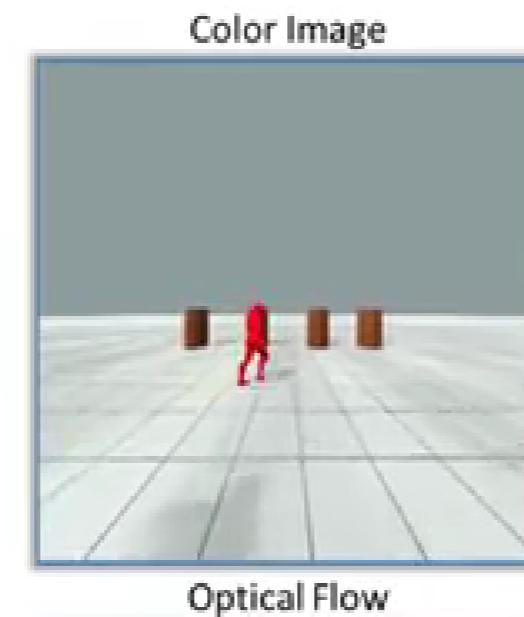
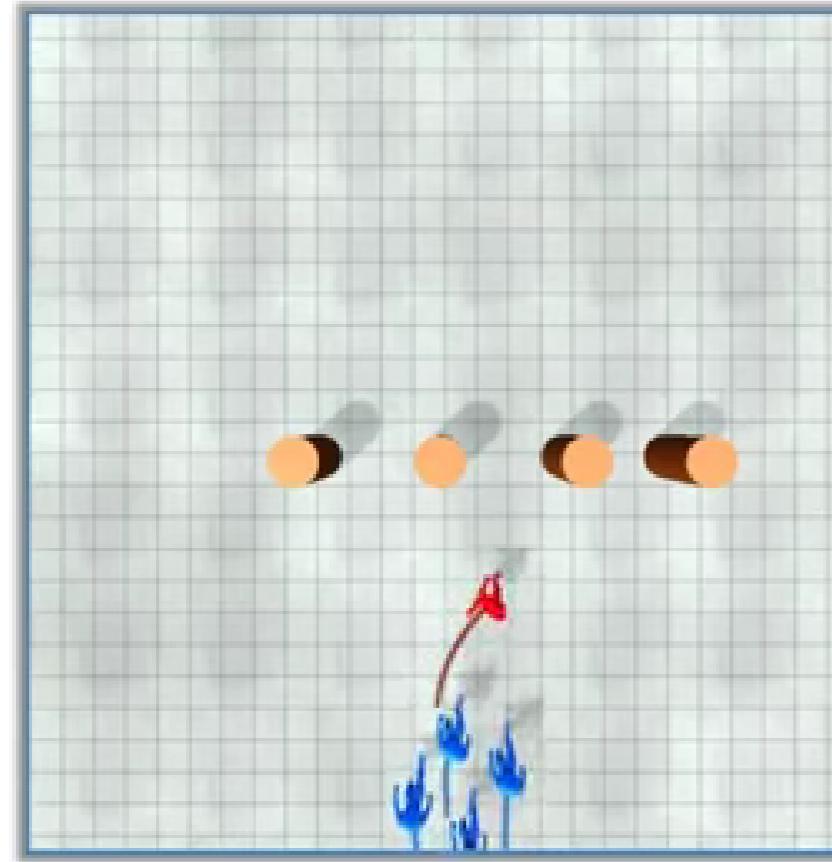
Render vision for each individual agent

Compute optical flow u .

Obstacles are approaching when $\text{div}(u) > 0$

Best results, but high computational cost.

Following with Obstacles



[*A Synthetic-Vision Based Steering Approach for Crowd Simulation.* J. Ondrej et al. SIGGRAPH 2010]

[*Character navigation in dynamic environments based on optical flow.* A. Lopez et al. EG 2019]

Example of crowd simulation software

Golaem

In Rennes

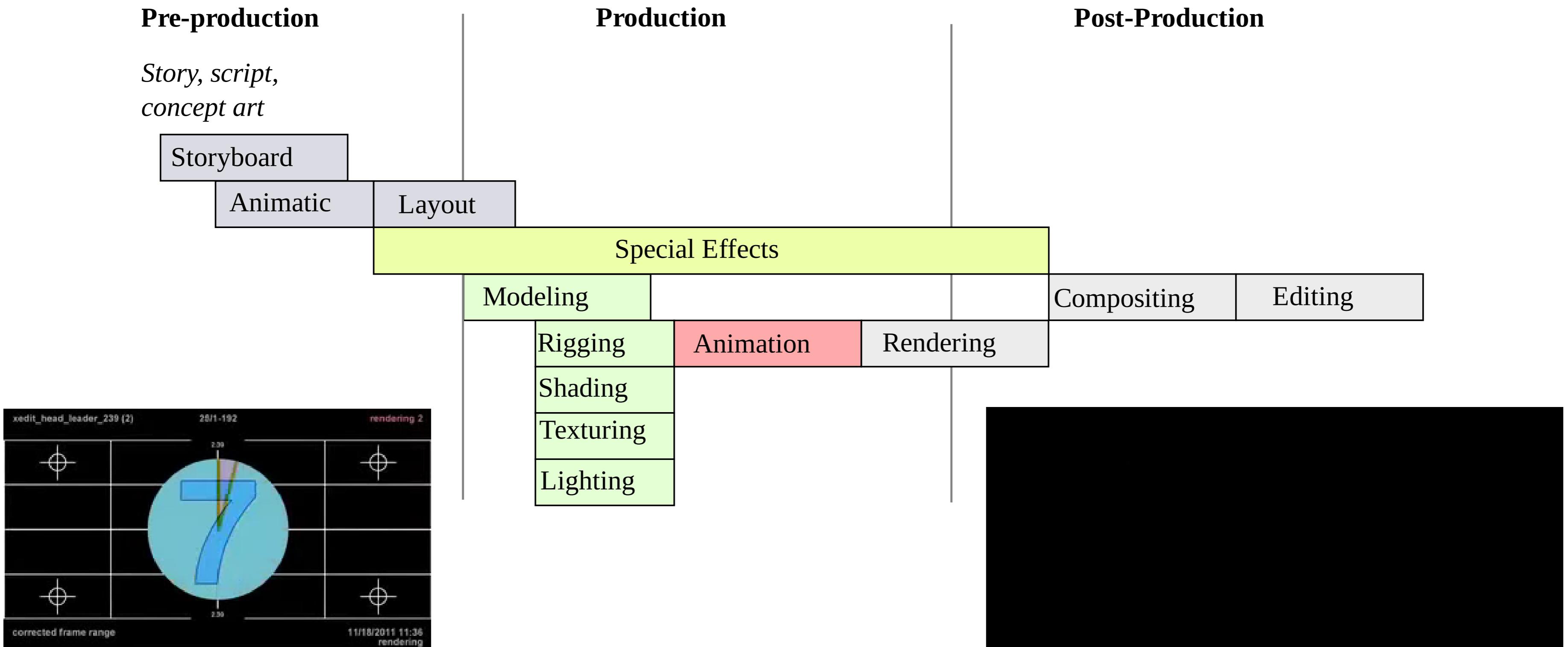


Production Pipeline

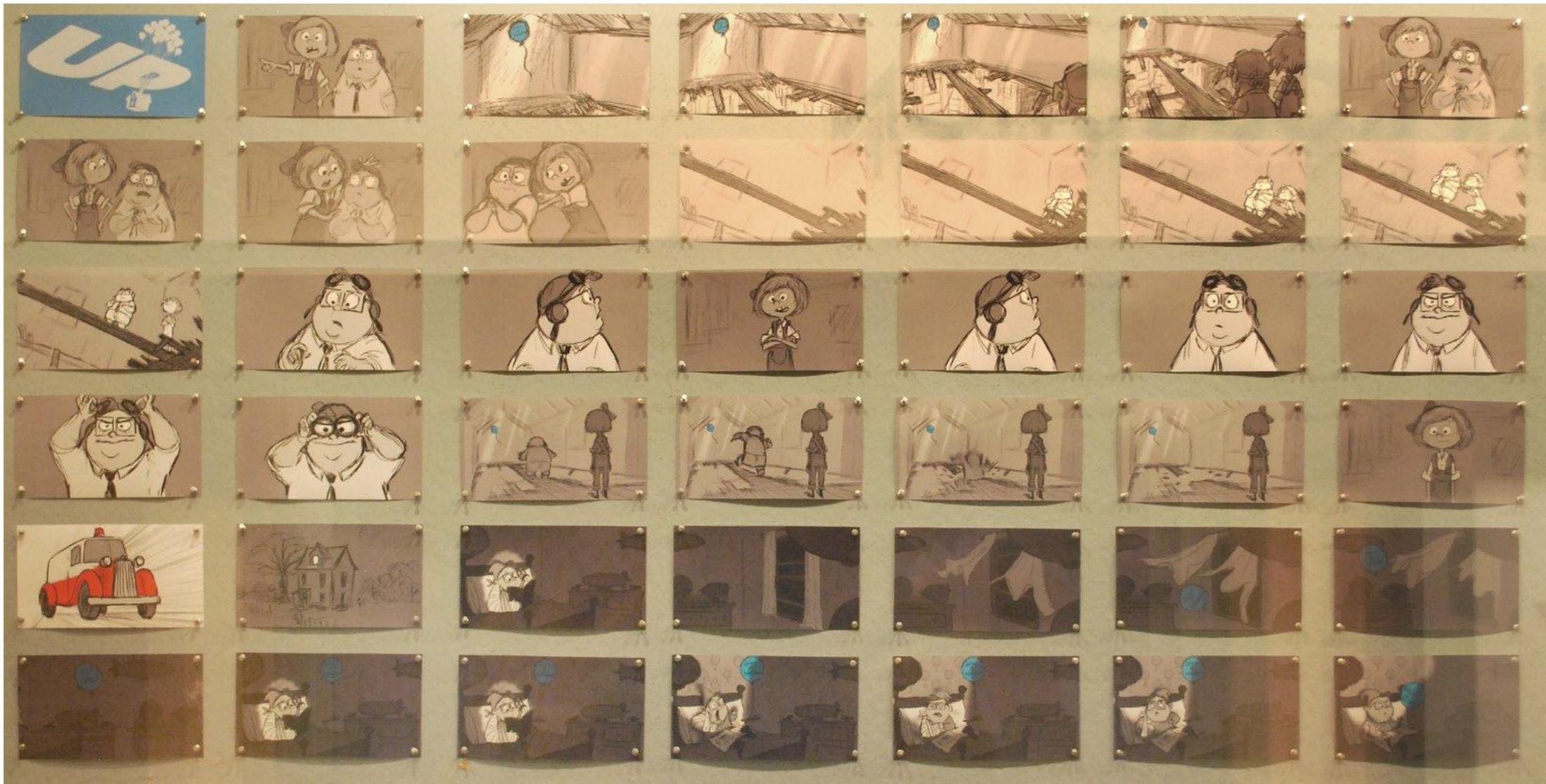
Case of Animation Cinema production

Production Pipeline

Fundamental structure for VFX/animation movie production.



Story-board



Few 2D drawings: express the story

Before mostly non-technical - artistic/creative based

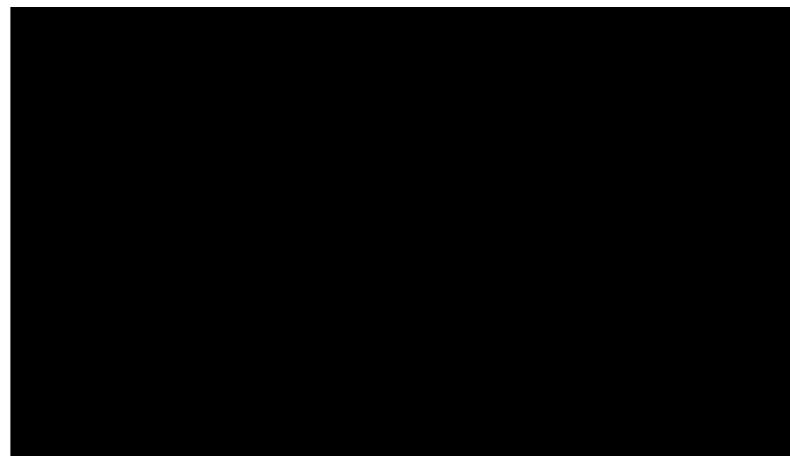
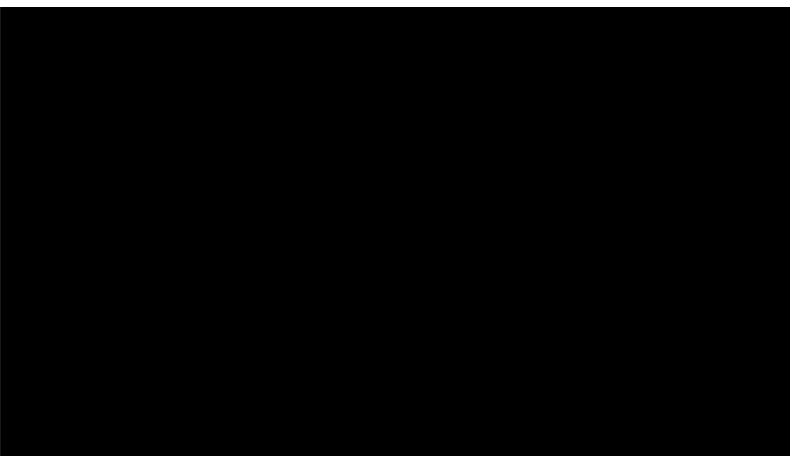
Currently Strong increase of Storytelling-related researchs in CG

ex. [Disney Research Studios](#), [Anima team at Inria](#)

Animatic

≈ Animated story-board, Various format

Rough sense of timing, visual, action: details not necessarily followed precisely in the final version.



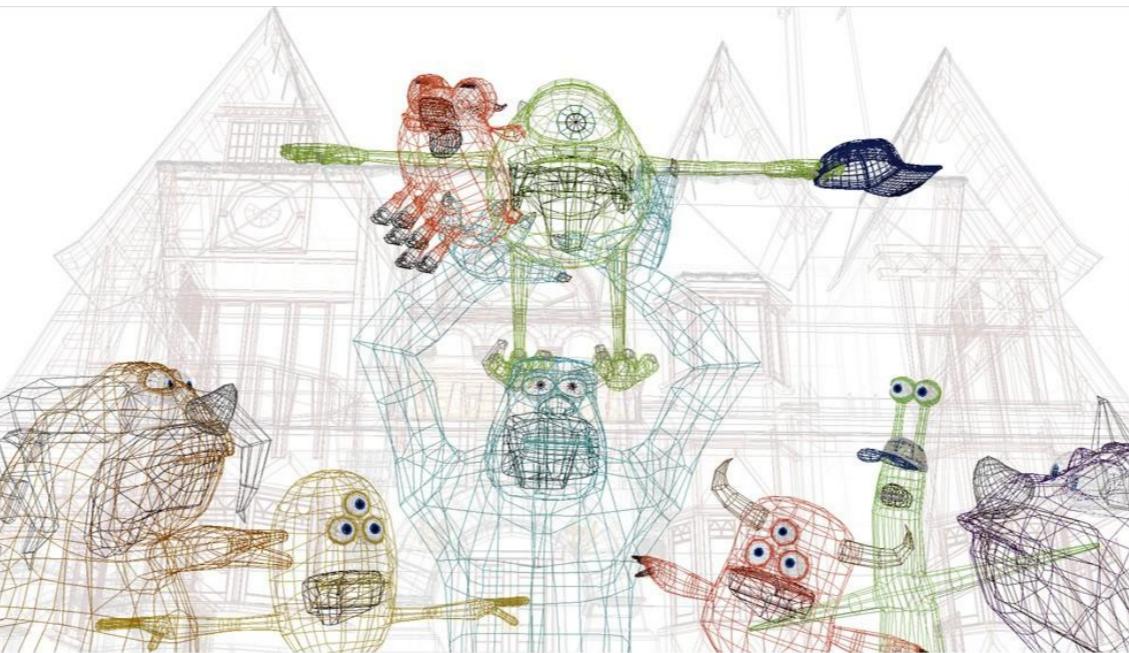
Layout: Moving into 3D

1st step: Rough 3D modeling and placement of

- Camera: visual field, perspective
3D much more constrained than 2D drawings
- Shape volumes, continuity
No details: face, etc.
Choice between 3D/2D elements



"MONSTERS UNIVERSITY" Progression Image 1 of 6: STORY
©2013 Disney•Pixar. All Rights Reserved.



"MONSTERS UNIVERSITY" Progression Image 3 of 6: MODELING
©2013 Disney•Pixar. All Rights Reserved.



"MONSTERS UNIVERSITY" Progression Image 4 of 6: LAYOUT
©2013 Disney•Pixar. All Rights Reserved.

3D Modeling

In production

- Polygonal mesh modeling

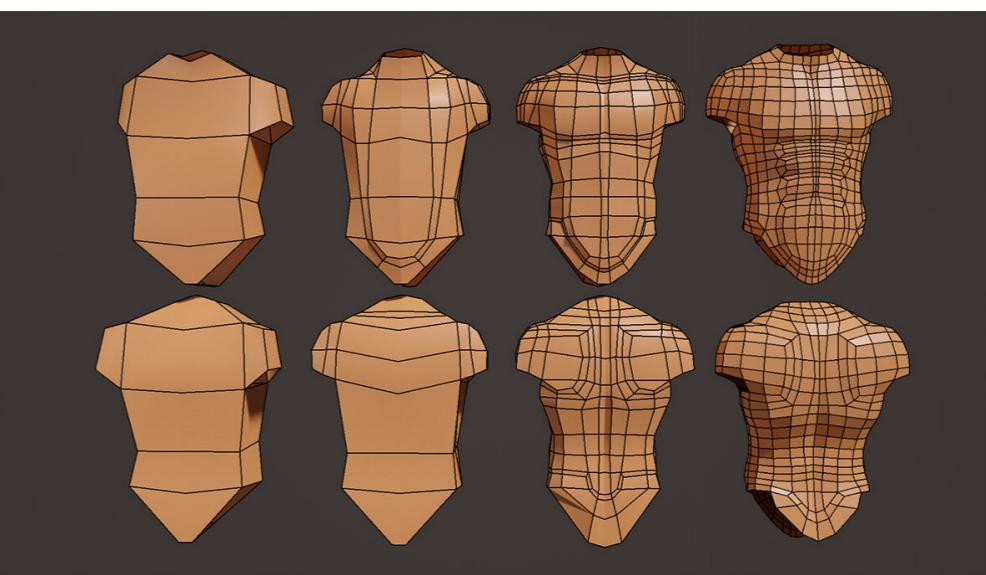
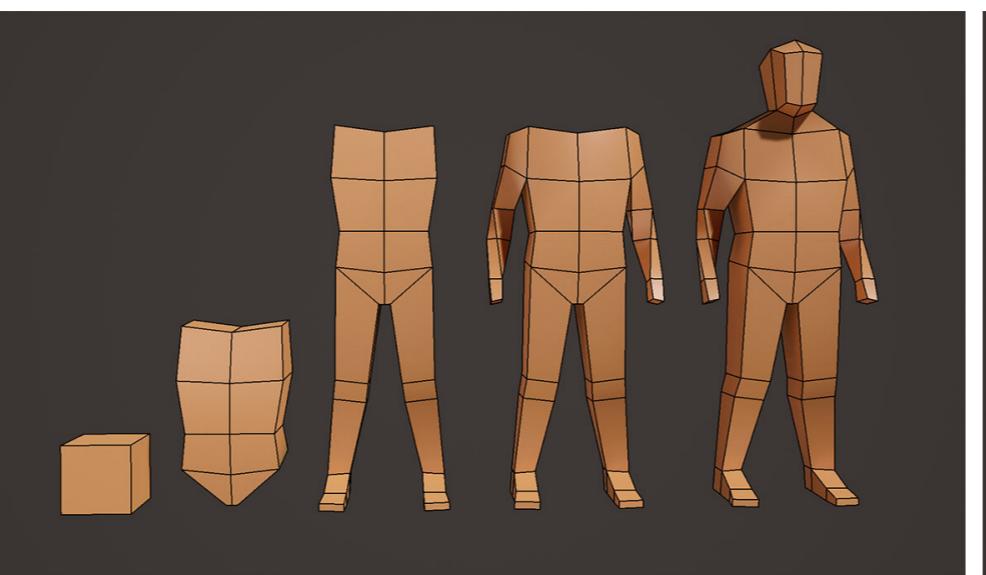
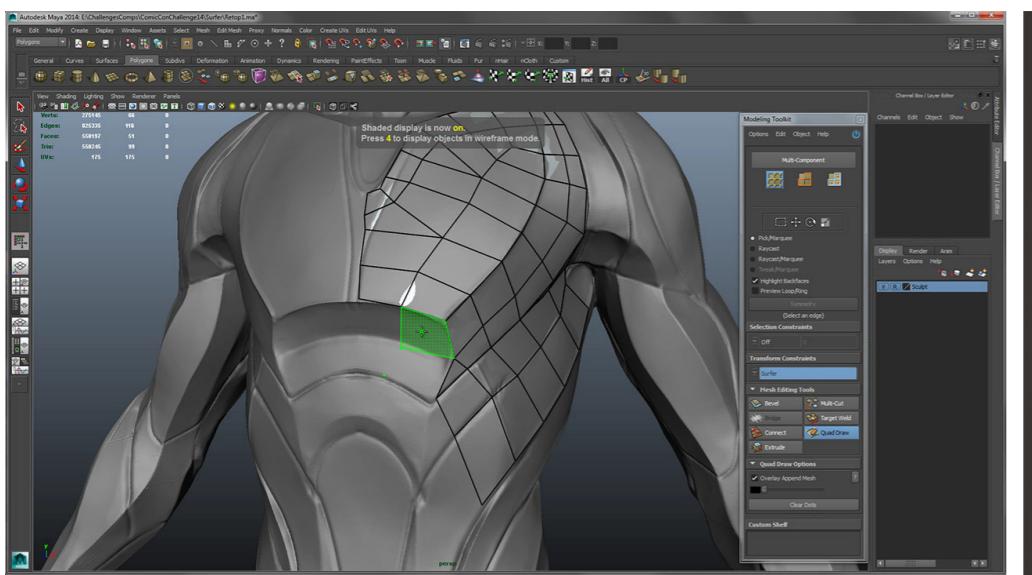
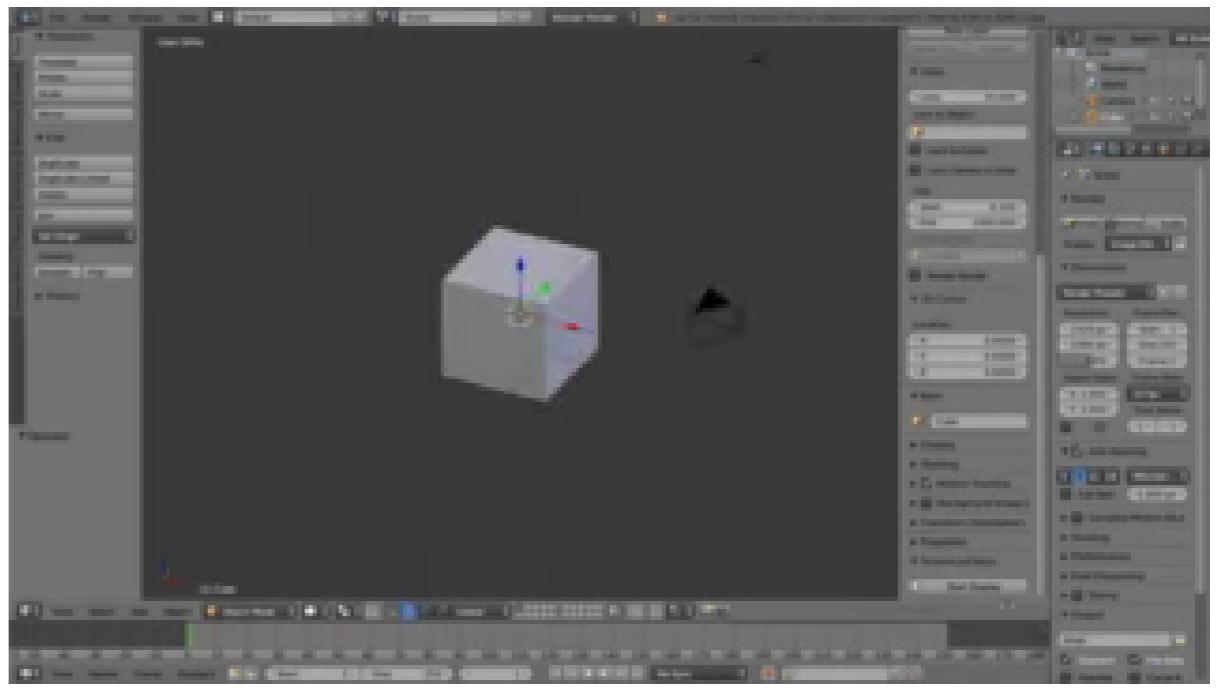
Coarse to fine approach

1. *Low res modeling (extrusion)*
2. *Subdivide, Refine*

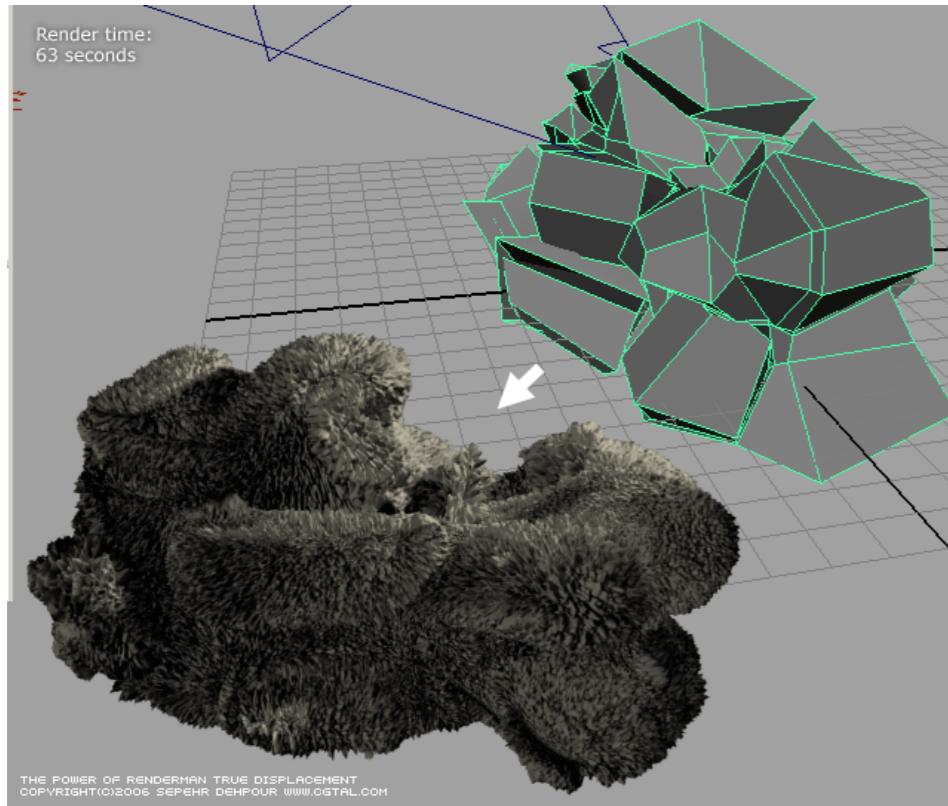
- Parametric (NURBS) modeling

Everything else is "VFX"

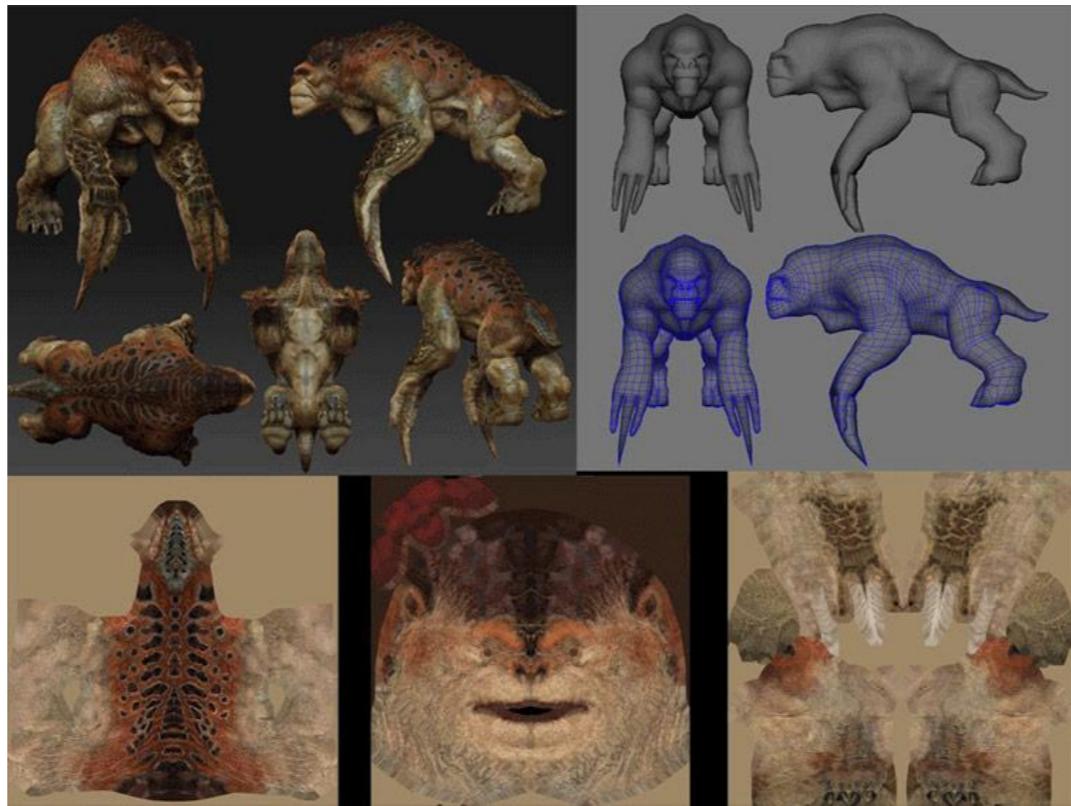
Common tools: Maya, 3DSMax, Cinema4D, Blender, etc.



Modeling appearance - Rendering purpose



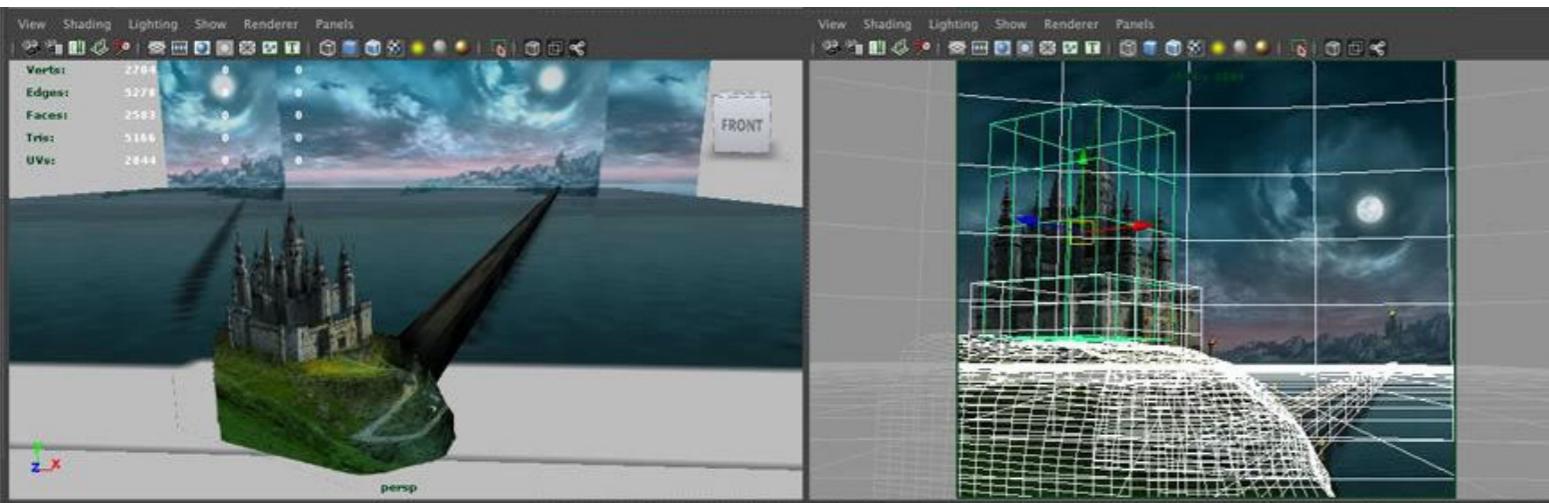
Shading



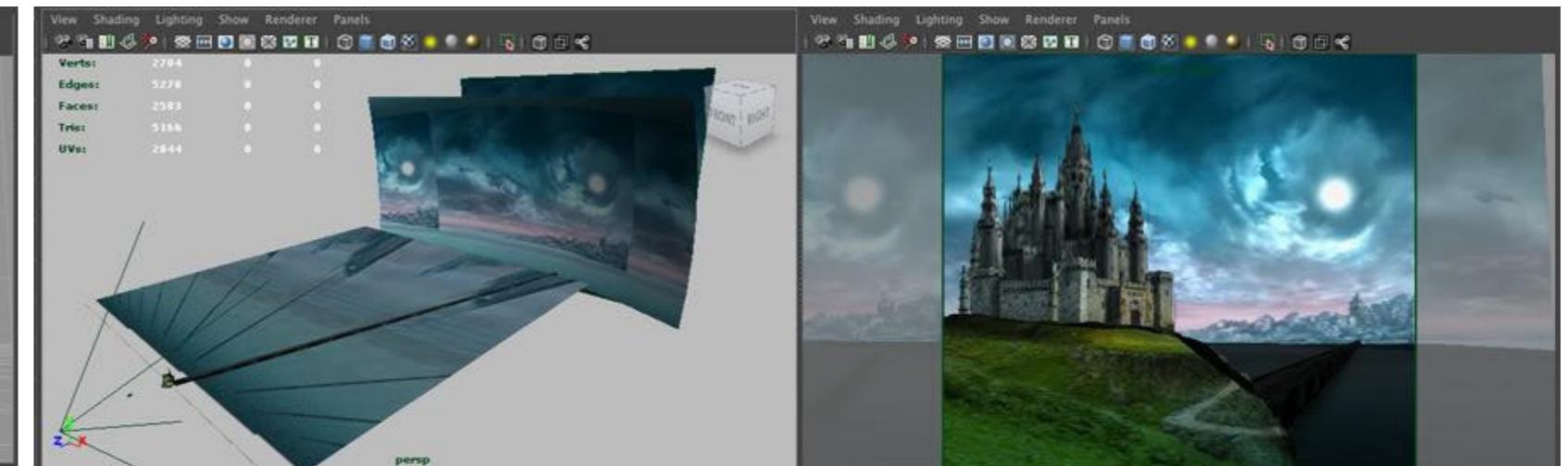
Texturing



Lighting



Mate painting



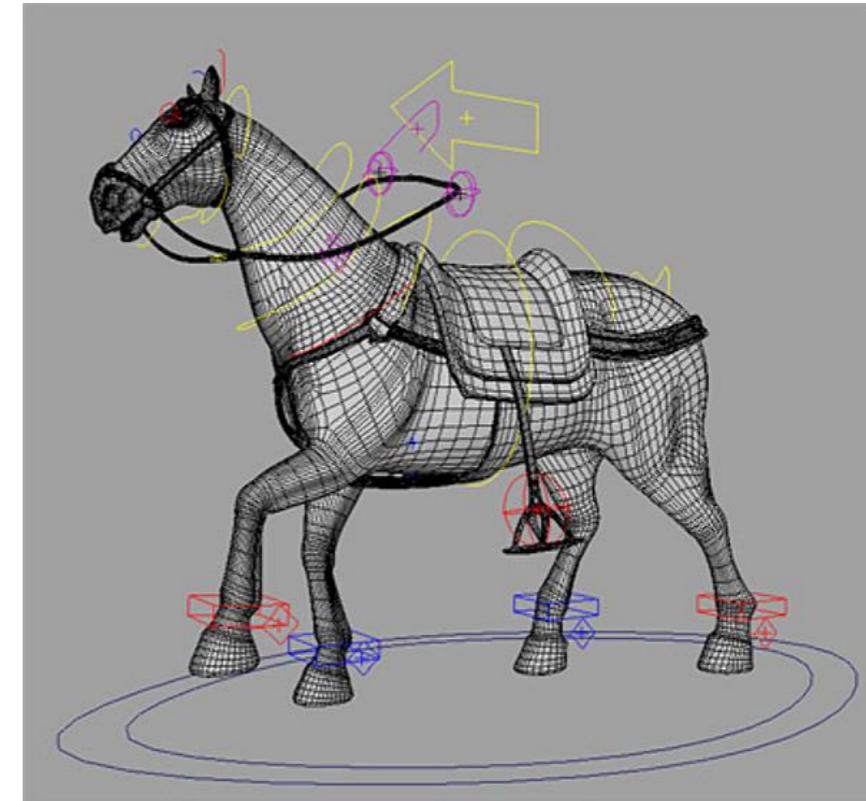
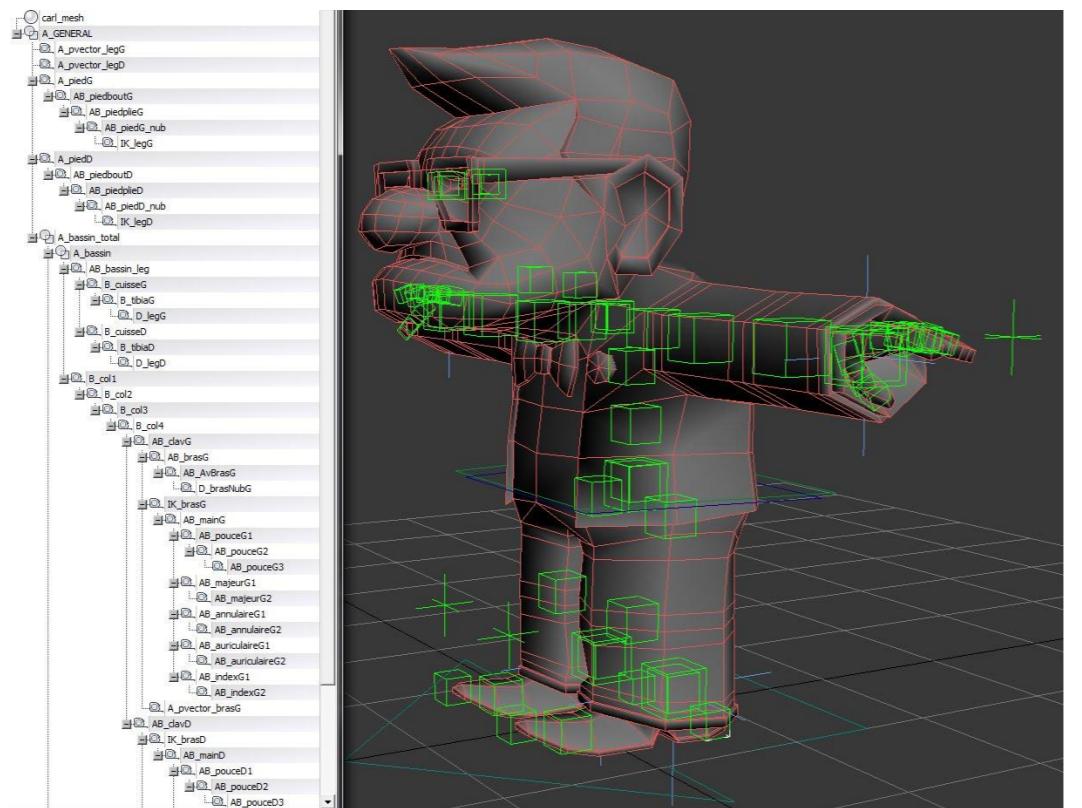
Rigging

Attach deformation handles to the mesh

Each handle (controler) is associated to a deformation - degrees of freedom

Rigging is a technical part

Python script, Mel (Maya), Lua, etc.



Animation

In production terminology: Animation = Key-frame animation of the rigged character
Set animation curves on rig controllers

Everything else is VFX



Animating the walk cycle (×40)



Result

Up to 75% of artists production studios are animators

Animation = The key element - higher cost - for production studios

One animator → 1-10 s of animation per day

Animation sub-parts

1- Posing the *key frames*

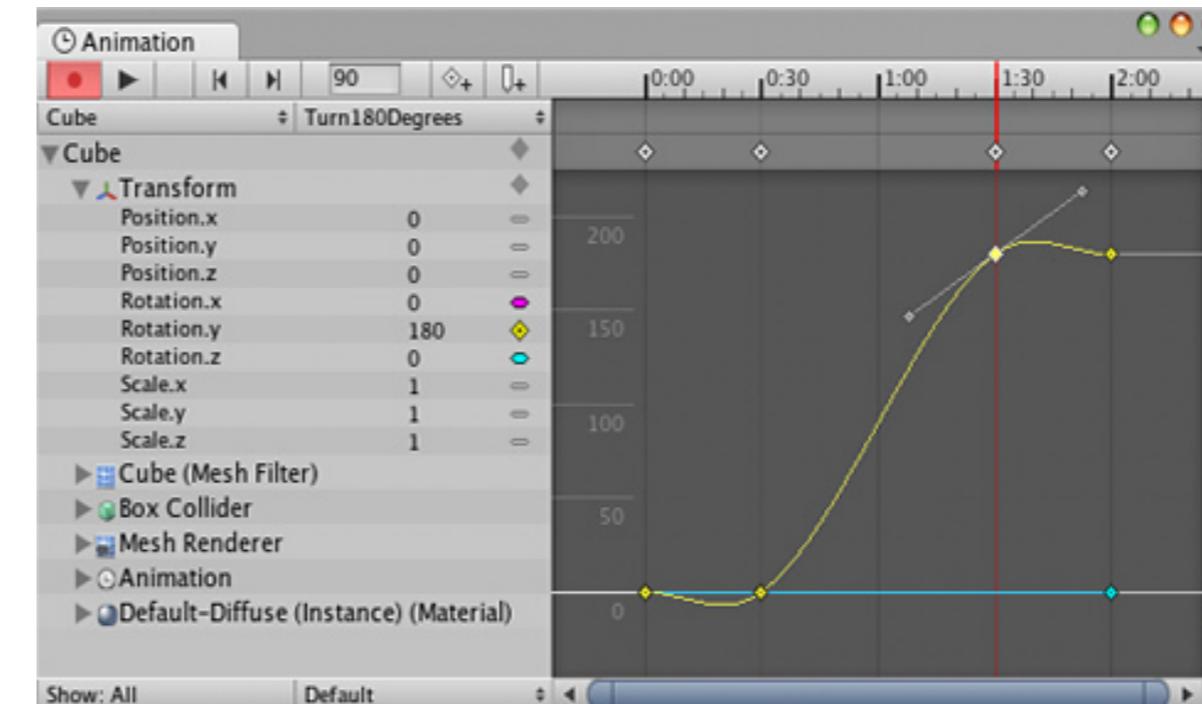
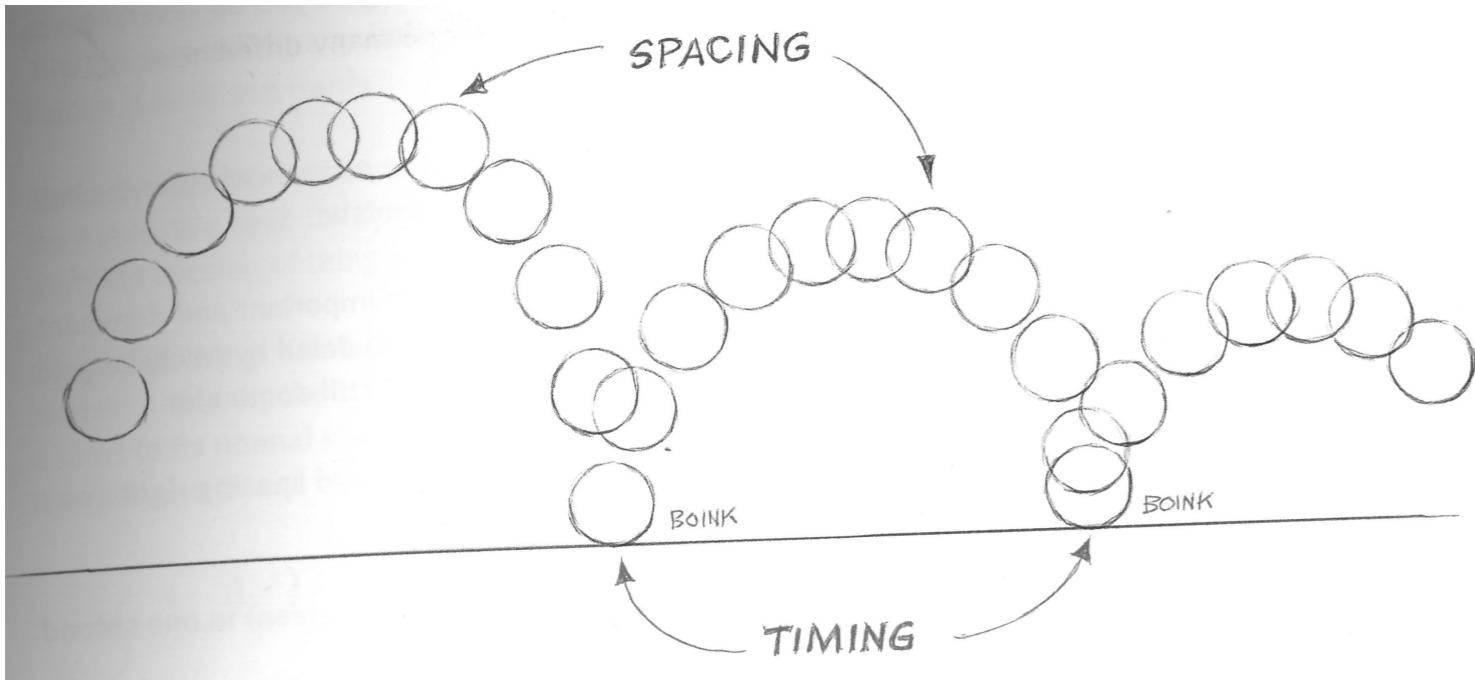
Set the main general posture of the character

*Linked to geometric **character deformation**, time is not involved*



2- Animating the in-betweens

- **Timing** : Place key frames at specific times (global length of an action)
- **Spacing** : Speed of the interpolation (dynamic of the action)



Special Effects (VFX)

Everything which is not handled by traditional modeling/rigging/animation

Physics (explosion, fluids, dynamic hairs, cloth, ...), particles systems, complex shape, crowd, etc.

Technical R&D part: One element can lead to the development of a dedicated system.

Main software: Houdini (SideFX)



Post Production

Compositing

Blend all layers: Rendered and real ones

Note: Rendering of color layers but also depth and normals.

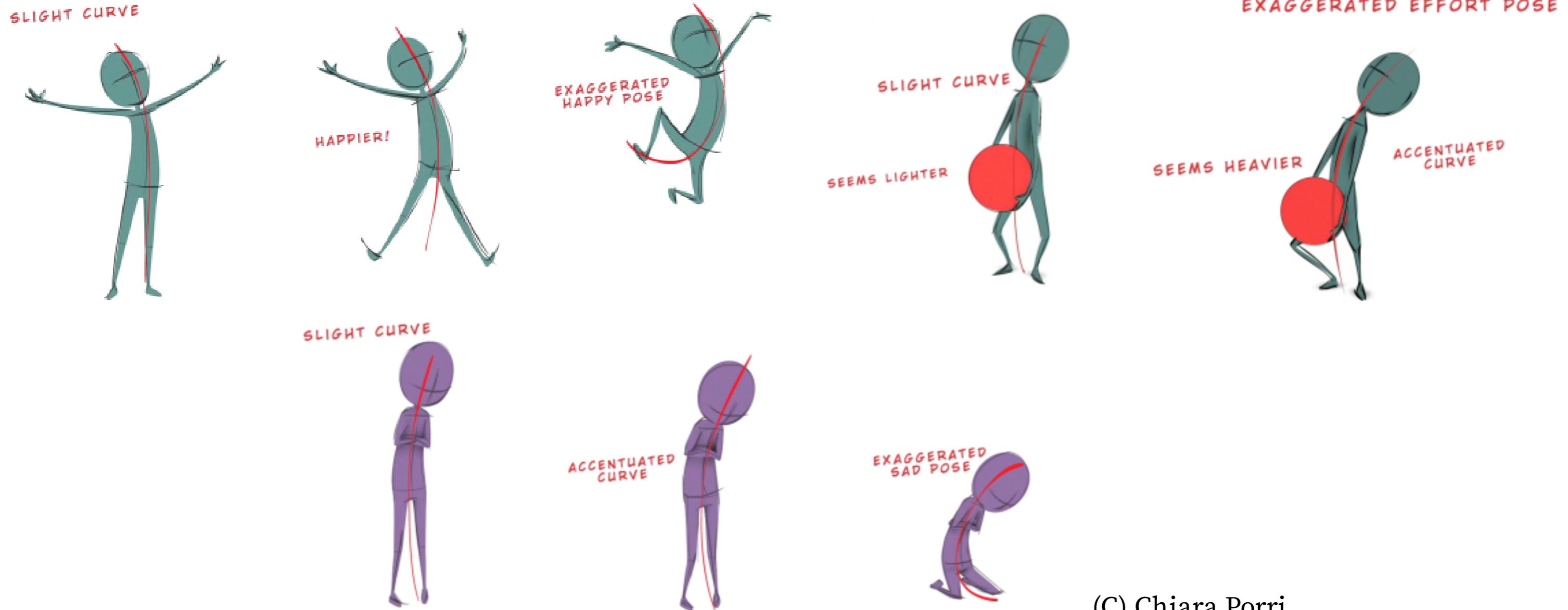
Main software: Nuke (Foundry)



Expressive Animation

Character Animation Posing - Line of Action

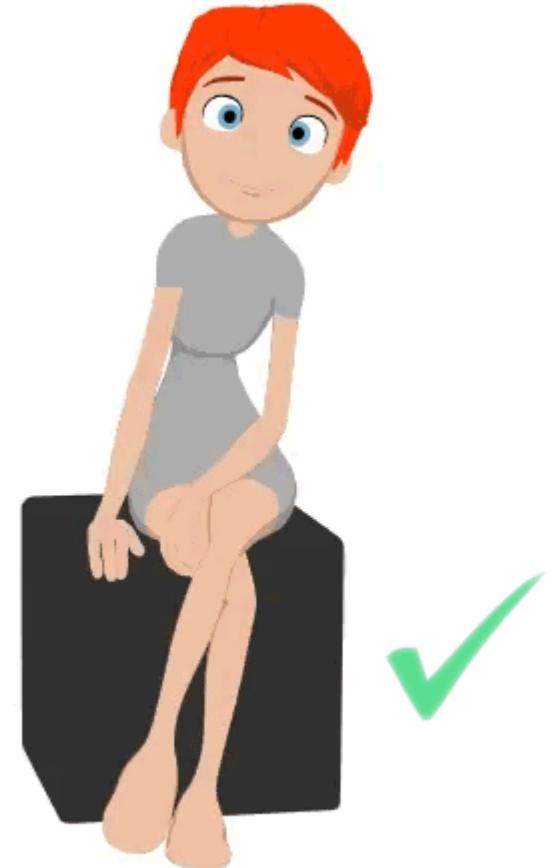
- Line of action: *Medial axis* expressing the character pose
- Express *statically* the dynamic of the action
 - Unstable pose \Rightarrow Dynamic action/motion



Principles of animation

- Interpolation between realistic poses isn't enough for expressive animation
- *12 principles of animation* by Disney *Illusion of Life*, 1981

1. Timing
2. Spacing
3. Slow-in, Slow-out
4. Squash & Stretch
5. Anticipation
6. Follow Through
7. Secondary Action
8. Exaggeration
9. Appeal
10. Arcs
11. Staging
12. Straight Ahead/Pose to Pose

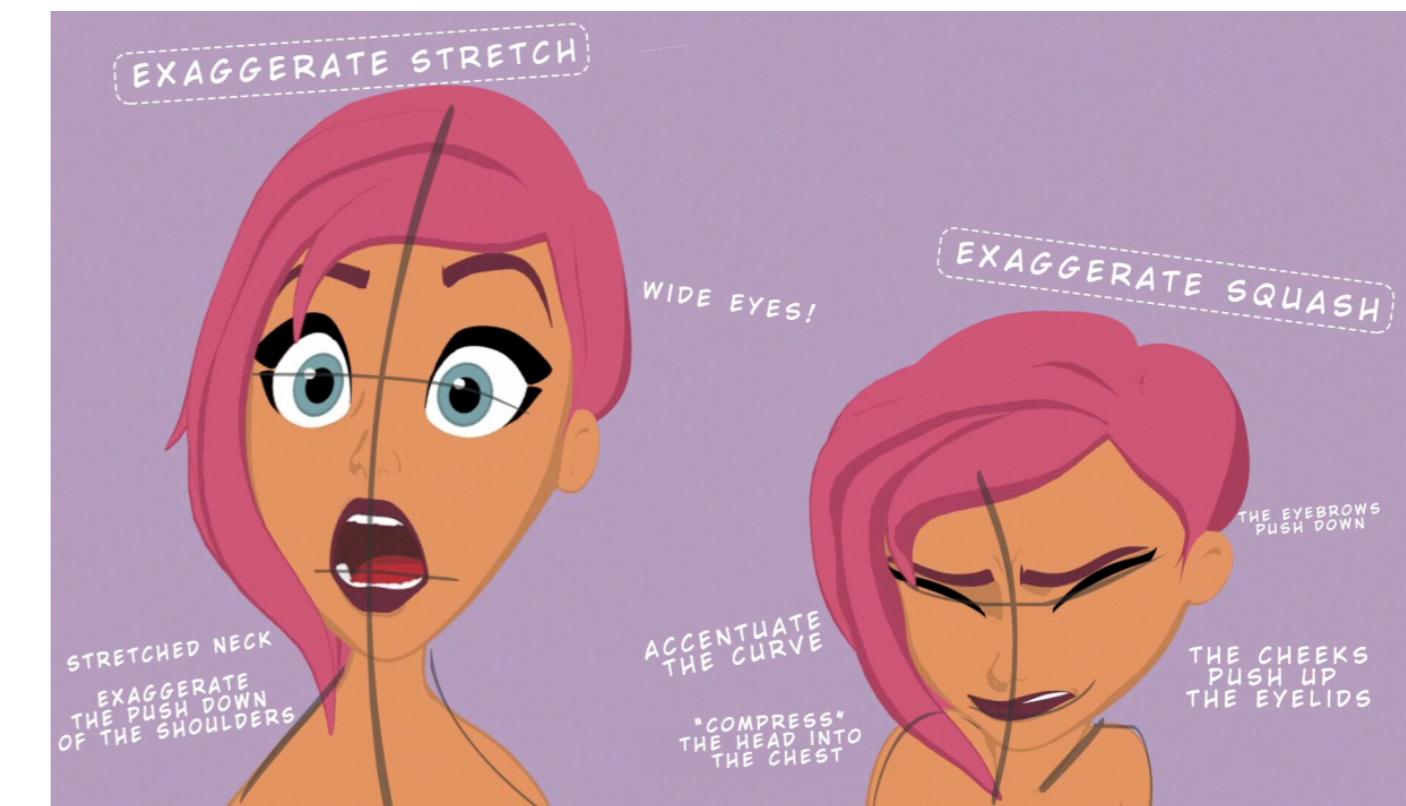
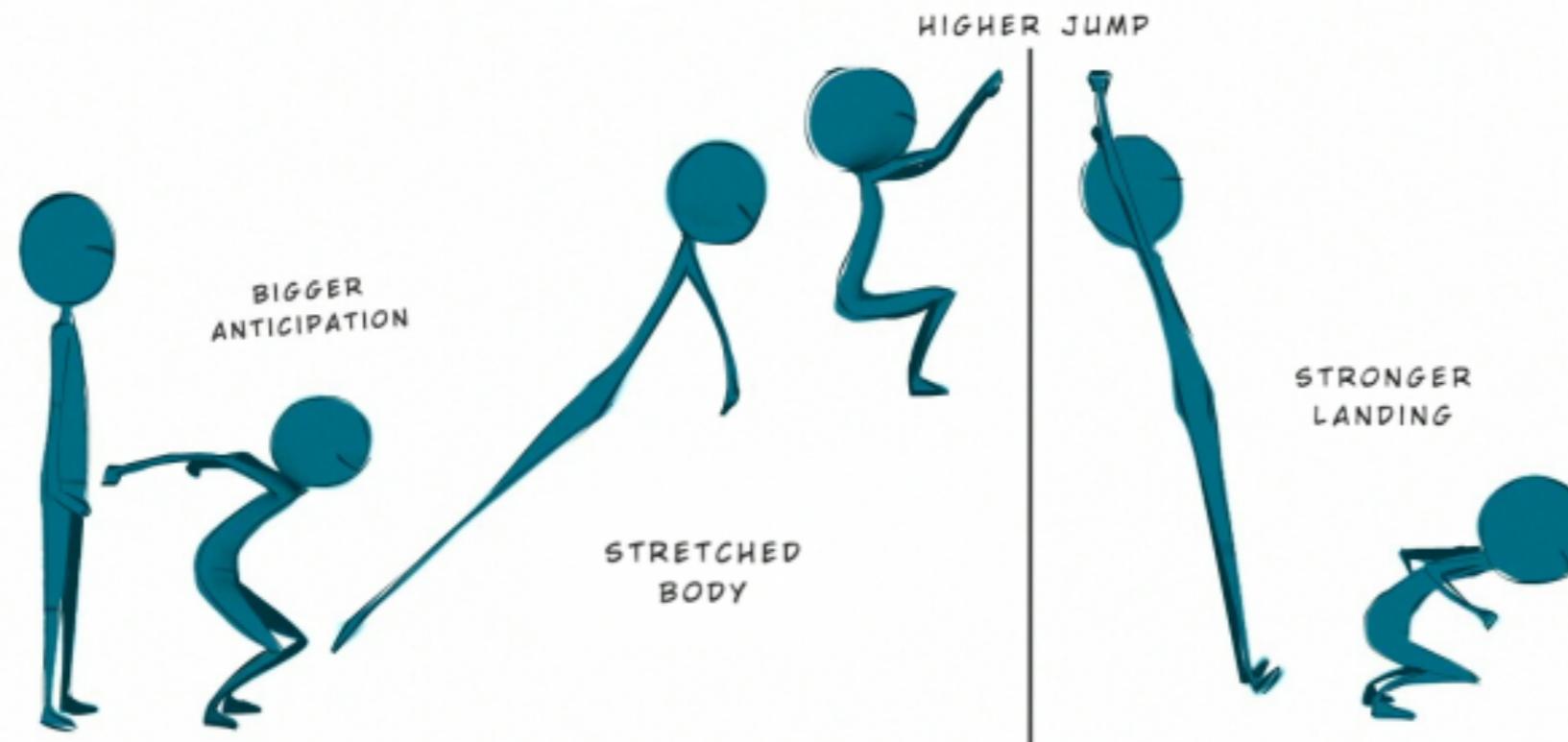
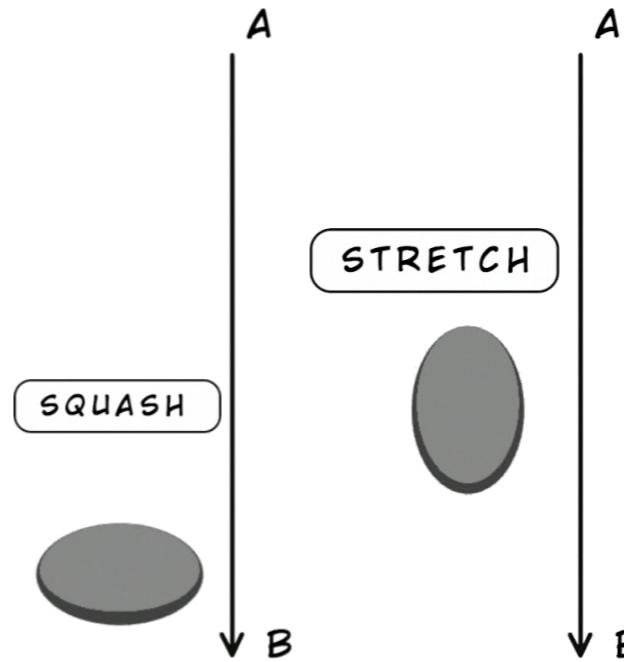


(C) Chiara Porri

Expressive animation

Squash & Stretch

- Very common in cartoon
- Unrealistic, but surprisingly *plausible*



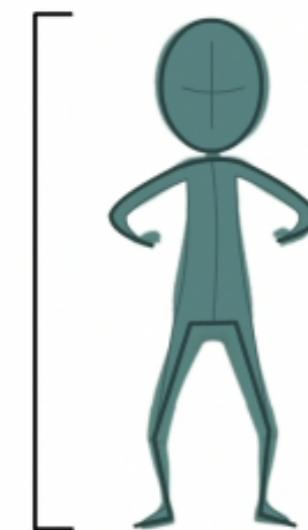
(C) Chiara Porri

Expressive animation

Anticipation

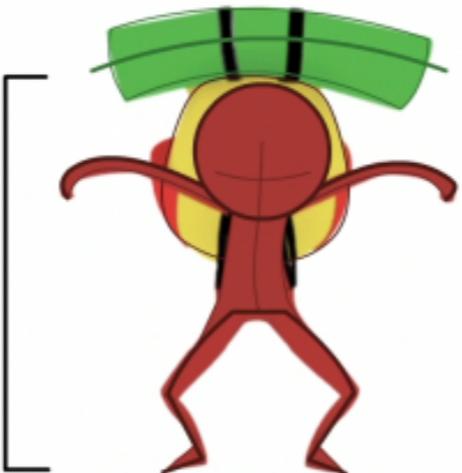


the character is pretty light



Softer Anticipation

the character is bringing an heavy object

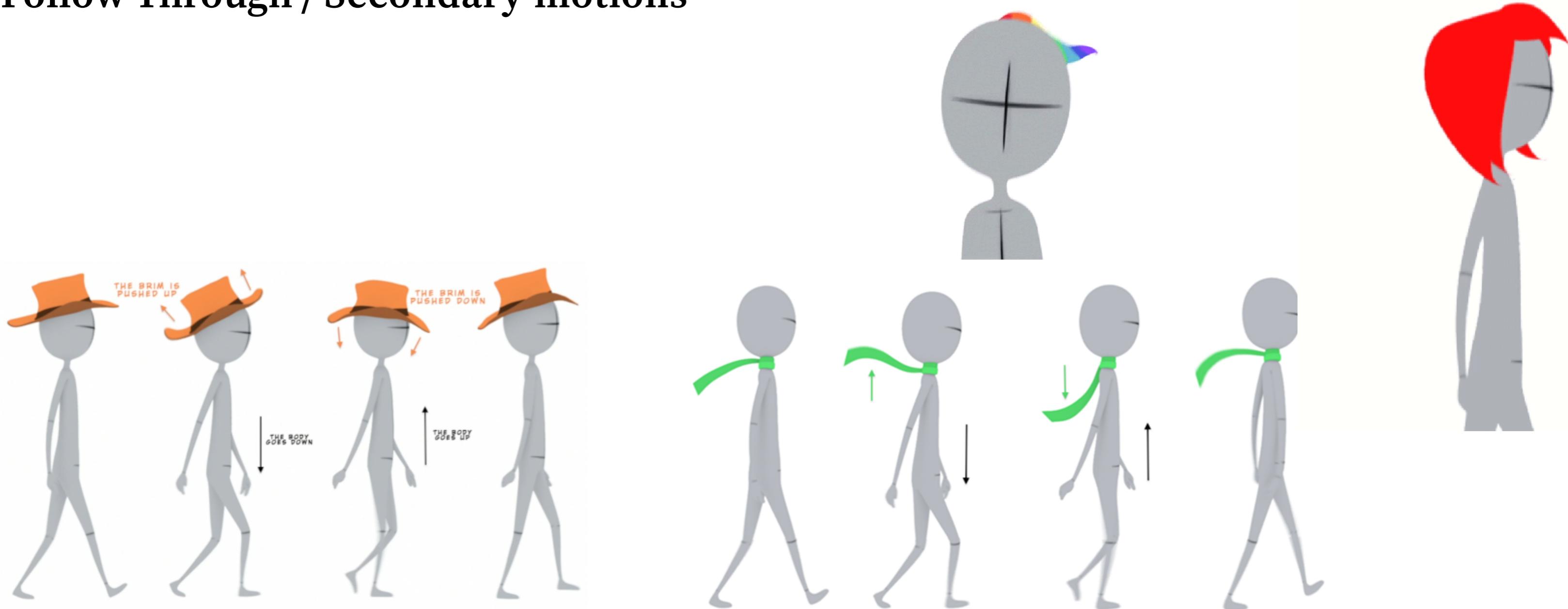


Stronger Anticipation



Expressive animation

Follow Through / Secondary motions



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